

# Precision Studies of QCD in the Low Energy Domain of the EIC

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## FOREWORD

In June 2020, an international team of nuclear scientists was assembled and submitted a proposal to the Center for Frontiers in Nuclear Science (CFNS) for an initiative to organize a series of workshops and discussions on the science and instrumentation of the second Interaction Region for the Electron-Ion-Collider (EIC). The initial team was composed by V. Burkert (JLab), M. Contalbrigo (INFN-Ferrara), A. Deshpande (Stony Brook), L. Elouadrhiri (JLab), H. Gao (Duke), B. Jacak (LBL), R. Milner (MIT), and F. Sabatie (Saclay/CEA). It was later extended to include J. Arrington (LBL), Y. Oh (APCTP), A. Vossen (Duke) and X. Ji (UMD).

This initiative followed DOE’s approval of “mission need” (known as CD-0) in December 2019 on a one-of-a-kind nuclear physics research facility to be built at DOE’s Brookhaven National Laboratory on Long Island with Jefferson Laboratory in Newport News, Virginia as a major partner. Since then the EIC has achieved Critical Decision 1 (CD-1) approval on July 6, 2021. This milestone marks the start of the project execution phase for a next-generation nuclear physics facility that will probe the smallest building blocks of visible matter, making the present initiative timely.

The EIC is designed to have two interaction regions that are suitable for the installation of large-scale detector systems for high priority nuclear physics experiments. The goal of this initiative was to take a fresh look at the changing landscape of the science underlying the need of a complementary approach towards the overall optimization and the execution of the EIC science program, and include, where appropriate, recent scientific advancements and challenges that go beyond the original motivation for the EIC. Several of the highly rated science programs proposed for the EIC were selected, as well as recent developments that have opened up new directions in nuclear science. It also included discussions on the machine requirements and performance of detection systems for the successful and efficient execution of the EIC science program.

The organizing team held a preparatory coordination meeting on December 15–16, 2020 [1] bringing in experts in the field to discuss the science of the EIC second interaction region, its instrumentation, and explore ways of its implementation in order to maximize the scientific impact of the EIC. The goal of this meeting was also to define the scientific program and the agenda for subsequent workshops.

The first workshop took place remotely on March 17-19, 2021, and was co-hosted by Argonne National Laboratory and the CFNS. Over 400 members of the international nuclear science community registered as participants [2]. This first workshop highlighted the science that will benefit the most from a second EIC interaction region, including the science of deep inelastic exclusive and semi-inclusive processes, the physics with jets, heavy flavor production, spectroscopy of exotic hadrons, and processes with light and heavy ions. This workshop was very timely as Brookhaven National Laboratory and Jefferson Laboratory had just announced the “Call for Collaboration Proposals for Detectors to be located at the EIC” in two interaction regions. Detector 2 could complement the project detector 1 and may focus on optimizing particular science topics or addressing topics beyond the requirements defined in previous published EIC documents. It also refers to possible optimization of the second interaction region towards such aims.

The second workshop [3] Precision Studies of QCD at EIC, co-hosted by Asia Pacific Center for Theoretical Physics (APCTP) and the CFNS, took place on July 19-23, 2021. This workshop examined the science requiring high luminosity at low to medium center of mass energies (20 to 60 GeV). The goal of this workshop was to motivate the study of high impact science in the context of the overall machine design, EIC operation, and detector performance, focusing on science highlights, detector concepts, and science documentation. As a result of this workshop technical working groups were formed to develop this white paper. It identifies part of the science program in the precision studies of QCD that require or greatly benefit from the high luminosity and low to medium center-of-mass energies, and it documents the scientific underpinnings in support of such a program. The objective of this document is to help define the path towards the realization of the second interaction region.

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## Executive Summary

The fundamental building blocks of ordinary matter in the universe, proton and neutron, together known as nucleons, have been discovered during the early part of the twenties century [4, 5]. For over half a century we have known that these nucleons are further composed of quarks and gluons. We also know that global properties of nucleons and nuclei, such as their mass and spin, and interactions are the consequences of the underlying physics of quarks and gluons, governed by the theory of strong interaction, Quantum-Chromo-Dynamics (QCD), whose fifties anniversary we celebrate in 2022. Yet we still do not understand how the properties of nucleons emerge from the fundamental interaction. This has resulted in the development of a new science of emergent phenomena in the nuclear medium and the 3D nuclear structure: nuclear femtography. A significant part of the science program currently at the Jefferson Laboratory 12 GeV CEBAF facility is aimed at this new science in the range where valence quarks dominate the internal structure and dynamics; the US Electron Ion Collider (EIC) in its low-to-medium center-of-mass energy is preferential for studying the region of  $x_B$  from 0.01 to 0.1 where non trivial flavor and quark-anti-quark differences are expected from Chiral Symmetry Breaking.

These capabilities will open the door to the exploration of the three-dimensional distributions in coordinate space and in momentum space of the quarks and gluons over an unprecedented kinematic range that connects to the range currently explored at lower energies in fixed-target scattering experiments. The combined result will be an unparalleled exploration of the way in which the phenomena of nuclear physics, the mass, and the spin, and the mechanical properties emerge from the fundamental interactions of the partons, and how these properties are distributed in the confined space inside nucleons and nuclei.

The EIC in its full range of 20 to 140 GeV center-of-mass energy and featuring high luminosity operation will be a powerful facility for the exploration of the most intricate secrets of the strong interaction, and the potential discovery of phenomena not observed before. Much of the compelling science program has been described in previous documents [6–8].

The EIC project scope includes the development of an interaction regions (IR) and day-one detector at IP6 and the baseline of an interaction region design for a second detector at IP8. A second EIC detector would be located at IP8 that will include a second focus approximately 50 m downstream of the collision point at a location with a large dispersion. Such an innovative design would enable a high-impact and highly complementary physics program to the day-one detector. The second focus thus makes it possible to move tracking detectors very close to the beam at a location where scattered particles separate from the beam envelope, thereby providing exceptional near-beam detection. This in turn creates unique possibilities for detecting all fragments from breakup of nuclei, for measuring light nuclei from coherent processes down to very low  $p_T$ , and greatly improves the acceptance for protons in exclusive reactions - in particular at low  $x$ . As such, a second detector at IP8 will significantly enhance the capabilities of the EIC for diffractive physics and open up new opportunities for physics with nuclear targets.

With this document we highlight the science benefiting from an optimized operation at instantaneous luminosity from  $0.5 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$  up to  $1.0 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$  is achievable in the center-of-mass range of 45 to 100 GeV, with significantly lower luminosity at 28 and 140 GeV. Furthermore, with a projected  $10^7$  sec of operation (100% equivalent) annually, the maximal integrated luminosity is  $100\text{fb}^{-1}$ .

This White Paper aims at highlighting the important benefits in the science reach of the EIC. High luminosity operation is generally desirable, as it enables producing and harvesting scientific results in a shorter time period. It becomes crucial for programs that would require many months or even years of operation at lower luminosity.

We also aim at providing the justification for the development of either or both EIC detectors with characteristics that will provide support for an exciting science program at low to medium-high center-of-mass electron-ion collisions that address many of the high impact physics topics. In particular, the 3D-imaging of the nucleon, requiring a large amount of data in order to fill the multi-dimensional kinematic space with high statistics data, including combinations of spin-polarized electrons and longitudinal and transverse spin-polarized protons. We also emphasize the importance of, in the future, including positrons for processes that can be isolated through the measurement of electrical charge differences in electron and positron induced processes. Furthermore, the availability of high spin polarization for both the electron and proton beam, in the longitudinal and in the transverse spin orientation, is critically important for the measurement of the quark angular momentum distribution in the proton.

**Generalized Parton Distributions:** The discovery of the Generalized Parton Distributions (GPDs) and the identification of processes that are accessible in high energy scattering experiments, has opened up an area of research with the promise to turn experimentally measured quantities into objects with 3-dimensional physical sizes at the femtometer scale. It requires precision measurements of exclusive processes, such as deeply virtual Compton scattering (DVCS) and deeply virtual meson production (DVMP). The tunable energy of the EIC combined with an instantaneous luminosity of up to  $L = 10^{34} \text{cm}^{-2}\text{s}^{-1}$  and high spin polarization of electrons, proton, and light nuclei, makes the EIC a formidable instrument to advance nuclear science from the one-dimensional imaging of the past to the 3-dimensional imaging of the quark and gluon structure of particles. For the quark structure this is shown in Fig. 7.



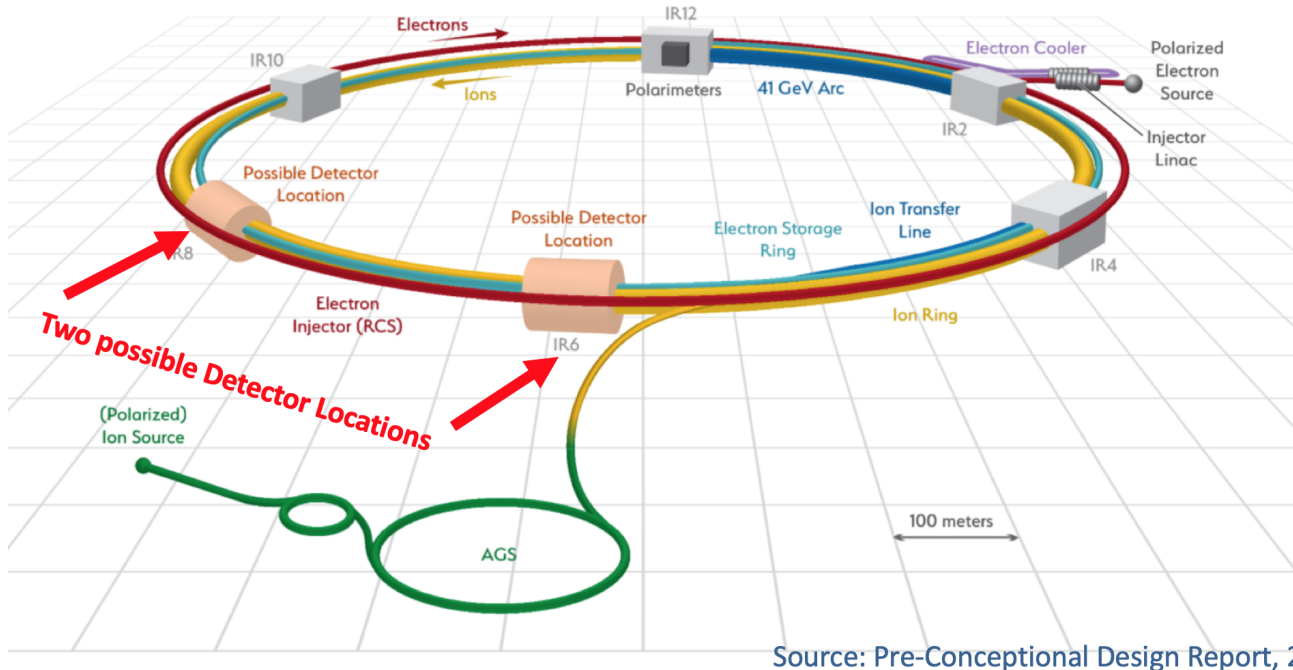


FIG. 1. The EIC concept at Brookhaven National Laboratory [9]. The electron and the ion beams are clearly identified. There are several beam intersection points, one at the 6 o'clock (IP6) location and at the 8 o'clock (IP8) location are suitable for the installation and operation of large scale detector systems. Interaction point IP8 may be most suitable for high-luminosity optimization at low to intermediate center-of-mass energies as well as for the installation of a secondary focus for forward processes requiring high momentum resolution. The electron beam energy ranges from 2.5 GeV to 18 GeV, while for protons the ion beam allows selected energies between 41 GeV and 275 GeV covering a collision center-mass energy from 20 GeV to 140 GeV. The ion beam is circulating counter clockwise, and the new electron ring with electrons circling clockwise. Both beams will be highly polarized with both electron and proton polarizations greater than 70%. The EIC will benefit from two existing large detector halls in IP6 and in IR8, both fully equipped with infrastructure.

57 This science is one of the cornerstones of the EIC experimental program and is complemented by theoretical advances  
 58 as a result of precise computations on the QCD lattice and through QCD-inspired pictures of the nucleon. To fully  
 59 capitalize on these experimental and theoretical efforts demands operation of the EIC with high luminosity at low to  
 60 medium center of mass energies. This will enable connecting the valence quark region, which is well probed in fixed  
 61 target experiments, to sea quarks and gluon dominated regions at medium and small values of the quark longitudinal  
 62 momentum fraction  $x$  correlating the quarks spatial distribution with its momentum. The great potential of the EIC  
 for imaging is illustrated in Fig. 7 with the extraction of Compton Form Factor  $\mathcal{H}$  covering a large  $x$  range.

63  
 64 **Gravitational Form Factors:** Knowledge of the GPDs facilitated the development of a novel technique to employ  
 65 the correspondence of the GPDs to the gravitational form factors (GFFs) through the moments of the GPDs. The  
 66 GFFs are form factors of the nucleon matrix element of the energy-momentum tensor and are related to the mechanical  
 67 properties of the proton. The Fourier transform over their  $t$ -dependence can be related to the distribution of forces,  
 68 of mass, and of angular momentum. The femto-scale images obtained will provide an intuitive understanding of the  
 69 fundamental properties of the proton, and how they arise from the underlying quarks and gluon degrees of freedom  
 70 as described by the QCD theory of spin-1/2 quarks and spin-1 gluons. This is one of the most important goals in  
 71 nuclear physics. The feasibility of this program has been demonstrated at experiments at lower energy, and expected  
 results at the EIC have been simulated.

72  
 73 **Mechanical Properties of Particles:** In the QCD studies, it has been realized that the matrix elements, and the  
 74 quark and gluon GFF, measured through DIS momentum sum rule and also the source for gravitational fields of the  
 75 nucleon, play important roles in understanding the spin and mass decomposition. The interpretation of the GFF  
 76  $D(t)$  in terms of mechanical properties has most recently generated much interest as its relations to deeply virtual  
 77 Compton scattering (DVCS) and deeply virtual meson production (DVMP) have been established. Moreover, the

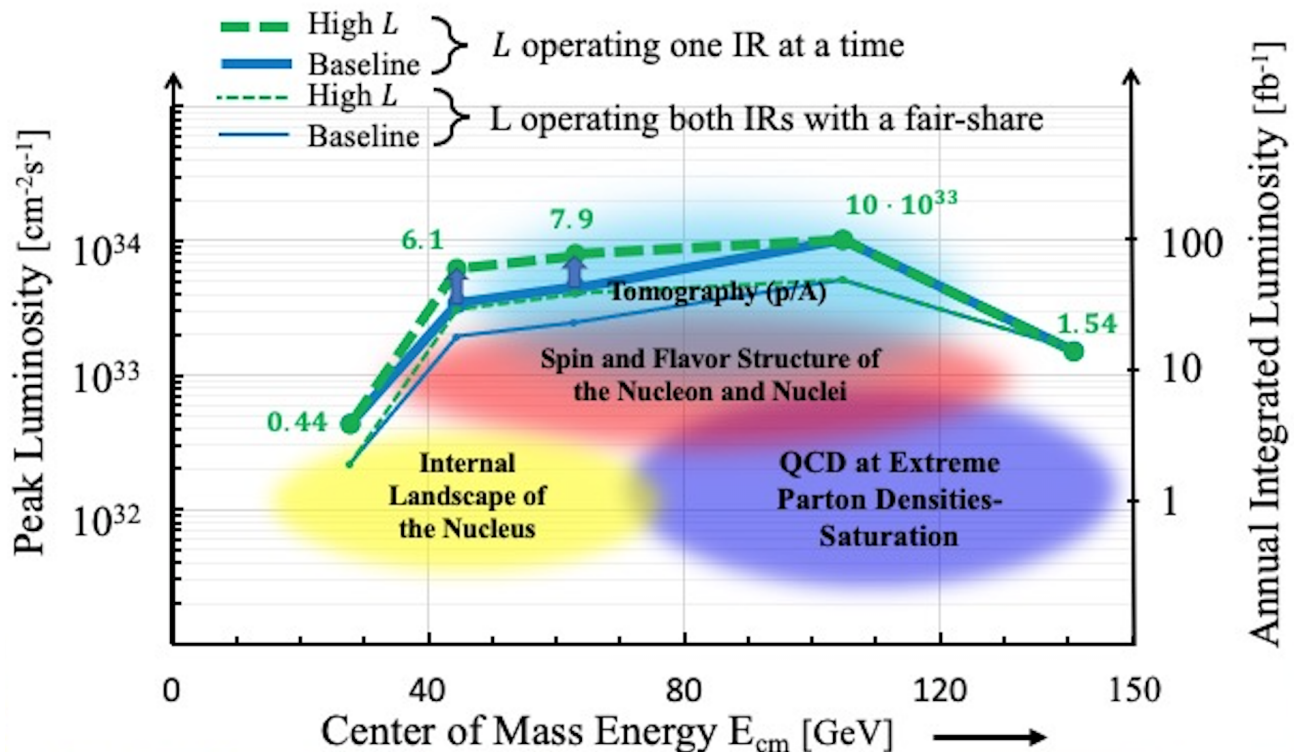


FIG. 2. Estimated luminosity versus center-of-mass energies for the operation of one (thick lines) or two (thin lines) interaction regions. The blue lines show the baseline performance. The green lines show the high luminosity operation for improved beam optics and cooling. The strong drop in luminosity from the CM energy 44.7 GeV to 28.6 GeV is caused by increased beam-beam interactions as the proton beam energy is reduced from 100 GeV to 41 GeV while keeping the electron energy of 5 GeV. This problem is still being studied by machine experts. One option might be to keep the proton energy at 100 GeV, thus avoiding an increase in beam-beam interactions and lower the electron beam energy from 5 GeV to 2.5 GeV, resulting in 31.6 CM energy.

78 gluon GFF are directly accessible through near-threshold heavy-quarkonium production as well. Furthermore, the  
 79 beam charge asymmetry in DVCS with a future positron beam will have important impact in directly accessing the  
 80  $D(t)$  form factor [10]. Figure 13 shows examples of estimated normal and shear force distributions inside the proton  
 that will become accessible with the EIC.

81

82 **Nuclear Structure in Momentum Space:** As the GPDs relate to imaging in transverse Euclidean and longitu-  
 83 dinal momentum space, the nucleon's 3-dimensional momentum structure may be accessed through measurements of  
 84 transverse momentum dependent parton distribution functions employing semi-inclusive deep-inelastic scattering as  
 85 a central part of the scientific mission of the EIC. This program focuses on an unprecedented investigation of the  
 86 parton dynamics and correlations at the confinement scale and will benefit substantially by an increased luminosity at  
 87 medium energies. Structure functions appearing at sub-leading twist are suppressed by a kinematic factor  $1/Q$ , which  
 88 makes data at relatively low and medium  $Q^2$  the natural domain for their measurement. Similarly, effects from the  
 89 intrinsic transverse momentum dependence are suppressed at high  $Q^2$ , when most of the observed transverse momenta  
 90 are generated perturbatively. As a consequence, the signal of TMDs is naturally diluted at the highest energies. At  
 91 the same time  $Q^2$  has to be high enough for the applicability of factorization theorems.

92 Dedicated running of the EIC at low to medium CM energy would therefore occupy kinematics where non-  
 93 perturbative and subleading effects are sizeable and current knowledge allows the application of factorization to  
 94 extract the relevant quantities [11]. The strong impact of a high luminosity EIC on the determination of the structure  
 function  $g_T$  is demonstrated in Figure 17 in comparison with the existing data.

95

96 **Exotic Mesons in Heavy Quark Spectroscopy:** The spectroscopy of excited mesons and baryons has played an  
 97 essential role in the development of the quark model and its underlying symmetries, which led to the decoding of what  
 98 was then called the "Particle Zoo" of hundreds of excited states. Modern electro/photo-production facilities, such as  
 99 those operating in Jefferson Lab, have demonstrated the effectiveness of photons as probes of the hadron spectrum.

100 However the energy ranges of these facilities are such that most states with open or hidden heavy flavor are out of  
 101 reach. Still, there is significant discovery potential for photoproduction in this sector. Already electron scattering  
 102 experiments at HERA observed low-lying charmonia, demonstrating the viability of charmonium spectroscopy in  
 103 electro-production at high-energies but were limited by luminosity. Now the EIC, with orders of magnitude higher  
 104 luminosity, will provide a suitable facility for a dedicated photoproduction spectroscopy program (by post-tagging  
 105 the near  $0^\circ$  scattered electron) extended to the heavy flavor sectors. In particular, the study of heavy-quarkonia and  
 106 quarkonium-like states in photon-induced reactions while complementary to the spectroscopy programs employing  
 107 other production modes will provide unique clues to the underlying non-perturbative QCD dynamics.

108 **Unique science with nuclei:** The EIC will enable deep inelastic scattering off of all nuclei with its polarized electron  
 109 beam for the first time in a collider geometry. Lightest nuclei like deuteron or helium would serve as surrogates for  
 110 neutrons to study flavor dependent parton distributions in kinematic regions that remain unexplored to-date. EIC's  
 111 high luminosity and unique far-forward detection capabilities will enable detailed measurements of nuclear breakup,  
 112 spectator tagging, and – in the case of light ions – coherent scattering reactions, far beyond what is possible in the  
 113 past fixed target facilities. Such measurements, would allow additional valuable controls over measurements and  
 114 promise to understanding reaction mechanisms and to study nuclear configurations that are believed to play crucial  
 115 role in the scattering process. Coherent scattering measurements in exclusive reactions enable 3D tomography of  
 116 light ions in their quark-gluon degrees of freedom. Nuclei can be used to study the influence of nuclear interactions  
 117 on non-perturbative properties of the nucleon (nuclear medium modifications). Precision measurements of the  $Q^2$   
 118 dependence of the EMC effect will pin down the influence of higher twist contributions on the medium modifications  
 119 of partonic distributions. The broad Bjorken- $x$  range covered by the EIC makes it an ideal machine to study the  
 120 gluon EMC effect.

121 **Paper organization:** The WP is organized in 10 sections, with section I through section V outlining an experimental  
 122 science program. Section VI is dedicated to the increasing role Lattice QCD will play in supporting the high level  
 123 experimental analysis, as well as opening up avenues of research that require information not (yet) available from prior  
 124 experiments for the interpretation. Section VII discusses aspects of the science requiring special instrumentation in the  
 125 far forward region of the hadron beam, and for the second interaction region at IP8 the option of implementing a high-  
 126 resolution forward ion spectrometer. Radiative effects are discussed in section VIII, which all experimental analyses  
 127 have to deal with, and may present special challenges in part of the phase space covered by the EIC detection system,  
 128 covering nearly the full phase space available. Section IX outlines some of the experimental and analysis aspects  
 129 that offer significant benefits from developing and employing artificial intelligence (AI) procedures in controlling  
 130 hardware and in guiding analysis strategies that can be widely developed before that EIC will begin operation.  
 131 Section X discusses the two interaction regions that can house dedicated detector systems, with emphasis on their  
 132 complementarity in performance at different center-of-mass energies and optics parameters.

## I. GPDS - 3D IMAGING AND MECHANICAL PROPERTIES OF THE NUCLEON

### A. Introduction & background

The discovery of GPDs [12–14] has opened a window on three-dimensional imaging of the nucleon, going far beyond the one dimensional longitudinal structure probed in deeply inelastic scattering (DIS) and the transverse structure encoded in the different form factors. This discovery facilitated the development of a novel technique that employs the remarkable correspondence of the GFF and the second x-moments of the generalized parton distribution functions, and relate them to the shear stress and pressure in the proton and the distribution of orbital angular momentum. These femto-scale images (or femtography) will provide an intuitive understanding of how the fundamental properties of the nucleon, such as its mass and spin, arise from the underlying quark and gluon degrees of freedom. And then, for the first time, we will have access to the forces and pressure distributions inside the nucleon. This science is one of the cornerstones of the EIC experimental program and is complemented by theoretical advances as a result of lattice QCD calculations and through QCD-inspired pictures of the nucleon. To fully capitalize on these experimental and theoretical efforts demands operation of the EIC with high luminosity at low to medium center of mass energies.

The standard approach of imaging is through diffractive scattering. The deeply virtual exclusive processes allow probing entirely new structural information of the nucleon through QCD factorization (see Fig.3).

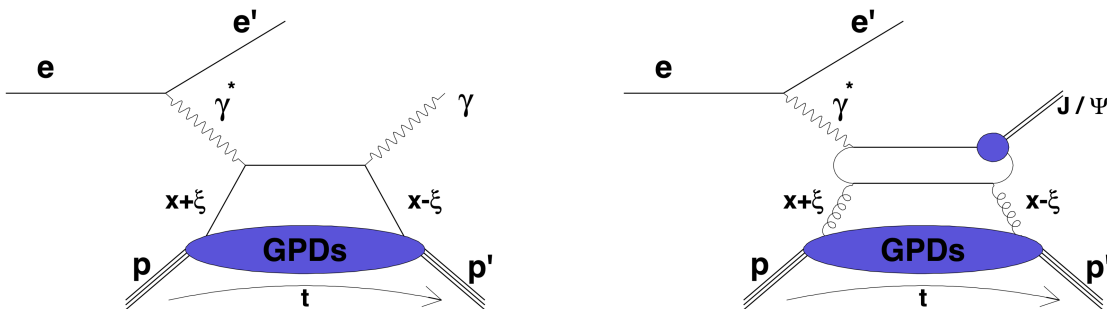


FIG. 3. Deeply virtual exclusive processes in electron scattering, as hard scattering events to probe the 3D quark distribution (left) and gluon distribution (right).

The golden process to study the quark GPDs is DVCS, where a virtual photon interacts with a single quark deep in the hadron, and the quark returns to the hadron initial ground state by emitting a high energy photon in the final state. Experimental observables in DVCS are parameterized by Compton Form Factors (CFFs) [15]. From the analysis of data from DESY, as well as the results of new dedicated experiments at JLab, and at CERN, early experimental constraints on CFFs have been obtained from global extraction fits [16–19]. However, data covering a sufficiently large kinematic range, and the different required polarization observables, have not been systematically available. The future EIC with high luminosity at large range in CM energies will provide comprehensive information on these hard diffractive processes, entering the precision era for GPD studies.

In what follows, after a brief review of the formalism in Section IB 1, we describe state of the art analysis methods in Section IB 2, and the study of the extraction of GFF performed at Jefferson Lab Hall B (Section IC). Additional processes sensitive to GPDs complementing the main EIC focus, as well as an outlook are presented in IE.

### B. Generalized Parton Distributions and Nucleon Tomography

GPDs, their theoretical properties, as well as phenomenological aspects related to their extraction from deeply virtual exclusive processes, have been the object of several review papers [18, 20–25] as well as of reports supporting the design of the upcoming EIC [6, 8]. The main properties of GPDs are outlined below while reminding the reader that many open questions concerning constraints on GPD models, such as the application of positivity bounds [26, 27], dispersion relations [28–32], flavor dependence [33], NLO perturbative evolution, as well as the separation of twist-2 and twist-3 contributions in the deeply virtual exclusive cross sections, are still intensely debated. The ultimate answer to many of these questions will be found in the outcome of carefully designed experiments at the EIC. It is therefore mandatory to define analysis frameworks to extract GPDs from data. Various approaches, listed in Section IB 2, have been developed which represent a new step towards realizing the goal of nucleon tomographic imaging.

1. Deeply Virtual Exclusive Processes, GPDs and Compton Form Factors

The non-perturbative part of the handbag diagram in Fig. 3(left) is parameterized by GPDs

$$\frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle p' | \bar{\psi}_q(0) \gamma^+ (1 + \gamma^5) \psi_q(y) | p \rangle = \bar{U}(p', \Lambda') \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} + \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] U(p, \Lambda) \quad (1)$$

where the index  $q$  refers to the quark flavor;  $P = \frac{1}{2}(p + p')$  is the average proton 4-momentum, while  $\Delta = p' - p$  is the 4-momentum transfer to the proton,  $t = \Delta^2$ . The Fourier transform is performed along the light-cone (LC) with  $y^+ = \vec{y}_\perp = 0$  (Fig.4).

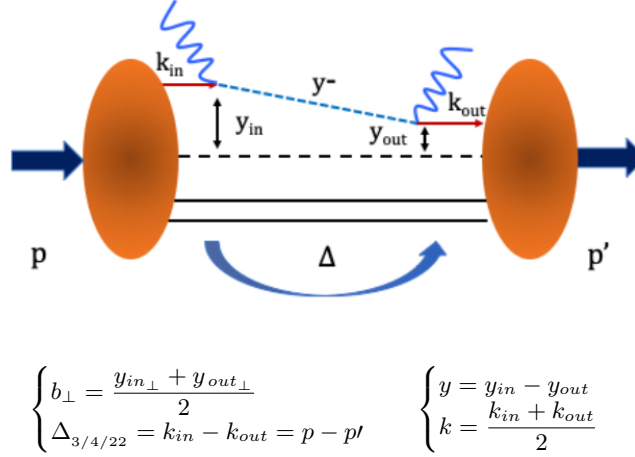


FIG. 4. Correlation function for the GPDs defined in Eq.(1), highlighting both momentum and Fourier conjugate spatial coordinates.

The active quark carries light cone momentum fractions  $x + \xi$  and  $x - \xi$ , respectively, in the initial and final states, so that the average quark LC momentum is,  $k^+ = xP^+$  and the LC momentum difference is,  $\Delta^+ = p'^+ - p^+ = -2\xi P^+$ . Ordinary parton distribution functions (PDFs) can be recovered from GPDs at  $\xi = 0, t = 0$  as,

$$\frac{1}{4\pi} \int dy^- e^{ixp^+y^-} \langle p | \bar{\psi}_q(0) \gamma^+ \psi_q(y) | p \rangle = H^q(x, \xi = 0, t = 0) = q(x) \quad (2)$$

and similarly  $\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$ . Furthermore, like ordinary parton distributions, all of the expressions considered here depend on the hard scale for the scattering process,  $Q^2$ , which is omitted in the expressions for ease of presentation. Because of Lorentz covariance, the  $n$ th Mellin moment of a GPD is a polynomial in  $\xi$  of order  $(n+1)$  [34]. Because of parity and time reversal invariance, these polynomials are even for the GPDs of spin-1/2 targets such as the proton. The coefficients of each power of  $\xi$  are functions of  $t$ , which constitute generalized form factors. For  $n=0$  in particular, the moments are independent of  $\xi$  and give the familiar elastic form factors. In section IC we will use the 2nd Mellin moments of GPD  $H$  and GPD  $E$  when discussing the GFF of the proton.

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t), \quad \int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t) \quad (3a)$$

$$\int_{-1}^1 dx \tilde{H}^q(x, \xi, t) = G_A^q(t), \quad \int_{-1}^1 dx \tilde{E}^q(x, \xi, t) = G_P^q(t) \quad (3b)$$

GPDs also encode information on the joint distributions of partons as functions of both the longitudinal momentum fraction  $x$  and the transverse impact parameter  $\vec{b}_\perp$ . For a nucleon polarized along the transverse  $X$  direction they are given by [35],

$$q_X^{In}(x, \mathbf{b}_\perp) = \int \frac{d^2 \Delta_\perp}{(2\pi)^2} \exp[i\mathbf{b}_\perp \cdot \Delta_\perp] \left[ H_q(x, 0, -\Delta^2) + i \frac{\Delta_y}{2M} (H_q(x, 0, -\Delta^2) + E_q(x, 0, -\Delta^2)) \right] \quad (4)$$

195 Figure 5 shows one of the projected results for the 2-dimensional images of the CFF  $\mathcal{E}(\xi, t)$  and  $\mathcal{H}(\xi, t)$  Fourier  
 196 transformed into impact parameter space  $(b_x, b_y)$ . The image was extracted from simulated CLAS12 measurements  
 197 of different polarization asymmetries and cross sections with the proton transversely polarized.

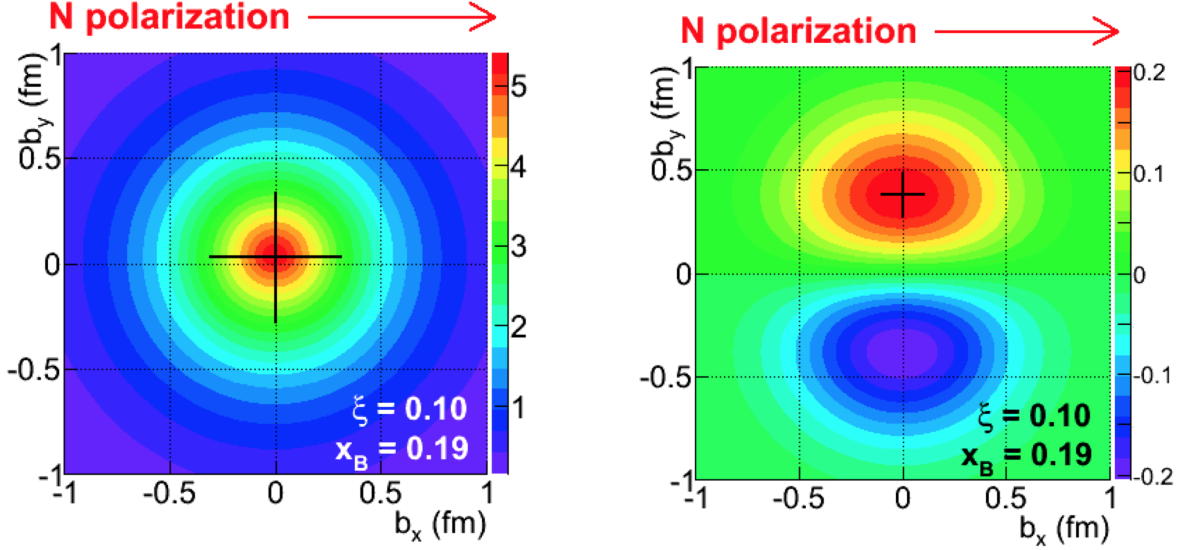


FIG. 5. Left: Image of the 2-dimensional distribution of  $\mathcal{H} + \mathcal{E}$  in the valence region for a spin-polarized proton with the polarization axis parallel to  $b_x$ . The polarization causes a vertical shift of the center. Right: Same as on the left, but showing the distribution of GPD  $\mathcal{E}$  separately, with the effect of the polarization more dramatically seen as a clear spatial separation of electrical charges, i.e. u- and d-quarks in  $b_y$  space, generating a flavor-dipole. Note that the color codes on the left and right panels have different scales to account for the much smaller amplitude of the  $\mathcal{E}$  CFF.

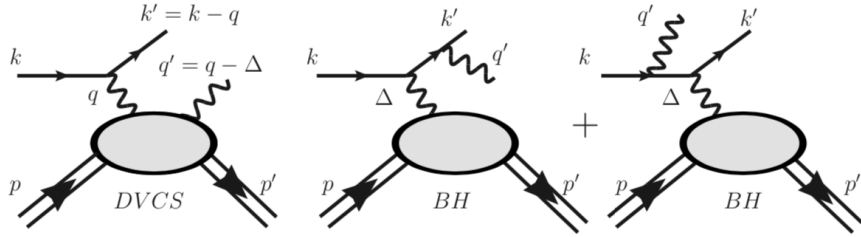


FIG. 6. Exclusive photon electroproduction through DVCS (left) and BH processes (middle and right).

198 In the following we focus on the DVCS process shown in Fig.6 (left). DVCS can be considered the prototype for all  
 199 deeply virtual exclusive scattering (DVES) experiments and as such it has been the most studied process. The DVCS  
 200 matrix elements are accessed through exclusive photoproduction,

$$201 \quad ep \rightarrow e'p'\gamma$$

202 where the final photon is produced at the proton vertex. A competing background process given by the Bethe-Heitler  
 203 (BH) reaction is also present, where the photon is emitted from the electron and the matrix elements measure the  
 204 proton elastic form factors, Fig.6 (right). The cross section is a function of four independent kinematic variables besides  
 205 the electron-proton center-of-mass energy  $\sqrt{s}$ , the scale  $Q^2$ , the skewness  $\xi$ , related to Bjorken  $x_B$  as  $\xi \approx x_B/(2-x_B)$ ,  
 206  $t$ , and the angle between the lepton and hadron planes,  $\phi$ . The CFFs are complex quantities which at leading order  
 207 in perturbative QCD, are defined through the convolution integral,

$$208 \quad \mathcal{F}(\xi, t; Q^2) = \int_{-1}^1 dx \left[ \frac{1}{\xi - x - i\epsilon} \pm \frac{1}{\xi + x - i\epsilon} \right] F(x, \xi, t; Q^2), \quad (5)$$

where  $\mathcal{F} = \mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}$ , and  $\pm$  indicates helicity independent (-) or helicity dependent (+) GPDs. Figure 7 displays estimates of  $x_B \text{Re}\mathcal{H}$  and  $x_B \text{Im}\mathcal{H}$  at fixed value of  $t$ .

It is however important to keep in mind that a study of various processes is necessary to access GPDs in a controllable way. Firstly, the time-like counterpart of DVCS, named time-like Compton scattering (TCS) [36, 37], accessed through the nearly forward photoproduction of a lepton pair  $\gamma N \rightarrow \gamma^* N'$  is crucial to test the universality and the analytical properties (in  $Q^2$ ) of the factorized scattering amplitude [38]. Deeply virtual meson production (DVMP) amplitude has also been proven to factorize but current data seem to delay the onset of the scaling regime, which makes the study of the process ( $\gamma^* N \rightarrow \mathcal{M} N'$ ) an important laboratory for the study of next to leading twist processes. Secondly, a new class of factorized amplitudes has emerged [39] where the hard scattering process is a  $2 \rightarrow 3$  process. The case of the process  $\gamma N \rightarrow \gamma \gamma N'$  with a large invariant mass of the diphoton [40, 41] and a quasi-real or virtual initial photon is particularly interesting since it probes the charge-conjugation odd part of the quark GPDs in contradistinction with the DVCS/TCS probe. Other processes where a meson-meson [42] or photon-meson pair (with a large invariant mass) is produced have been studied [43, 44]; when a transversely polarized  $\rho$  meson enters the final state, they should give access to the eluding transversely quark GPDs.

The electroweak production of a single charmed meson has also been proposed [45] to access in a new way these transversely quark GPDs. Reconstructing the final state  $D$  or  $D^*$  meson is however an experimental challenge.

All these new reactions have quite small cross-sections and would greatly benefit from a high luminosity option in the low energy range of the EIC. More detailed feasibility studies need to be performed but first order of magnitude estimates show that they need a quite large coverage of photon detection which seems in line with current detector designs.

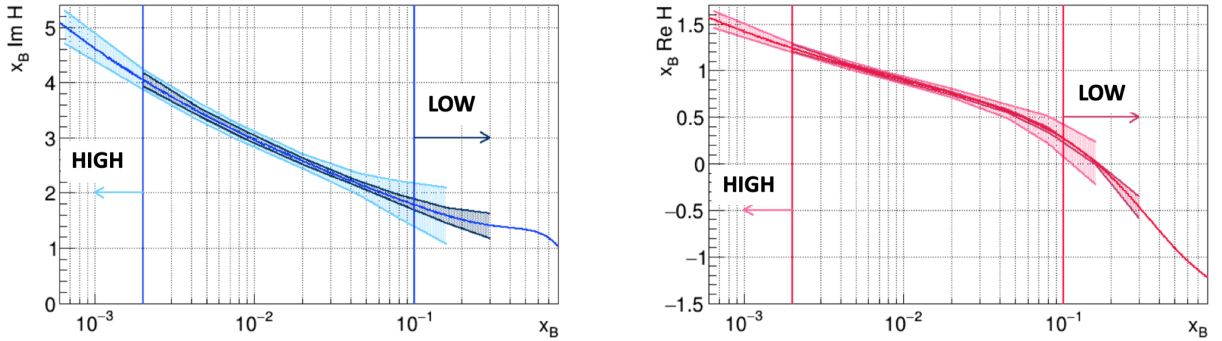


FIG. 7. Compton form factors  $\text{Im}\mathcal{H}$  and  $\text{Re}\mathcal{H}$  extracted at local  $x_B$  values from simulated DVCS events at different CM beam energies,  $\sqrt{s} = 31.6$  GeV (LOW) and  $\sqrt{s} \geq 100$  GeV (HIGH). The dark shaded bands represent the reach and the uncertainties at the lower CM-energy. The lighter shaded bands represent the higher CM-energy. The  $x_B$  regions labeled LOW can only be covered at the low CM-energy with reasonable uncertainties. The  $x_B$  region labeled HIGH can only be reached with the high CM-energy. The widths of the bands indicate the estimated uncertainties due to overall reconstruction effects, statistics and systematic uncertainties. For each of the two CM-energies a combined integrated luminosity of  $200 \text{ fb}^{-1}$  equally split between longitudinally polarized and transversely polarized proton runs is assumed. At  $x_B > 0.1$  smaller uncertainties can be achieved at the low CM-energy, which provides overlapping  $x_B$  kinematics with the JLab 12 GeV experiments (not shown). The region  $x_B < 2 \times 10^{-3}$  can only be reached at the high CM-energy. Note, that the CFF  $\mathcal{E}$  and  $\tilde{\mathcal{H}}$  are determined simultaneously. Here we have used same integrated luminosity for the two CM energies. The results are statistics limited and may be scaled for different assumptions. Regarding the luminosity assumptions at the low CM energy see comments in the caption of Fig. 2.

## 2. Analysis methods

GPDs are projections of Wigner distributions that give access to the unknown mechanical properties of the nucleon involving both space and momentum correlations. Among these are the quark and gluon angular momentum, along with spin directed  $qqg$  interactions [18, 21–25]. An accurate knowledge of GPDs would unveil an unprecedented amount of information on nucleon structure and on the working of the strong interactions. Nevertheless, after two decades of experimental and phenomenological efforts, it has been, so far, impossible to extract these important quantities directly from experiment. The problem lies at the core of their connection with observables: the cleanest probe to observe GPDs is from the matrix elements for deeply virtual Compton scattering (DVCS) (Fig.6, and Sec.IB). In a nutshell, GPDs are multi-variable functions depending on the kinematic set of variables,  $x, \xi, t, Q^2$  (see eq.[1]), which enter the DVCS cross section in the form of convolutions with complex kernels, calculable in perturbative

QCD, known as Compton Form Factors (CFFs). Furthermore, because GPDs are defined at the amplitude level, they appear in bilinear forms, in all observables, including various types of asymmetries. An additional consequence is that all four GPDs,  $H$ ,  $E$ ,  $\tilde{H}$ ,  $\tilde{E}$ , enter simultaneously any given beam/target spin configuration. It is therefore necessary to consider simultaneously a large array of different observables in order to extract the contribution of each individual GPD, even before addressing the issues of their flavor composition, and of the sensitivity of observables to quark/antiquark components (for a detailed analysis of the DVCS cross section we refer the reader to [46–48]).

For high precision femtography, which is required to obtain proton structure images, the hadron physics community has been developing sophisticated analyses. The success of Machine Learning (ML) methodologies in modeling complex phenomena make this a prime choice for GPD extraction.

Three main frameworks using ML are currently being pursued aimed at the extraction of GPD from data, which differ in the techniques, methodologies, and in the types of constraints derived from theory. In this respect, it has become clear that the use of lattice QCD results will be indispensable in GPD analyses [49, 50] and efforts in this direction are under way.

The Zagreb group [16, 51, 52] addresses the extraction of CFF from experimental data on various DVCS observables for different beam and target polarizations based on a neural network (NN) architecture, or a multilayer perceptron. The recent analysis in Ref.[51] introduces variable network configurations depending on whether the model is for an unflavored or flavored quark. The use of theoretical constraints is explored, in this case given by the assumption that the CFFs obey a dispersion relation [29–31]. Results of the fit highlight the existence of hidden correlations among CFFs arising from different harmonics in  $\phi$  appearing in the cross section formulation of Refs.[15, 53]. Comparisons with previous, unconstrained results, and with a standard least-squares model fit to the same data show large uncertainties and often an inversion of the trend of data as a function of  $\xi$  and  $t$ .

The PARTONS group addresses two different stages of the analysis, namely, the extraction of CFF from data [19, 54], and, most recently, the determination of GPDs [55]. CFFs are extracted in Refs.[19, 54] from global fits of all available DVCS data using a standard NN augmented by a genetic algorithm. This work’s purpose is to help benchmarking the group’s future NN based analyses. The GPD effort is centered around the concept of “shadow GPDs” [56], which broadly define the set of all local minima generated by regression analysis using given functional parametrizations. Shadow GPDs propose a practical pathway to solve the inverse problem of extracting GPDs from CFFs. The practicality of the concept still remains to be demonstrated.

More recently, the UVA group developed an analysis initially focused on the DVCS cross section [57]. The framework devised in Ref.[57] serves as a first step towards the broader scope of developing a complete analysis for the extraction of CFFs and GPDs from experimental data. Industry standard ML techniques are used to fit a cross section model based on currently available DVCS experimental data, allowing for efficient and accurate predictions interpolating between experimental data points across a wide kinematic range. Estimating model uncertainty allows one to make informed decisions about predictions well outside of the region defined by data, extrapolating to unexplored kinematic regimes. While the results of this analysis show that, for instance, the network can effectively generalize in  $t$ , even in regions with no data, the study also points out several of the practical challenges of fitting the sparse NN with significant experimental uncertainty, as defined by current DVCS data availability. Another important aspect of this study is the handling of the uncertainties from experimental data which is ubiquitous to physics analyses but less commonly considered in building ML models.

Standard least-squares based model fits are also currently being performed at this stage to provide a baseline for new more exploratory approaches. The result of one of these studies are presented in Fig.7 and in Section I C. The latter are equivalent to local fits where CFFs are independently determined from measurements between different kinematic bins. In a more recent development, the free coefficients of a given CFF parameterization are matched to experimental data and the kinematic bins are no longer treated independently, allowing for interpolation between measurements of the same observable on neighboring kinematic bins. This method also affords to extrapolate outside the experimental data, paving the way for impact studies. However, a systematic uncertainty is introduced by the functional choice of a parameterization, which could potentially impact the predictivity of the approach. Furthermore, while ML based approaches provide solutions to overcome the occurrence of local minima, standard fits are not flexible in this respect. This approach can be most useful in the earlier phase of an experimental program when insufficient data are available, preventing use of more flexible alternatives.

All of the studies mentioned above are not only beneficial to the physics community but provide an interesting overlay of objectives for the physics, applied math, computer science and data science communities. A future investment of resources to bring together all communities will allow for a precise extraction of the 3D structure of the nucleon by using a wide range of new methodologies: from including the simulation uncertainties directly in the training procedure, to developing unsupervised (or weakly supervised) procedures, improving the calibration of simulations, developing new inference techniques to improve the efficiency in using simulations, and many more ongoing developments.

In the next section we describe a CFF extraction method based on dispersion relations [29, 30]. The foremost advantage of this approach is that it reduces the number of unknown parameters to be extracted, by calculating the



Real part of the amplitude from the corresponding Imaginary part plus a subtraction constant. The key observation here is that the same subtraction constant (with a flipped sign) enters in the dispersion relations for the CFFs  $\mathcal{H}$  and  $\mathcal{E}$ , while the subtraction constants for CFFs  $\tilde{\mathcal{H}}$  and  $\tilde{\mathcal{E}}$  vanish. These global fits require to be performed with analytical parameterizations of the CFFs dependences, since one needs to extrapolate beyond the available data to perform the full dispersion integral. Furthermore, it is known that dispersion relations are affected by a kinematic,  $t$ -dependent threshold dependence which partially hampers a direct connection to GPDs and affects the extraction of the subtraction term [31]. Although the precision of present data does not allow for a full evaluation of these systematic uncertainties, a dedicated study will be possible in the wider kinematic range of the EIC.

### C. $D$ -term form factor, and mechanical properties of the nucleon - beyond tomography

In section IB tomographic spatial imaging was discussed through access to GPDs employing the DVCS process. This section discusses how to obtain information about gravitational/mechanical properties of the proton. Mechanical properties that relate to gravitational coupling, such as the internal mass distributions, the quark pressure, and the angular momentum distribution inside the proton, are largely unknown. These properties are encoded in the proton's matrix element of the Energy Momentum Tensor (EMT) [58, 59] and are expressed through the GFF [13].

$$\langle p_2 | \hat{T}_{\mu\nu}^{q,g} | p_1 \rangle = \bar{u}(p_2) \left[ A^{q,g}(t) \frac{P_\mu P_\nu}{M} + B^{q,g}(t) \frac{i(P_\mu \sigma_{\mu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M} + D^{q,g}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{4M} + M \bar{c}^{q,g}(t) g_{\mu\nu} \right] u(p_1) \quad (6)$$

The form factors  $A^{q,g}(t)$ ,  $B^{q,g}(t)$ ,  $\bar{c}^{q,g}(t)$ ,  $D^{q,g}(t)$  encode information on the distributions of energy density, angular momentum, and internal forces in the interior of the proton as described in detail in Sec. II C. By virtue of energy-momentum conservation, the terms  $\bar{c}^{q,g}(t)$  contribute to both the quark and to the gluon part with same magnitude but with opposite signs, so that  $\sum_q \bar{c}^q(t) + \bar{c}^g(t) = 0$ . Experimental information on the gluon contribution may come from trace anomaly measurements in  $J/\Psi$  production at threshold, or possibly with the help from LQCD.

The superscripts  $q, g$  indicate that the breakdown is valid for both quarks  $q$  and gluons  $g$ . Most of the discussion in this section is related to the quark contributions, and we will omit the reference to the gluon part for the remainder of this subsection. The GFFs of quarks and gluons also depend on the renormalization scale  $\mu^2$  (associated with the hard scale  $Q^2$  of the process) that we omit in the formalism for simplicity. The total GFFs,  $A(t) = \sum_q A^q(t) + A^g(t)$  and analog for  $B(t)$  and  $D(t)$ , are renormalization scale independent.

The GFF are the entry into the mechanical and other properties of the protons. However, there is not a practical, direct way to measure these form factors as it would require measurements employing the graviton-proton interaction, a highly impractical proposition due to the extreme weakness of the gravitational interaction [58, 59]. More recent theoretical development showed that the GFFs may be indirectly probed in deeply virtual Compton scattering (DVCS) [60]. DVCS allows probing the proton's quark structure expressed in the GPDs, as the basis for the exploration of its mechanical or gravitational properties [61].

The handbag diagram for the DVCS amplitude 3 contains contributions from non-local operators with collinear twist 2, 3, and 4, where the latter two can be neglected at large  $Q^2$ . These operators can be expanded through the operator product expansion in terms of local operators with an infinite tower of  $J^{PC}$  quantum numbers. This includes operators with the quantum numbers of the graviton, so information about how the target would interact with a graviton is encoded within this tower. The GPDs  $H^q$  and  $E^q$  are mapped to the GFF  $D^q(t)$ ,  $A^q(t)$ , and  $J^q(t) = \frac{1}{2} A^q(t) + \frac{1}{2} B^q(t)$  in the Ji sum rule [60], involving the second Mellin moment of the GPD  $H^q$  and  $E^q$  as

$$\int dx x [H^q(x, \xi, t) + E^q(x, \xi, t)] = 2J^q(t), \quad (7)$$

$$\int dx x H^q(x, \xi, t) = A^q(t) + \xi^2 D^q(t). \quad (8)$$

In the following we focus on the term  $D^q(t)$  that encodes information about mechanical properties, see Sec. II C. This new direction of nucleon structure research has recently resulted in the first estimate of the pressure distribution inside the proton based on experimental data [62], employing CLAS DVCS-BH beam-spin asymmetry data [63] and differential cross sections [64], and constraints from parameterized data covering the full phase space.

With the EIC as a high luminosity machine and a large energy reach these properties can be accessed covering a large range in  $x_B$ ,  $Q^2$  and  $-t$  in the exclusive DVCS process. As shown in Figure 8 the lower EIC CM energy range of  $3 \times 10^{-3} < x_B < 0.1$  will cover the valence quark and sea-quark domains, while at the high CM energies the gluon contributions will be accessible at  $10^{-4} < x_B < 10^{-2}$ .

Ideally, one would determine the integrals in Eqs.(7) and (8) by measuring GPD  $H$  and  $E$  in the entire  $x$  and  $\xi$  space and in a large range of  $t$ . For the DVCS experiments, such an approach is impractical as the GPDs are not

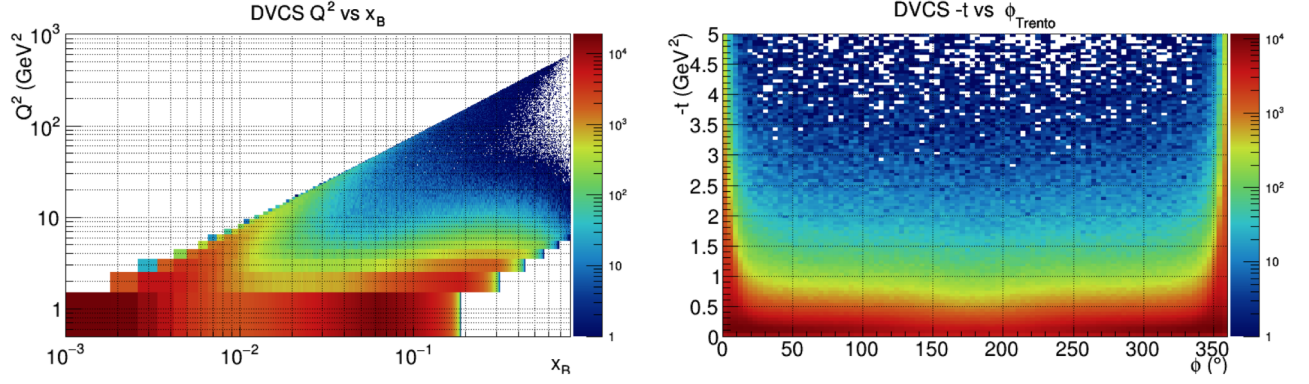


FIG. 8. Accessible ranges in  $x_B$  vs  $Q^2$  (left), and  $t$  vs azimuth angle  $\phi$  (right) for the DVCS process at a center-of-mass energy  $\sqrt{s} = 28$  GeV. The color code indicates the number of events per pixel for a given luminosity.

346 directly accessible in the full  $x, \xi$ -space, but only at the constrained kinematics  $x = \pm\xi$ . The GPDs also do not directly  
 347 appear in the experimental observables. Instead, GPDs appear inside the Compton Form Factors defined in Eqn. (5)  
 348 that depend only on the two variables  $\xi, t$ , where one has traded the real function of 3 parameters  $H(x, \xi, t)$  with  
 349 the complex functions of 2 parameters  $\text{Re}\mathcal{H}(\xi, t)$  and  $\text{Im}\mathcal{H}(\xi, t)$  that can be related more directly to experimentally  
 350 accessible observables. The CFF appear in experimental cross sections and in polarization observables. CFF  $\mathcal{H}(\xi, t)$   
 351 as well as  $\mathcal{E}(\xi, t)$  are thus accessible through a careful analysis of differential cross sections and the responses to spin  
 352 polarization of the electron and the proton beam.

353 As discussed in section IB 2, the extraction of the  $\text{Im}\mathcal{H}(\xi, t)$  and  $\text{Re}\mathcal{H}(\xi, t)$  CFF has been pursued by employing  
 354 global parameterizations for the  $\xi$  and  $t$  dependencies [62] and using machine learning (ML) and artificial neural  
 355 networks approaches [18, 19, 57]

356 In order to determine the  $D^q(t)$  form factor we can employ a subtracted fixed- $t$  dispersion relation that relates  
 357 the real and imaginary parts of the CFF  $\mathcal{H}$  to a subtraction term  $\Delta^q(t)$  whose determination requires additional  
 358 experimental information. The dispersion relation and its relationship to the subtraction term  $\Delta^q(t)$  is given as

$$359 \quad \text{Re}\mathcal{H}^q(\xi, t) = \Delta^q(t) + \frac{1}{\pi} \mathcal{P} \int_0^1 dx \left[ \frac{1}{\xi - x} - \frac{1}{\xi + x} \right] \text{Im}\mathcal{H}^q(x, t), \quad (9)$$

360 where  $\mathcal{P}$  is the principal value of the Cauchy integral, for simplicity written without threshold effects [29, 31].

361 The subtraction term  $\Delta^q(t)$  was shown to be related to the D-term [29, 30] through the series of Gegenbauer  
 362 polynomials. When only the first term in the series is retained and we assume  $D^u(t) \approx D^q(t)$  based on large- $N_c$   
 363 predictions [23] and neglect strange and heavier quark contributions which at JLab energies is a good approximation  
 364 (recall that in DVCS the contributions of different quark flavors enter weighted by squares of the fractional quark  
 365 charge factors), then we obtain:

$$366 \quad D^Q(t) = \sum_q D^q(t) \approx \frac{18}{25} \sum_q e_q^2 \Delta^q(t) \quad (10)$$

367 This truncation of the Gegenbauer polynomials causes a model-dependence as the higher order terms can not be  
 368 isolated with DVCS measurements alone, and must currently be computed in models. The chiral Quark Soliton  
 369 Model [65] predicts a 30% contribution due to the next term in the Gegenbauer expansion. Computations of the next  
 370 leading term may in future become possible from LQCD (see also section VI for more detailed discussion on LQCD  
 371 contributions to GPDs and 3D imaging). ← reference ?? to lattice section

372 It is important to remark that the different terms in the Gegenbauer expansion of  $\Delta^q(t)$  have different renormaliza-  
 373 tion scale dependencies. The broader  $Q^2$ -coverage at EIC may therefore provide the leverage to discriminate between  
 374 the different terms and help to isolate the leading term related to  $D^q(t)$ . In the limit of the renormalization scale  
 375 going to infinity, all higher Gegenbauer terms vanish and asymptotically  $\Delta^q(t) \rightarrow 5 D^q(t)$  [23]. We note that in the  
 376 limit renormalization scale going to infinity it is  $\sum_q D^q(t) \rightarrow D(t) N_f / (N_f + 4C_F)$  and  $D^q(t) \rightarrow D(t) 4C_F / (N_f + 4C_F)$   
 377 where  $D(t)$  is the total GFF,  $N_f$  is the number of flavors and  $C_F = (N_c^2 - 1)/(2N_c)$  [66].

### D. Backward hard exclusive reactions and probing TDAs with high luminosity EIC

378

379 A natural and promising extension of the EIC experimental program for hard exclusive processes is the study of  
 380 hard exclusive electroproduction and photoproduction reactions in the near-backward region [67]. These measurements  
 381 will allow further exploration of hadronic structure in terms of baryon-to-meson and baryon-to-photon Transition  
 382 Distribution Amplitudes [68] which extend both the concepts of Generalized Parton Distributions (GPDs) and baryon  
 383 Distribution Amplitudes (DAs).

384 Baryon-to-meson (and baryon-to-photon) TDAs arise within the collinear factorization framework for hard exclu-  
 385 sive reactions in a kinematic regime that is complementary to the usual near-forward kinematic in which a familiar  
 386 GPD-based description applies for hard exclusive meson electroproduction reactions and DVCS. Technically, TDAs  
 387 are defined as transition matrix elements between a baryon and a meson (or a photon) states of the same non-local  
 388 three-quark operator on the light-cone occurring in the definition of baryon DAs. In Fig. 9 we sketch the collinear  
 389 factorisation reaction mechanism involving TDAs (and nucleon DAs) for hard exclusive near-backward electroproduc-  
 390 tion of a meson off a nucleon target  $\gamma^* N \rightarrow N' M$  [69] and of hard exclusive near-backward photoproduction of a  
 391 lepton pair off a nucleon target (backward Timelike Compton Scattering (TCS))  $\gamma N \rightarrow \gamma^* N' \rightarrow \ell^+ \ell^- N'$  [70].

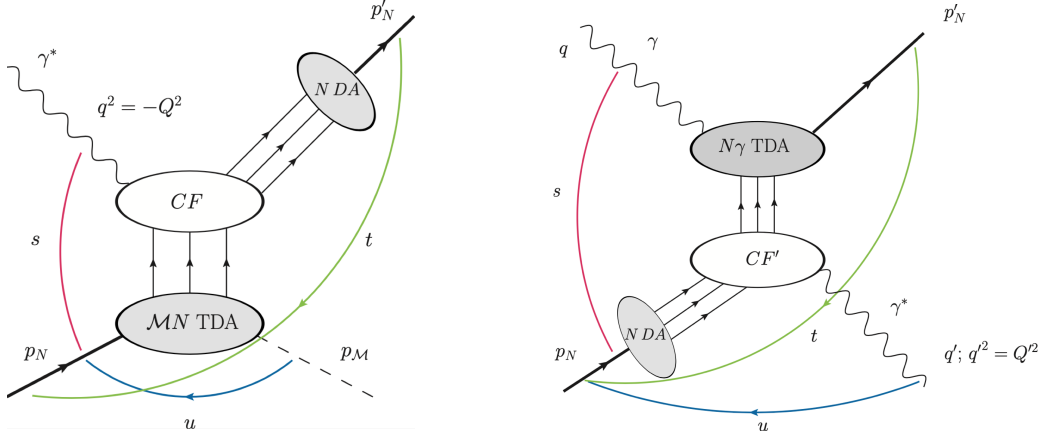


FIG. 9. Left: Collinear factorization mechanism for hard exclusive electroproduction of mesons ( $\gamma^* N \rightarrow N' M$ ) in the near-backward kinematic regime (large  $Q^2$ ,  $W^2$ ; fixed  $x_B$ ;  $|u| \sim 0$ ). Right: Collinear factorization of TCS ( $\gamma N \rightarrow \gamma^* N'$ ) in the near-backward kinematic regime (large  $Q'^2$ ,  $W^2$ ; fixed  $\tau \equiv \frac{Q'^2}{2p_N \cdot q}$ ;  $|u| \sim 0$ ); MN ( $N\gamma$ ) TDA stands for the transition distribution amplitudes from a nucleon-to-a-meson (photon-to-a-nucleon); N DA stands for the nucleon distribution amplitude;  $CF$  and  $CF'$  denote the corresponding hard subprocess amplitudes (coefficient functions).

The physical contents of baryon-to-meson and baryon-to-photon TDAs is conceptually similar to that of GPDs and baryon DAs. Since the non-local QCD operator defining TDAs carries the quantum numbers of a baryon it provides access to the momentum distribution of baryonic number inside hadrons. It also enables the study of non-minimal Fock components of hadronic light-front wave functions. Similarly to GPDs, by switching to the impact parameter space, one can address the distribution of the baryonic charge inside hadrons in the transverse plane. This also enables to study the mesonic and electromagnetic clouds surrounding hadrons and provides new tools for “femtophotography” of hadrons. Testing the validity of the collinear factorized description in terms of TDAs for hard backward electroproduction and photoproduction reactions requires a detailed experimental analysis. The very first experimental indications of the relevance of the TDA-based description for hard electroproduction of backward mesons off nucleons were recently obtained at JLab in the studies of backward pseudoscalar meson electroproduction

$$ep \rightarrow e' n \pi^+$$

by the CLAS collaboration and in Hall A [71, 72], and backward vector meson electroproduction

$$ep \rightarrow e' p' \omega$$

392 by Hall C [73]. This latter analysis enabled checking one of the crucial predictions of the TDA-based formalism, the  
 393 dominance of the transverse cross section  $\sigma_T$ . A dedicated study of backward neutral pseudoscalar meson production  
 394 with a complete Rosenbluth separation of the cross section to challenge  $\sigma_T \gg \sigma_L$  condition is currently prepared by  
 395 Hall C [74].

The hard exclusive backward reactions to be studied with the EIC include the hard exclusive backward electroproduction of light pseudoscalar unflavored  $\pi$ ,  $\eta$ , and strange mesons  $K$  and vector  $\rho$ ,  $\omega$ ,  $\phi$  mesons as well as backward DVCS. Another option can be the study of hard exclusive backward photoproduction of lepton pairs (backward TCS) and of heavy quarkonium. The peculiar EIC kinematics, as compared to fixed target experiments, allows, in principle, a thorough analysis of the backward region pertinent to TDA studies. Higher  $Q^2$  providing a larger lever arm to test the characteristic scaling behavior would be accessible in a domain of moderate  $\gamma^*N$  energies, *i.e.* rather small values of the usual  $y$  variable and not too small values of  $x_B$ . It worth mentioning that since TDA-related cross sections are usually small the high luminosity is definitely needed to scan a sufficiently wide  $Q^2$  range. This will allow the new domain of backward hard exclusive reactions physics to be further explored.

The detection of  $u$ -channel exclusive electroproduction:

$$e + p \rightarrow e' + p' + \pi^0$$

seems easily feasible thanks to the  $4\pi$  coverage of EIC detector package. A preliminary study documented in [8] shows the feasibility of detecting exclusive  $\pi^0$  production at  $u \sim u_0$ . The scattered electrons are well within the standard detection specification. The two photons (from decaying  $\pi^0$ ) project a ring pattern at the zero degree calorimeter (tagging detector along the incidence proton beam) close to the effective acceptance, while recoiled proton enters forward EM calorimeter at high pseudorapidity. The detector optimization and efficiency for detecting these process is currently undergoing.

Also a rough vector meson dominance model based estimates of backward TCS cross section for the EIC kinematical conditions presented in [70] suggest a considerable number of events within the high luminosity regime to study photon-to-nucleon TDAs.

More phenomenological prospective studies and further theoretical development are needed to establish a sound experimental program focusing on TDAs for EIC.

### E. Outlook - Beyond the EIC initial complement

Spin polarized electron and proton beams lead to single-spin dependent cross sections that are proportional to the imaginary part of the DVCS-BH interference amplitude. Double-spin dependent cross sections provide an access to the real part of the interference amplitude but suffer from strong to dominant contributions of the BH amplitude which makes difficult and inaccurate the experimental determination of the real part from this observable. An indisputable and precise determination of this quantity is required to unravel the mechanical properties of the nucleon.

Accessing the real part of interference amplitude is significantly more challenging than the imaginary part. It appears in the unpolarized cross sections for which either the BH contribution is dominant, or all three terms (pure BH, pure DVCS, and DVCS-BH interference amplitudes) are comparable. The DVCS and interference terms can be separated in the unpolarized cross-sections by exploiting their dependencies on the incident beam energy, a generalized Rosenbluth separation. This is an elaborated experimental procedure, which needs some theoretical hypothesis to finally extract an ambiguous physics content [75–77]. Time-like Compton scattering (TCS),  $\gamma p \rightarrow l^+l^-p$  is another process which can, in principle, provide direct but luminosity challenging access to the  $\text{Re}\mathcal{H}(\xi, t)$  in a back-to-back configuration [78] as displayed in Fig. 10. TCS requires zero-degree electron scattering, generating  $l^+l^-$  pairs in quasi-real photo-production over a continuous mass range above resonance production. The feasibility of measuring

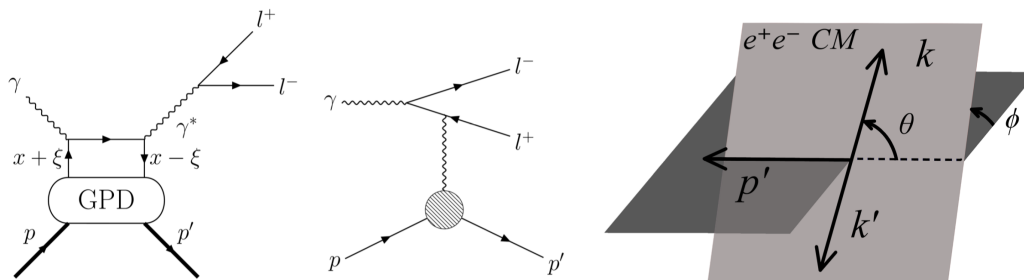


FIG. 10. Left: Handbag diagram of the TCS process. Middle: Diagram of the BH processes. Right: Relevant angles for the TCS kinematics in CMS to isolate the  $\text{Re}\mathcal{H}$  contribution in the interference term.

TCS, and its strong sensitivity to the D-term, has already been established at CLAS12 [78].

A more convenient access to the real part of the interference amplitude is obtained from the comparison between unpolarized electron and positron beams [79]. Indeed, at leading twist, the electron-positron unpolarized DVCS cross

section difference is a pure interference signal, linearly dependent on the real part of the DVCS-BH interference term. As such it provides the cleanest access to this crucial observable, without the need for additional theoretical assumptions in the CFFs extraction procedure [80]. Implementation of a positron source, both polarized and unpolarized [81], at the EIC would thus significantly enhance its capabilities in the high impact 3D imaging science program, with respect, for instance, to the extraction of the CFF  $\text{Re}\mathcal{H}(\xi, t)$  and of the gravitational form factor  $D^q(t)$ .

## II. MASS AND SPIN OF THE NUCLEON

The most fundamental physical properties of the nucleons as well as other hadrons are their masses and spins. Understanding how they arise from the QCD theory of light spin-1/2 quarks and massless spin-1 gluons is one of the most important goals in nuclear physics [82]. The experimental study of the proton spin structure began in the 1980's and has continuously driven the field of hadronic physics for the last thirty years [83]. Despite much effort, a complete picture of the proton spin structure is still missing [25]. The origins of the proton mass have mostly been a theoretical interest in QCD-motivated models or effective approaches such as chiral perturbation theory, and its understanding in the QCD-based framework and related experimental tests have gained attentions only recently [84].

Gaining insight into the emergence of hadron mass from the experimental results on the pion/kaon electromagnetic form factors and PDFs analyzed within the continuum Schwinger method (CSM) represents an important aspect of efforts in experiments of the 12 GeV era at JLab [85] and those foreseen at the EIC in the US [86] and at the EIC in China [87]. A successful description of the electroexcitation amplitudes of the  $\Delta(1232)3/2^+$ ,  $N(1440)1/2^+$ , and  $\Delta(1600)3/2^+$  resonances of different structure [88] has been achieved within the CSM [89, 90] employing the same momentum-dependent dressed quark mass evaluated from the QCD Lagrangian [91] and supported by the experimental results on the structure of the pion/kaon and the ground state nucleon. This success has demonstrated a promising opportunity to address challenging and still open problems in the Standard Model on the emergence of hadron mass by confronting the predictions from QCD-rooted approaches on a broad array of different hadron structure observables with the results from experiments with electromagnetic probes already available and those foreseen from intermediate energy facilities at the luminosity frontier.

In the QCD studies, it has been realized that the matrix elements/form factors of the quark and gluon energy momentum tensor (EMT), measured through DIS momentum sum rule and also the source for gravitational fields of the nucleon, play important roles in spin and mass [13, 92]. Moreover, the interpretation of the GFF  $C(Q^2)$  in terms of mechanical properties has generated much interest [66]. Experimentally, the form factors of EMT can be accessed through the second-order moments of quark and gluon GPDs which can be probed through DVCS and DVMP as discussed in the early sections [13]. EIC is particularly important for probing the GPDs of gluons which are a crucial part of the nucleon [6]. It has been suggested recently that the gluon EMT form factors might be directly accessible through near-threshold heavy-quarkonium production [93].

### A. Nucleon mass

Unlike non-relativistic systems in which the masses mostly arise from the fundamental constituents, masses of relativistic systems arise predominantly through interactions. Indeed, without the strong interactions, three current quarks making up the nucleon weigh about  $\sim 10$  MeV (at  $\mu_{\overline{\text{MS}}} \sim 2$  GeV), presumably from electroweak symmetry breaking but actually there is no way of knowing what the quark masses are in the absence of strong interactions, which is about 1% of the bound state mass [94]. Schematically, we can write the nucleon mass in terms of quark masses and the strong interaction scale  $\Lambda_{\text{QCD}}$ ,

$$M_N = \sum_i \alpha_i m_i + \eta \Lambda_{\text{QCD}} , \quad (11)$$

where  $\alpha_i$  and  $\eta$  are dimensionless coefficients determined from the strong interaction dynamics. Note that  $\Lambda_{\text{QCD}}$  is a free parameter of QCD, which in principle can take any value, and therefore, the nucleon mass can be 10 TeV or 100 MeV, independent of the details of strong interaction physics. One cannot hope, therefore, to explain from QCD itself why the nucleon mass is 940 MeV, not any other value, without invoking more fundamental theories such as grand unifications which may explain why  $\Lambda_{\text{QCD}}$  takes the value that we measured [95].

In the nucleon models,  $\Lambda_{\text{QCD}}$  scale has generally been replaced with some parameters with more direct physical interpretations. For instance, in the models emphasizing chiral symmetry breaking,  $\Lambda_{\text{QCD}}$  is superseded by the chiral symmetry breaking scale and the constituent quark and/or gluon masses [96]. On the other hand, in the models such as the MIT bags which stress the color confinement,  $\Lambda_{\text{QCD}}$  has been associated with the energy density of the

false vacuum inside a bag [97]. In the instanton liquid models,  $\Lambda_{\text{QCD}}$  is reflected through typical instanton size and density [98]. Unfortunately, the effective degrees of freedom in models cannot be studied directly in experiments, and therefore the pictures cannot be directly verified without additional assumptions. In lattice QCD calculations,  $\Lambda_{\text{QCD}}$  is tied with lattice spacing  $a$  which is an ultraviolet momentum cut-off and the strong coupling associated with the cut-off. As we shall discuss below, a model-independent way to introduce this scale might be through the gluonic composite scalar field which breaks the scale symmetry, a Higgs-like scale-generation mechanism [99].

So then what are the meaningful questions one can ask about the nucleon mass, and can they be answered through experiments at EIC? The most discussions so far in the literature are about mass distributions into different dynamical sources and about spatial distributions inside the nucleon. For example, what will be the proton mass if all quark masses were zero? This question has been studied in chiral perturbation theory in 1980's [100]. Through Lorentz symmetry relation, it has been found that the quark and gluon kinetic energy contributions to the nucleon mass can be studied through deep-inelastic scattering [92]. Moreover, it has been suggested that the trace anomaly contribution to the nucleon mass can be measured directly as well [101]. All of these studies are based on understandings of the energy sources in the strong interaction Hamiltonian,  $H_{\text{QCD}}$ . Experimental measurements and theoretical calculations of these mass contributions constitute important tests on an important aspect of our understandings of the nucleon mass.

The spatial distributions of mass/energy densities are an important concept in gravitational theories as they are sources of gravitational potentials. In the limit when the quantum mechanical fluctuations can be neglected or the mass is considered heavy, the proton can have a fixed center-of-mass position with spatial profiles of mass and other densities. Studies of these profiles can be done through the GFF as one has learned about the spatial distributions of the electric charges and currents [66]. Moreover, the trace anomaly contribution is related to the scalar form factor which maps out the dynamical “bag constant” [99].

### 1. Masses in dynamical energy sources

A complete picture of the mass distributions into different sources starts from the QCD Hamiltonian [92]. In relativistic theories, the Hamiltonian is a spatial integral of (00)-component of the second-order EMT  $T^{\mu\nu}$ . Despite that field theories are full of UV divergences, the full EMT is conserved and hence finite. This second-rank tensor can be uniquely decomposed into a trace term proportional to the metric tensor  $g^{\mu\nu}$  and a traceless term  $\bar{T}^{\mu\nu}$ . They are separately finite due to Lorentz symmetry. Thus the QCD Hamiltonian contains two finite pieces, the scalar and (second-order) tensor terms,

$$H = H_S + H_T . \quad (12)$$

A general feature of the Lorentz-symmetric QFT in (3+1)D is that the  $H_S$  contributes 1/4 of a bound state mass, and the tensor term  $H_T$  contributes 3/4 [92], namely

$$E_{S,T} = \langle P | H_{S,T} | P \rangle; \quad E_T = 3E_S = \frac{3}{4}M , \quad (13)$$

where the expectation value is taken in a static hadron (nucleon) state  $|\vec{P} = 0\rangle$ . Again, this is independent of any other specifics of an underlying theory.

A further decomposition of the tensor part of the Hamiltonian (energy) can be done through quark and gluon contributions,

$$E_T = E_{Tq}(\mu) + E_{Tg}(\mu) . \quad (14)$$

These energy sources can be probed through the matrix elements of the corresponding parts in the EMT in terms of the momentum fractions of the parton distributions,  $E_{Tq,g}(\mu) = (3/4)M_N \langle x \rangle_{q,g}(\mu)$ , where the quark and gluon  $\langle x \rangle_{q,g}(\mu)$  can be obtained from the phenomenological PDFs [92]. Therefore, a major part of the proton mass can be understood in terms of quark and gluon kinetic energy contributions, although the latter separation depends on scheme and scale as indicated by argument  $\mu$ .

The scalar energy that contributes to the 1/4 of the proton mass comes from the following matrix element,

$$E_S = \frac{1}{8M} \langle P | (1 + \gamma_m) m \bar{\psi} \psi + \frac{\beta(g)}{2g} F^2 | P \rangle , \quad (15)$$

where  $\gamma_m$  and  $\beta$  are perturbative anomalous dimension and (appropriately normalized) QCD beta function, respectively. The operator is twist-four in high-energy scattering and its matrix element is difficult to measure directly.

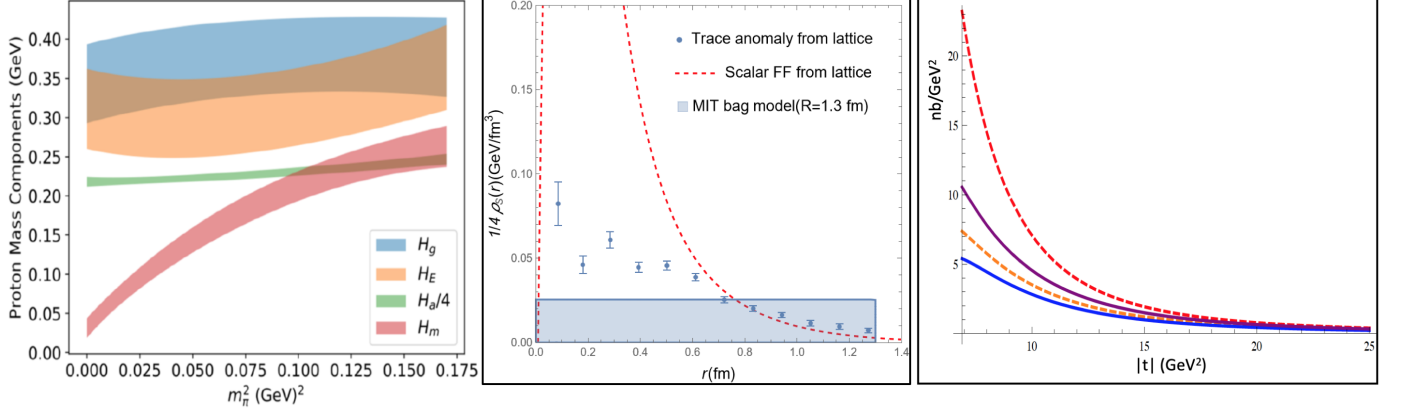


FIG. 11. Left: the proton mass decomposition, calculated from lattice QCD, into different sources, including the quark mass ( $H_m$ ), quark and gluon kinetic and potential energy ( $H_g, H_E$ ), and quantum anomalous energy contributions ( $H_a$ ) [104, 105]. Middle: the scalar density distribution in space which can be constructed from the GFF [110–112]. Right: Differential cross section  $d\sigma/dt$  in units of nb/GeV<sup>2</sup> for exclusive threshold  $J/\Psi$  production at EIC as a function of  $|t|$  at  $W = 4.4$  GeV,  $Q^2 = 64$  GeV<sup>2</sup>. The dashed curves are for  $D^g = 0$  and the solid curves are for nonzero  $D^g$  (from LQCD). The split between the two solid curves, or two dashed curves is caused by the variation in the gluon scalar matrix element  $0 < b < 1$  [109].

532 However, the up and down quark mass contribution has been historically related to the so-called  $\pi$ -N  $\sigma$ -term which  
 533 can be extracted from experimental data [102]. The strange quark mass contribution is related the baryon-octet mass  
 534 spectrum through chiral perturbation theory [103]. A lattice QCD calculation of various contributions to the proton  
 535 mass is shown on the left panel in Fig. 11 [104, 105].

536 The most interesting and surprising is the contribution of the gluon trace-anomaly term  $F^2$ , which sets the scale  
 537 for other contributions. To understand the physics of this contribution, one can consider the composite scalar field  
 538  $\phi \sim F^2$  which has a vacuum expectation value through the gluon condensate. Inside the nucleon, however, the  $\phi$  field  
 539 is not the same. In fact,  $\phi$  gets a contribution through its static response to the valence quarks inside the nucleon,  
 540 with physics similar to the MIT bag model constant  $B$ , shown as the dots and shaded area on the mid-panel in Fig.  
 541 11. This response can also be calculated dynamically as the exchange of a series of  $0^{++}$  scalar particles. If this is  
 542 dominated by a single scalar particle like the  $\sigma$  meson, the mechanism of mass generation is then identical to the  
 543 Higgs mechanism.

544 It has been suggested that this matrix element can be measured through the threshold heavy-quarkonium production  
 545 of photon or electron on scattering on the proton target [101, 106]. However, due to large differences between the  
 546 initial and final nucleon momenta, the interpretation has initially been suggested in the vector dominance model  
 547 (VDM). A better phenomenological description might be through AdS/CFT models [107, 108]. At EIC, one may  
 548 consider deeply-virtual  $J/\Psi$  production to directly measure gluon matrix elements. In the large  $Q^2$  and skewness- $\xi$   
 549 limit, the twist-2 gluon GFF and twist-4  $F^2$  matrix (enhanced by  $1/\alpha_s$ ) elements may dominate. Shown on the right  
 550 panel in Fig. 11 is the sensitivity of the cross section on the anomaly matrix element [109].

551 An indirect approach to access the scalar matrix element is to use the momentum-current conservation,  $\partial_\mu T^{\mu\nu} = 0$ ,  
 552 from which the form factors of the tensor part is related to that of the scalar part. The GFF were defined in equation 6,  
 553 which is reproduced here for reference:

$$554 \langle p_2 | \hat{T}_{\mu\nu}^{q,g} | p_1 \rangle = \bar{u}(p_2) \left[ A^{q,g}(t) \frac{P_\mu P_\nu}{M} + B^{q,g}(t) \frac{i(P_\mu \sigma_{\mu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M} + D^{q,g}(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{4M} + M \bar{c}^{q,g}(t) g_{\mu\nu} \right] u(p_1)$$

555 One of the combinations yields the (twist-four) scalar form factor [84]

$$556 G_s(t) = MA(t) + B(t) \frac{t}{4M} - D(t) \frac{3t}{4M}, \quad (16)$$

557 which contains only the twist-two contributions from the tensor part due to the conservation law. Thus, to get the  
 558 contribution of the trace anomaly term, either in experiments or from lattice QCD simulations, one needs to measure  
 559 the form factors  $A$ ,  $B$  and  $D$  from combined quark and gluon contributions. The Fourier transformation of the  $G_s(t)$   
 560 from lattice QCD [110, 111] is shown as the dotted line in the middle panel on Fig. 11. Shown also as dots in the  
 561 same panel is the the anomaly contribution from lattice QCD [112].

2. Mass radius and “confining” scalar density

The energy density profile in space requires study of the elastic form factors of the EMT as in the case of electric charge distribution. The relevant mass/energy ( $T^{00}$ ) form factor in the Breit frame is

$$G_m(t) = MA(t) + B(t)\frac{t}{4M} - D(t)\frac{t}{4M} . \quad (17)$$

As discussed extensively in the literature, when a particle has a finite mass, the spatial resolution of a coordinate-space distribution is limited by its Compton wavelength. In the case of the nucleon, this is about 0.2 fm. Since the nucleon charge diameter is around 1.7 fm, one can talk about an approximate coordinate-space profile. Thus, one can define the spatial distribution of energy as the Fourier transformation of the mass form factor [66]

$$\rho_m(r) = \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{i\mathbf{q}\cdot\mathbf{r}} G_m(t) . \quad (18)$$

The alternative is to interpret the nucleon form factors in the infinite momentum frame, which yield a 2D profile [113].

From the spatial energy distribution, one can define the Sachs-type mass radius as

$$\langle r^2 \rangle_m = 6 \left. \frac{dG_m(t)/M}{dt} \right|_{t=0} = 6 \frac{dA(t)}{dt} - 3 \frac{D(0)}{2M^2} . \quad (19)$$

The recent data from  $J/\psi$  production at threshold has motivated extracting the proton’s mass radius using either VDM or AdS/CFT type interpretation [114, 115]. A QCD factorization study indicates that a connection with the gluon contribution can be established, while the quark contribution can be obtained through a similar form factor. Both contributions have been computed on the lattice QCD [110, 111], from which one can extract the mass radius as 0.74 fm [84].

Another interesting quantity is the scalar density,

$$\rho_s(r) = \int \frac{d^3\mathbf{q}}{(2\pi)^3} e^{i\mathbf{q}\cdot\mathbf{r}} G_s(t) , \quad (20)$$

defining a scalar field distribution inside the nucleon.  $G_s(q)$  can either be deduced directly from the trace part of the EMT or indirectly through the form factors of the twist-2 tensor, as discussed above. This scalar field is the analogue of the MIT bag constant  $B$ , which is a constant inside the nucleon but zero outside, and may be considered as a confining scalar field. A plot of a LQCD calculation of the scalar density [111] is shown in the middle panel of Fig. 11.

One can define the scalar or confining radius as ,

$$\langle r^2 \rangle_s = 6 \left. \frac{dG_s(t)/M}{dt} \right|_{t=0} = 6 \frac{dA(t)}{dt} - 9 \frac{D(0)}{2M^2} , \quad (21)$$

which can be compared with the bag radius. The difference between the confining and mass radii is

$$\langle r^2 \rangle_s - \langle r^2 \rangle_m = -3 \frac{D(0)}{M^2} . \quad (22)$$

Therefore, a consistent physical picture that the confining radius is larger than the mass radius requires the  $D$ -term  $D(0) < 0$  [84].

## B. Nucleon Spin Structure

The spin structure of the nucleon has been one of the most important driving forces in hadronic physics research in the last thirty years. Non-relativistic quark models have simple predictions about the spin structure, which have been shown incorrect through dedicated deep-inelastic scattering studies [83]. On the other hand, this is not unexpected because QCD quarks probed by high-energy scattering are different from the constituent quarks used in the simple quark models, and a connection between them is difficult to establish.



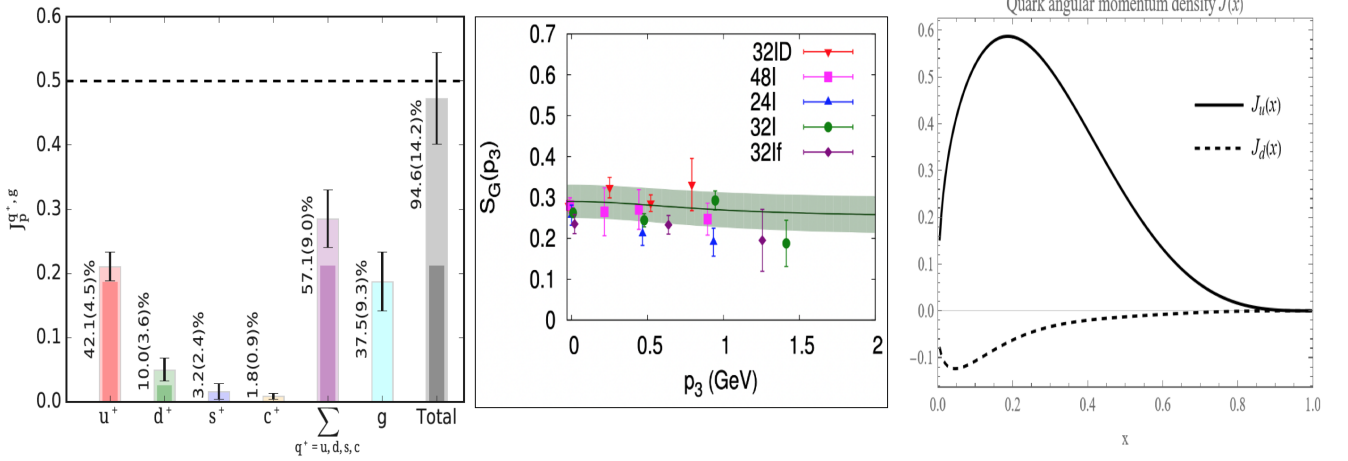


FIG. 12. Proton spin structure calculated from lattice QCD. (Left panel) the covariant spin decomposition [116]. (Middle panel) the gluon helicity contribution  $\Delta G$  calculated from large momentum effective theory [117],  $p_3$  is the absolute value of the 3-momentum  $\mathbf{p}(0, 0, p_3)$ . (Right panel) Integrated quark transverse angular momentum density versus quark momentum fraction  $j_q(x)$  of the proton from LQCD, which can be measured through twist-2 GPD  $E(x)$ .

597

### 1. Longitudinal-Spin Sum Rules

598 The most common approach to study the proton spin is to understand the longitudinal polarization in the infinite  
 599 momentum frame in which the quasi-free quarks and gluons are probed in high-energy scattering [118]. In particular,  
 600 quark and gluon helicity contributions can be measured through summing over parton helicities  $\Delta\Sigma = \int dx \sum_i \Delta q^+(x)$   
 601 and  $\Delta G = \int dx \Delta g(x)$  which appear in the leading-twist scattering observables, where + indicates summing over  
 602 quarks and antiquarks. The EIC planned at BNL will make an important study of  $\Delta G$  through  $Q^2$  evolution and  
 603 two-jet production [6]. A complete spin sum rule also requires measurement of the partonic orbital contributions  
 604  $l_{q,g} = \int dx l_{q,g}(x) dx$ , where  $l_{q,g}(x)$  are orbital angular momentum carried by quarks and gluons with momentum  
 605 fraction  $x$  [119], such that

$$606 \quad \frac{1}{2} \Delta\Sigma + \Delta G + l_q + l_g = \hbar/2. \quad (23)$$

607 This spin sum rule was derived from QCD angular momentum operator by Jaffe and Manohar [118]. Since the  
 608 proton helicity does not grow as the momentum of the proton, it is a twist-three quantity in high-energy scatter-  
 609 ing. Thus, a measurement of partonic  $l_q(x)$  and  $l_g(x)$  requires experimental data on twist-three generalized parton  
 610 distributions [120–122], which will be challenging at EIC [123, 124].

611 Therefore, it appears that the longitudinal spin structure is not simple to measure and interpret in the IMF. This,  
 612 however, is not the case if instead considering a gauge-invariant sum rule [13],

$$613 \quad \frac{1}{2} \Delta\Sigma + L_q + J_g = \hbar/2, \quad (24)$$

614 which are not based on partons, where  $L_q$  and  $J_g$  are related to the GFF through  $J_g = (A_g(0) + B_g(0))/2$ ,  $J_q =$   
 615  $\Delta\Sigma/2 + L_q = (A_q(0) + B_q(0))$ . This sum rule is frame-independent, and does not have a simple partonic interpretation  
 616 when going to the IMF. On the other hand,  $J_q$  and  $J_g$  can be extracted from twist-2 GPDs,

$$617 \quad J_{q,g} = \frac{1}{2} \int dx x (E_{q,g}(x, \xi, t=0) + H_{q,g}(x, \xi, t=0)). \quad (25)$$

618 In the IMF, the twist-2  $L_q$  contains both the twist-three parton orbital angular momentum  $l_q$  and a contribution  
 619 from potential orbital angular momentum. This connection between twist-2 and twist-3 observables is a reflection of  
 620 Lorentz symmetry, through which, one can construct the frame-independent longitudinal spin sum rule by measuring  
 621 the twist-two GPDs [125].

622 Lattice QCD calculations of the angular momentum structure of the nucleon have been investigated by a number  
 623 of groups (see a review in [25]). In particular, the frame-independent longitudinal spin sum rule has been explored

with gauge invariant operators on the lattice. Shown on the left panel in Fig. 12 is a calculation of the spin sum rule by the ETMC collaboration [116]. A more recent result from the  $\chi$ QCD collaboration can be found in [126]. The gluon helicity contribution  $\Delta G$  has been extracted from polarized RHIC experiments and calculated in the large momentum effective field theory [117], shown on the middle panel in the same figure.

## 2. Transverse-Spin Sum Rules

The spin structure of a transverse polarized proton has been less studied both theoretically and experimentally. However, it is not widely known that the transverse spin in the IMF is simpler to understand than the longitudinal one [127]. This is due to that the transverse angular momentum  $J_\perp$  grows with the momentum of nucleon,

$$J_\perp \sim \gamma \rightarrow \infty \quad (26)$$

where  $\gamma$  is the Lorentz boost factor [128].  $J_\perp$  is then a leading-twist quantity and has a simple twist-2 partonic interpretation.

Introducing the parton's transverse angular momentum distribution  $j_q(x)$  for quarks and  $j_g(x)$  for gluon, one has

$$j_{q,g}(x) = \frac{1}{2}x \left( E_{q,g}(x, t=0) + \{q, g\}(x) \right). \quad (27)$$

Physically,  $j_{q,g}(x)$  is the transverse angular momentum density of the quarks and gluons when the partons carry the longitudinal momentum fraction  $x$  [127]. These densities represent the total angular momentum contributions which cannot be separated into spin and orbital ones, as the former is sub-leading for the transverse polarization. Using the above, one has the simple twist-2 partonic sum rule for transverse spin

$$\int_0^1 dx \left( \sum_q j_q(x) + j_g(x) \right) = \hbar/2 \quad (28)$$

which is the analogy of the well-known momentum sum rule. Physically, experimental measurements of  $E_{q,g}(x, t)$  are best performed with transversely polarized targets with leading-twist observables. An example of  $j_{u,d}(x)$  is shown on the right panel of Fig. 12, which is obtained from lattice calculation of  $E_q(x)$  and phenomenological  $q(x)$ .

There is another transverse spin sum rule at the twist-3 level, which is the rotated version of the Jaffe-Manohar sum rule for longitudinal spin [35],

$$\frac{1}{2}\Delta\Sigma_T + \Delta G_T + l_{qT} + l_{gT} = \hbar/2. \quad (29)$$

The numerical values of these quantities are the same as the ones without the  $T$  subscript. However, they are integrated from twist-3 parton densities, e.g.,  $\Delta\Sigma_T = \sum_q \int dx (\Delta q^+(x) + g_2^q(x))$ , where  $g_2$  is a well-known transverse-spin distribution which integrates to zero, and similarly for others. Like the Jaffe-Manohar sum rule, the twist-3 parton densities pose great challenges to measure experimentally.

## C. D-term and strong forces in the interior of the nucleon

The gravitational form factors  $A^{q,g}(t)$ ,  $B^{q,g}(t)$ ,  $\bar{c}^{q,g}(t)$ ,  $D^{q,g}(t)$  defined in Eq. (6) contain information on the spatial distributions of the energy density, angular momentum, and internal forces. The interpretation in the Breit frame, where  $P^\mu = \frac{1}{2}(p' + p)^\mu = (E, 0, 0, 0)$  and  $\Delta^\mu = (p' - p)^\mu = (0, \vec{\Delta})$ , is done by introducing the static EMT by means of a 3D Fourier transform as [61]

$$T_{\mu\nu}(\vec{r}) = \int \frac{d^3\Delta}{2E(2\pi)^3} e^{-i\vec{\Delta}\cdot\vec{r}} \langle p_2 | \hat{T}_{\mu\nu} | p_1 \rangle. \quad (30)$$

The interpretation can be performed also in frames other than Breit frame [129] or in terms of 2D densities [113, 129, 130] with Abel transformations allowing one to switch back and forth between the 2D and 3D interpretations [131]. The consideration of 2D densities for a nucleon state boosted to the infinite momentum frame is of particular advantage as then the transverse center of mass of the nucleon is well-defined [132]. In other frames and in the 3D case, this is not possible impeding the 3D spatial EMT distributions from being exact probabilistic parton densities. The reservations are similar to the interpretation of the electric form factor  $G_E(t)$  in terms of a 3D electrostatic charge

distribution and the definition of a charge radius (which, despite all caveats, gives us an idea of the proton size). The 3D formalism is nevertheless mathematically rigorous [66] and the 3D interpretation is valid from a phase-space point of view [133] becoming exact for the nucleon in the limit of a large number of colors  $N_c$  [66, 134, 135].

In Eq. (30) we quote the total static EMT,  $T_{\mu\nu} = T_{\mu\nu}^q + T_{\mu\nu}^g$ , but one can also define the separate quark and gluon static EMTs [61]. The meaning of the different components of the static EMT is intuitively clear with  $T_{00}(\vec{r})$  denoting the energy density which yields the nucleon mass when integrated over space, and  $T_{0k}(\vec{r})$  being related to the spatial distribution of the angular momentum which upon integration over space yields the nucleon spin  $\frac{1}{2}$ . The distributions of energy density and angular momentum are unknown, but in both cases we at least know very well their integrals, namely the total nucleon mass and total spin  $\frac{1}{2}$ .

The arguably most interesting components of the static EMT are  $T_{ij}(\vec{r})$ , for two reasons. First, they describe the stress tensor and the distribution of internal forces [61] and are related to the  $D$ -term, a property on the same footing as mass, spin and other fundamental characteristics of the proton [136] which was completely unknown until recently. It is worth pointing out that a free non-interacting fermion has a mass and spin but no  $D$ -term [137] which hence emerges as a particle property generated by the dynamics and the interactions in a theory. Second, in order to access the quark and gluon distributions of energy density and angular momentum the knowledge of all GFFs is needed which are encoded in GPDs via Eqs. (7, 8) which in turn are encoded in the Compton form factors in Eq. (5), the actual observables in DVCS. In comparison to that, information on the GFF  $D^q(t)$  can be inferred much more directly from measurements of the Compton form factors via the fixed- $t$  dispersion relation in Eq. (9).

The key to investigating the mechanical properties of the proton is the stress tensor  $T_{ij}(\vec{r})$  which is symmetric and can be decomposed in terms of a traceless part and a trace as

$$T^{ij}(\vec{r}) = \left( e_r^i e_r^j - \frac{1}{3} \delta^{ij} \right) s(r) + \delta^{ij} p(r) \quad (31)$$

with  $s(r)$  known as the distribution of shear forces and  $p(r)$  known as the distribution of pressure forces while  $e_r^i$  are the components of the radial unit vector  $\vec{e}_r = \vec{r}/|\vec{r}|$ . The distributions  $s(r)$  and  $p(r)$  are not independent of each other but related by the differential equation  $\frac{2}{3} s'(r) + \frac{2}{r} s(r) + p'(r) = 0$  which originates from energy-momentum conservation  $\nabla^i T^{ij}(\vec{r}) = 0$ . At this point it is worth stressing that the distributions of energy density and angular momentum can be equally well discussed in the 2D interpretation. But pressure, i.e. force acting on a surface element, is intrinsically a 3D concept. (One can introduce the notion of a 2D pressure [113, 129, 130], but in that case one loses the connection to the familiar meaning of pressure in physics and in the daily life.)

If the form factor  $D(t)$  is known, the distributions  $s(r)$  and  $p(r)$  can be determined via the relations [66]

$$s(r) = -\frac{1}{2M} r \frac{d}{dr} \frac{1}{r} \frac{d}{dr} \tilde{D}(r), \quad (32)$$

$$p(r) = \frac{1}{6M} \frac{1}{r^2} \frac{d}{dr} r^2 \frac{d}{dr} \tilde{D}(r), \quad (33)$$

$$\text{with } \tilde{D}(r) = \int \frac{d^3 \Delta}{(2\pi)^3} \exp^{-i \Delta \mathbf{r}} D(-\Delta^2).$$

If the separate  $D^q(t)$  and  $D^g(t)$  form factors are known, one can analogously define “partial” quark and gluon shear forces  $s^q(r)$  and  $s^g(r)$ . Also “partial” pressures  $p^q(r)$  and  $p^g(r)$  can be defined, but for that besides respectively  $D^q(t)$  and  $D^g(t)$  one needs also the form factor  $\bar{c}^q(t) = -\bar{c}^g(t)$  which is responsible for the “reshuffling” of forces between the gluon and quark subsystems inside the proton [138]. The instanton vacuum model predicts  $\bar{c}^q(t)$  to be very small [138] which would allow one to define partial quark pressures  $p^q(r)$  in terms of  $D^q(t)$  alone. The form factor  $\bar{c}^q(t)$  is difficult to access experimentally but it can be computed in lattice QCD.

An equivalent, compact way to express the relation of  $s^q(r)$  and  $p^q(r)$  and the form factor  $D^q(t)$  is given by (for gluons analogously)

$$D^q(t) = 4M \int d^3 \mathbf{r} \frac{j_2(r\sqrt{-t})}{t} s^q(r) \quad (34)$$

$$D^q(t) = 12M \int d^3 \mathbf{r} \frac{j_0(r\sqrt{-t})}{2t} p^q(r),$$

where  $M$  is the proton mass,  $j_0$  and  $j_2$  are spherical Bessel functions of  $0^{th}$  and  $2^{nd}$  order, respectively. Taking the limit  $t \rightarrow 0$  in Eqs. (34, 35) one obtains two equivalent expressions for the  $D$ -term  $D = D(0)$  given by

$$D = -\frac{4}{15} M \int d^3 r r^2 s(r) = M \int d^3 r r^2 p(r), \quad (35)$$

The derivation of (35) requires the use of the von Laue condition  $\int_0^\infty dr r^2 p(r) = 0$  [139], a necessary but not sufficient condition for stability which follows from energy-momentum conservation.

The stress tensor  $T^{ij}(\vec{r})$  is a  $3 \times 3$  matrix which can be diagonalized. One eigenvalue is the normal force per unit area given by  $p_n(r) = \frac{2}{3} s(r) + p(r)$  with the pertinent eigenvector  $\vec{e}_r$  while the other two eigenvalues are degenerate in spin-0 and spin- $\frac{1}{2}$  cases, with the degeneracy lifted only for higher spins, are referred to as tangential forces per unit area and are given by  $p_t(r) = -\frac{1}{3} s(r) + p(r)$  whose eigenvectors can be chosen to be unit vectors in  $\vartheta$ - and  $\varphi$ -directions in spherical coordinates [66].

The normal force makes appearance if we consider the force  $F^j = T^{ij} dS^i = [\frac{2}{3} s(r) + p(r)] dS e_r^j$  within the proton acting on an area element  $dS^i = dS e_r^i$ . Mechanical stability requires this force to be directed towards the outside, otherwise the system would implode. This implies that the normal force per unit area must be positive [140]

$$\frac{2}{3} s(r) + p(r) > 0. \quad (36)$$

At this point it is instructive to notice that this is exactly the condition which is imposed when calculating the radius of a neutron star. Neutron stars are basically macroscopic hadronic systems (“giant nuclei”) in which gravity and general relativity effects cannot be neglected. Based on a chosen model for the equation of state of nuclear matter, one solves the Tolman-Oppenheimer-Volkoff equation which yields the radial pressure inside the neutron star as function of the distance  $r$  from the center of the neutron star. In our notation, the radial pressure corresponds to  $\frac{2}{3} s(r) + p(r)$ . The solution of the Tolman-Oppenheimer-Volkoff equation yields a radial pressure which is positive in the center and decreases monotonically until it drops to zero at some  $r = R_*$  and would become negative for  $r > R_*$ . This would correspond to a mechanical instability and is avoided by defining the point  $r = R_*$  to be the radius of the neutron star, see for instance [141]. In this way, within the neutron star the mechanical stability condition (36) is always valid, and the point where the normal force per unit area drops to zero coincides with the “edge” of the system.

The proton has of course no sharp “edge” being “surrounded” by a “pion cloud” due to which the normal force does not drop literally to zero but exhibits a Yukawa-tail-type suppression at large  $r$  which becomes proportional to  $\frac{1}{r^6}$  in the chiral limit [134]. In the less realistic but nevertheless very instructive and inspiring bag model, cf. Sec. II A, one does have an “edge”, namely at the bag boundary, where the normal force drops to zero [142]. However, in contrast to the neutron star one does not determine the “edge” of the bag model in this way. Rather the normal force drops “automatically” to zero at the bag radius which reflects the fact that from the very beginning the bag model was thoughtfully constructed as a simple but mechanically stable model of hadrons [97].

The normal force per unite area  $\frac{2}{3} s(r) + p(r)$  is, thanks to positivity in Eq. (36) guaranteed by mechanical stability, an ideal quantity to define the size of the system. Notice that a quantity like electric charge distribution can be used to define an electric charge radius for the positively charged proton which is a meaningful proxy for the “proton size”. However, for an electrically neutral hadron this is not possible. One can still define an electric mean square charge radius  $r_{\text{ch}}^2 = 6 G'_E(0)$  in terms of the derivative of the electric form factor  $G_E(t)$  at  $t = 0$ . But for the neutron  $r_{\text{ch}}^2 < 0$  which gives insights about the distribution of the electric charge inside the neutron, but does not tell us anything about its size. This is ultimately due to the neutron’s charge distribution not being positive definite.

The positive-definite normal force per unite area  $\frac{2}{3} s(r) + p(r)$ , Eq. (36), allows us to define the *mechanical radius* as follows [66, 143]

$$r_{\text{mech}}^2 = \frac{\int d^3r r^2 \left( \frac{2}{3} s(r) + p(r) \right)}{\int d^3r \left( \frac{2}{3} s(r) + p(r) \right)} = \frac{6 \int D(0)}{\int_{-\infty}^0 dt D(t)}. \quad (37)$$

Interestingly, this is an “anti-derivative” of a form factor as opposed to the electric mean square charge radius defined in terms of the derivative of the electric form factor at  $t = 0$ . With this definition the proton and neutron have the same radius (up to small isospin violating effects). Another advantage is that the (isovector component of the) electric mean square charge radius diverges in the chiral limit which makes it an inadequate proxy for the proton size in the chiral limit, while the mechanical radius in Eq. (37) remains finite in the chiral limit [66]. The mechanical radius of the proton is predicted to be somewhat smaller than its charge radius in soliton models at the physical value of the pion mass [134, 144]. In quark models both radii become equal when one takes the non-relativistic limit [135, 142].

An immediate consequence of the positive-definite nature of the normal force per unite area  $\frac{2}{3} s(r) + p(r)$  in Eq. (36), is that the  $D$ -term  $D = D(0)$  is negative [140]. This has been confirmed in model and lattice QCD calculations, see e.g. [134, 135, 140, 142, 144–146] and the review [66]. The behaviour of the EMT spatial distributions at large- $r$  is dictated by the behavior of the GFFs at small  $t$  which can be studied in chiral perturbation theory [147]. This allows one to derive a model-independent bound formulated in terms of a low-energy constant. According to this bound the  $D$ -term of the nucleon is negative and  $D \leq -0.20 \pm 0.02$  [148].

761 Among the open questions in theory is the issue of how to define the  $D$ -term in the presence of long-range forces  
 762 such as the electromagnetic interaction. It was shown in a classical model that the  $D(t)$  of the proton diverges for  
 763  $t \rightarrow 0$  like  $1/\sqrt{-t}$  when QED effects are included [149]. The form factor  $D(t)$  exhibits a divergence for  $t \rightarrow 0$  due  
 764 to QED effects also for charged pions [150]. Similar behavior was observed for  $D(t)$  of the electron in 1-loop QED  
 765 calculations [151]. Also for the H-atom, a bound state of the electromagnetic interaction, does one find conflicting  
 766 results [152, 153]. These findings are not entirely surprising as the presence of a massless state (the photon) in a  
 767 theory may have profound consequences. Notice that  $D(t)$  is the only GFF which exhibits a divergence for  $t \rightarrow 0$  when  
 768 QED effects are included. Also this is not surprising given the relation of  $D(t)$  to the forces present in a system. The  
 769 behavior of  $D(t) \propto 1/\sqrt{-t}$  at small- $t$  is relevant only in the unmeasurable region of very small  $|t| < 10^{-3}\text{GeV}^2$  such  
 770 that this is of no practical concern for experiments [149]. However, a satisfactory theoretical definition of the  $D$ -term  
 771 may even require the inclusion of gravitational forces which, no matter how weak, are present in every system and  
 772 are also long-range forces [154]. Notice that that despite the divergence of  $D(t)$  due to QED effects the accompanying  
 773 prefactor  $(\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2)$  ensures that the matrix element  $\langle p_2 | \hat{T}_{\mu\nu}^{q,g} | p_1 \rangle$  is well-behaving in the forward limit.

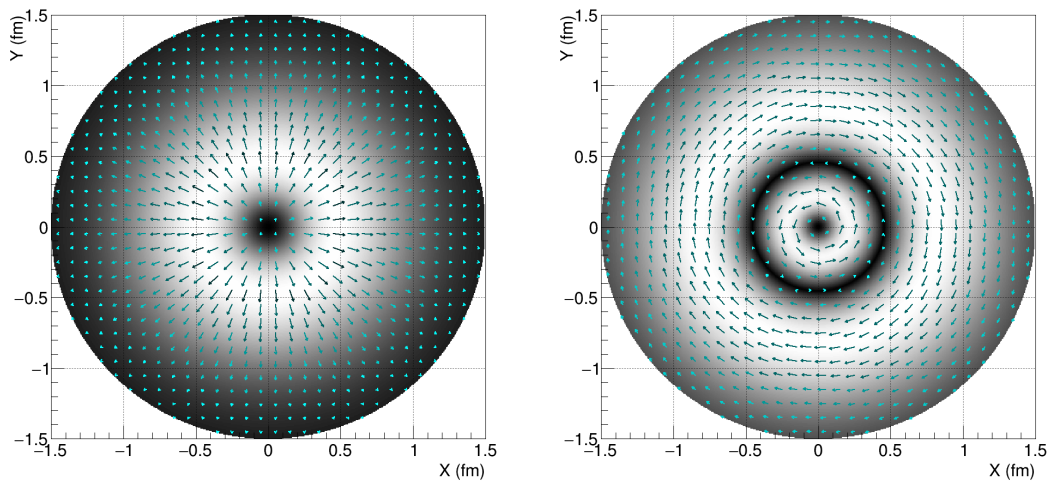


FIG. 13. Left: Spatial distribution of radial force, which has a positive sign everywhere. Right: Distribution of tangential force, which exhibits a node near a distance  $r \approx 0.45\text{fm}$  from the center, where it also reverses sign as indicated by the direction of the arrows. The lines represent the magnitude of force acting along the orientation of the surface. Note that pressure acts equally on both sides of a hypothetical pressure gauge immersed in the system. A positive magnitude of pressure means that an element of the proton is being pushed on, while a negative magnitude means it is being pulled on from both directions. [129, 155].

774 The first experimental information from Jefferson Lab experiments allows one to present first visualization of the  
 775 pressure inside the proton. Using expression for  $D^q(t)$  in (10) and the parameterization of  $\Delta(t)$  in [156] the Fourier  
 776 transforms (34) and (35) can be inverted to determine respectively  $s^q(r)$  which is also referred to as pressure anisotropy,  
 777 and  $p^q(r)$  which is also referred to as the isotropic pressure.

778 Figure 13 shows an example of a tangential pressure distribution inside the proton using parameterizations of  $\mathcal{H}(\xi, t)$   
 779 and  $\Delta(t)$ . We stress that these results have been obtained with parameterizations of the kinematic observables  $\xi$  and  
 780  $t$  extrapolated into unmeasured physical territory. The extension of these measurements into the EIC kinematics  
 781 domain and the availability of transversely polarized protons, will enable experiments with strong sensitivity to the  
 782 CFF  $\mathcal{E}(\xi, t)$  and  $\mathcal{H}(\xi, t)$  and unprecedented kinematic coverage.

### 783 III. ACCESSING THE MOMENTUM DEPENDENT STRUCTURE OF THE NUCLEON IN 784 SEMI-INCLUSIVE DEEP INELASTIC SCATTERING

#### 785 A. Overview

786 Accessing the spin dependent and spin averaged nucleon structure encoded in Transverse Momentum Dependent  
 787 parton distribution functions (TMD PDFs, or simply TMDs) as well as subleading twist parton distribution functions  
 788 (twist3 PDFs) in semi-inclusive deep-inelastic scattering [157] is a central part of the scientific mission of the EIC [8].  
 789 This program focuses on an unprecedented investigation of the parton dynamics and correlations at the confinement

scale and will benefit substantially by an increased luminosity at medium energies for the following reasons.

- Structure functions appearing at sub-leading twist are suppressed by a kinematic factor  $1/Q$ , which makes data at relatively low and medium  $Q^2$  the natural domain for their measurement. Similarly, effects from the intrinsic transverse momentum dependence are suppressed at high  $Q^2$ , when most of the observed transverse momenta are generated perturbatively. As a consequence, the signal of TMDs is naturally diluted at the highest energies. However, at the same time  $Q^2$  has to be high enough for the applicability of factorization theorems, which makes most fixed target data already challenging. Running the EIC at low- to medium-CM energies might therefore occupy a sweet spot at which non-perturbative and subleading effects are sizeable and current knowledge allows the application of factorization to extract the relevant quantities [11]. The Sivers asymmetry, related to one of the most intriguing parton dynamics which will be discussed below, is shown in Fig. 14 for different EIC energy options, illustrating the rapid fall of the expected TMD signal as higher and higher  $Q^2$  is accessed.
- To map out the structure of the nucleon encoded in TMDs and twist3 PDFs, high precision, multi-dimensional measurements are needed, which requires very high statistics. For our understanding of the evolution and proper domain of these objects, it is essential to cover an extended kinematic phase space region connecting the future collider to the ongoing fixed-target precision measurements, *e.g.* by the JLab experiments. Figure 15 shows the estimated phase space covered by the existing JLab12 program compared to the lowest and highest EIC energy options.
- Finally, intermediate energies have an advantage for a SIDIS program, as its foremost detector requirements are excellent tracking and particle identification. The most significant signals are expected for particles that carry a large momentum fraction  $z$  of the fragmenting quark, as these particles are most closely connected to the original quark properties. As illustrated in Fig. 16, at intermediate EIC energies, all particles that are detected at mid-rapidity are within the momentum acceptance range of the reference detectors. This is not necessarily true for the highest energies, when particle identification within the typical EIC detector dimensions becomes challenging.

The remainder of this section is organized as follows. Section III B will discuss the physics case for twist-3 observables, Sec. III will give a short overview of the TMD framework and impact studies for unpolarized and Sivers TMD, which were identified as golden channels in the Yellow Report. This section will also briefly discuss TMDs in medium. Finally, Sec. III D will introduce the case for jet physics at intermediate energies and high luminosity. Radiative corrections might complicate the picture, as the impact on cross-sections and asymmetries can be sizable, depending on the kinematic regime. Because the interplay between radiative corrections and TMD extraction is still very much under investigation, these effects are not considered for the studies shown in this section.

## B. Accessing Quark-Gluon Correlations at sub-leading Twist

The interest for contributions that are suppressed by factors of  $(M/Q)^{t-2}$  has recently grown with the possibility to access them in low-energy experiments, such as HERMES and CLAS. Moderate  $Q^2$  values at EIC will offer unique opportunities for precision analyses of higher-twist distribution functions. Such PDFs are often associated to multi-parton correlations as, to some extent, the operator that defines such objects is made of quarks and gluon fields. Such operators are almost unexplored by phenomenology [157, 160–164]. As argued below, the physics of twist-3 distributions is broader than the already important quark-gluon-quark interaction, whose third Mellin moments receive an interpretation in terms of forces [165].

A well-known example of higher-twist objects is the twist-3 contribution to the axial-vector matrix element,  $g_T$ . The latter can be expressed in terms of a leading-twist distribution through the Wandzura-Wilczek relation, and a genuine twist-3 contribution. Data have shown that the genuine term is not necessarily small [161, 162]. In the Yellow Report for the EIC, the access to  $g_T$  through double-spin asymmetry  $A_{LT}$  in inclusive DIS has been proposed as the golden channel towards the study of multi-parton correlations. It was shown that the impact on the uncertainty, based on the previous JAM analyses, is expected to be significant. Figure 17 shows the impact of the EIC data with high luminosity at low and medium energies on  $g_T$  extraction.

The scalar PDF,  $e(x)$ , is preeminent in that it relates to diverse aspects of non-perturbative dynamics, such as the scalar charge of the nucleons and an explicit quark-mass term, in addition to the quark-gluon correlations. The scalar charge is particularly interesting in view of the mass decomposition of the proton as it constitutes a unique avenue towards the phenomenological extraction of the scalar condensate [166]. While there exist semi-phenomenological approaches to the determination of the pion-nucleon sigma-term, *e.g.* [167, 168], the twist-3  $e(x)$  can provide a determination that is minimally biased by the underlying theoretical assumptions. Some model dependence is, based on our current understanding, inevitable, since the extraction of the sigma requires knowledge of  $e(x)$  in particular

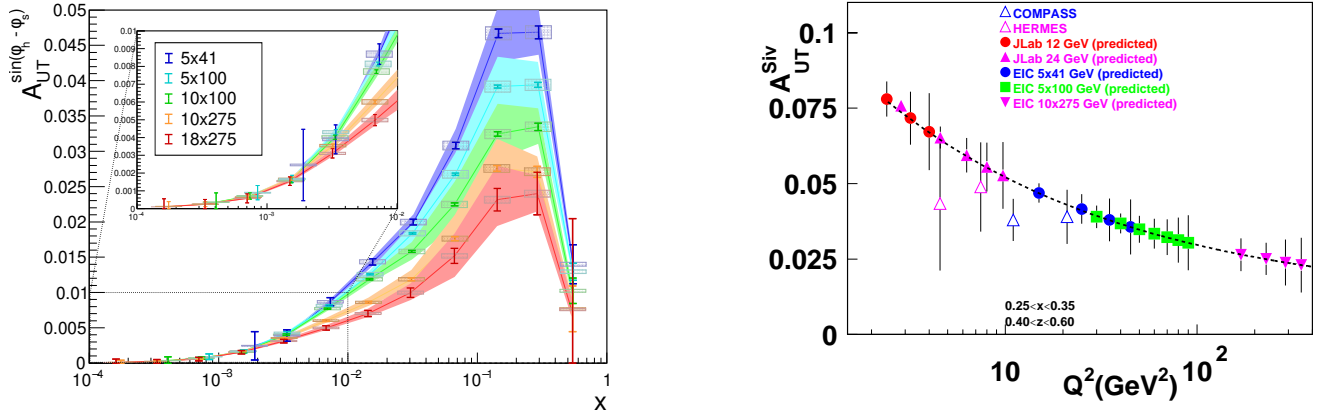


FIG. 14. Left: Projected Sivers asymmetry for various EIC run settings. (Example for ATHENA pseudodata), 2% point-to-point systematic uncertainties assumed. Right: projected Sivers asymmetries for 100 days of data taking at each CM setting with the baseline luminosity vs.  $Q^2$  for  $0.25 < x < 0.35$  and  $0.4 < z < 0.6$  at the luminosity optimized EIC, JLab12 and the proposed JLab24. For the JLab projections, the acceptance of the CLAS detector is used. The proposed SoLID experiment will be able to run at higher luminosity values and is expected to improve on these projections [158, 159]. The drop of the amplitude with  $Q^2$  is evident. At the same time the projected uncertainties rise, as the valence quark region is harder to access at high  $Q^2$ . A constraint of  $y > 0.05$  is used for this figure.

843 down to  $x = 0$ , which is not experimentally accessible. The access to the scalar PDF through longitudinal beam-spin  
 844 asymmetries in (dihadron) SIDIS [169] was proposed as a silver channel in the Yellow Report. Up to date, the scalar  
 845 PDF has been accessed at JLab, in CLAS [170] and CLAS12 [171], for low values of  $Q^2$  and  $x$  ranging from 0.1 – 0.5,  
 846 leading to the first point-by-point phenomenological extraction [172]. While the parameterization of  $e(x)$  is still a  
 847 work in progress, the impact from the EIC was shown to be significant thanks to the broad kinematical reach. The  
 848  $x$  range will be extended towards small- $x$  values, in the region relevant for the evaluation of the sum rules – such  
 849 as the relation to the scalar charge. The  $Q^2$  range, spanning a broad window of mid- $Q^2$  values, will allow analyses  
 850 that account for QCD evolution effects on each contribution. EIC thus represents a unique opportunity to expand  
 851 the current exploratory studies towards global QCD analyses of the rich phenomenology of higher-twist distribution  
 852 functions.

853 In Fig. 18 the theoretical predictions are shown for the contribution of  $e^a(x)$  to the beam spin asymmetry in semi-  
 854 inclusive di-hadron production in the collinear framework for two different center of mass energies, showing larger  
 855 projected asymmetries for lower energies as expected. This asymmetry receives a contribution not only from  $e^a(x)$  but  
 856 also from a term involving a twist-3 di-hadron fragmentation function together with  $f_1^a(x)$  [169]. The latter has not  
 857 been considered here [172]. The uncertainties in Fig. 18 come from the envelope of the uncertainties on the interference  
 858 fragmentation function [173] and two models for  $e^a(x)$ , the light-front constituent quark model [174] and model of  
 859 the mass-term contribution to  $e^a(x)$  with an assumed constituent quark mass of 300 MeV and the unpolarized PDF  
 860 from MSTW08LO. All PDFs and fragmentation functions are taken at  $Q^2 = 1 \text{ GeV}^2$  and the projected uncertainties  
 861 for the EIC are shown only for  $Q^2$  values smaller than  $10 \text{ GeV}^2$ .

862 As the leading twist analysis addressed further below, all higher-twist analyses will rely on the possibility to separate  
 863 the contributions of the various flavors from different observables, and mostly from different targets. In particular,  
 864 deuteron and  $^3\text{He}$  nuclei will provide effective neutron targets to complement the proton data.

865 The phenomenological efforts can be paired with the progress made from the lattice [49, 50]. Moments of higher-twist  
 866 distributions have been determined on the lattice [175], frameworks for quasi-PDFs are being studied as well [176].

867 Beyond the collinear twist-3 mentioned above, there is a plethora of higher-twist TMDs that could be studied at  
 868 the EIC. Moreover, the second IR will grant us the opportunity to explore the relations between twist-3 collinear  
 869 PDFs and twist-2 TMDs, the understanding of which is key for the interpretation of low-energy dynamics.

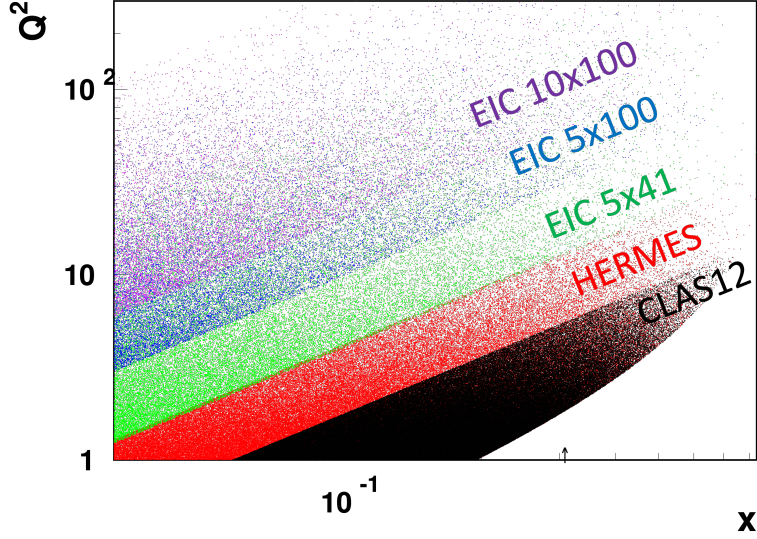


FIG. 15. Estimated coverage of JLab12, HERMES and EIC data for different energy configurations. The need to deliver high luminosity for the low and medium energy configurations to fill in the phase space between fixed target experiments and the higher EIC options is obvious. The data are constraint to  $y > 0.05$ .

870

### C. Measurements of TMDs

871 The lepton-hadron semi-inclusive deep inelastic scattering (SIDIS) at the EIC will provide excellent opportunities  
 872 to probe the confined motion of quarks and gluons inside the colliding hadron, which are encoded in the transverse  
 873 momentum dependent parton distribution functions (TMD PDFs, or simply, TMDs). With the scattered lepton and  
 874 an observed hadron (or jet) with sensitivity to transverse momentum in the final-state, SIDIS provides not only a  
 875 hard scale  $Q \gg \Lambda_{\text{QCD}}$  from the virtuality of the exchanged virtual photon to localize an active quark or gluon inside  
 876 the colliding hadron, but also a natural “soft” scale from the momentum imbalance between the observed lepton and  
 877 hadron in the final-state, which is sensitive to the transverse momentum of the active quark or gluon.

878 With the one-photon approximation, the “soft” scale is the transverse momentum of the observed hadron in the  
 879 photon-hadron (or the Breit) frame,  $\mathbf{P}_{h_T} \gtrsim \Lambda_{\text{QCD}}$ . When  $Q \gg |\mathbf{P}_{h_T}|$ , the unpolarized SIDIS cross section can be  
 880 factorized as [177],

$$881 \frac{d\sigma^{\text{SIDIS}}}{dx_B dQ^2 d^2\mathbf{P}_{h_T}} \propto x \sum_i e_i^2 \int d^2\mathbf{p}_T d^2\mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h_T}/z) \omega_i(\mathbf{p}_T, \mathbf{k}_T) f_i(x, p_T^2) D_{h/i}(z, k_T^2) \equiv \mathcal{C}[\omega f D], \quad (38)$$

882 which provides the direct access to the TMD PDFs,  $f_i(x, p_T^2)$  of flavor  $i$  and transverse momentum  $p_T^2 \equiv \mathbf{p}_T^2$ , and  
 883 TMD fragmentation functions (FFs),  $D_{h/i}(x, k_T^2)$  for a parton of flavor  $i$  and transverse momentum  $k_T^2 \equiv \mathbf{k}_T^2$ , to evolve  
 884 into the observed hadron  $h$  of transverse momentum  $P_{h_T}$  in this photon-hadron frame. In Eq. (38), the  $\omega_i(\mathbf{p}_T, \mathbf{k}_T)$   
 885 is a known function depending on the kinematics, the type of TMDs and corresponding angles between the parton  
 886 transverse momenta.

887 With many more TMDs than PDFs, it will be possible to learn much more on QCD dynamics that holds the  
 888 quarks and gluons together to form the bound hadron, despite being harder to extract and separate these TMDs  
 889 from experimental data. On the other hand, with a good detector able to cover the angle distribution between two  
 890 well-defined planes, the leptonic plane determined by the colliding and scattered leptons, and the hadronic plane  
 891 defined by the colliding and observed hadrons, SIDIS measurements at the EIC will allow the extraction of various  
 892 TMDs by evaluating independent angular modulations of the angle distribution between the two planes as well as the  
 893 distribution between the hadron spin vector and one of the planes.



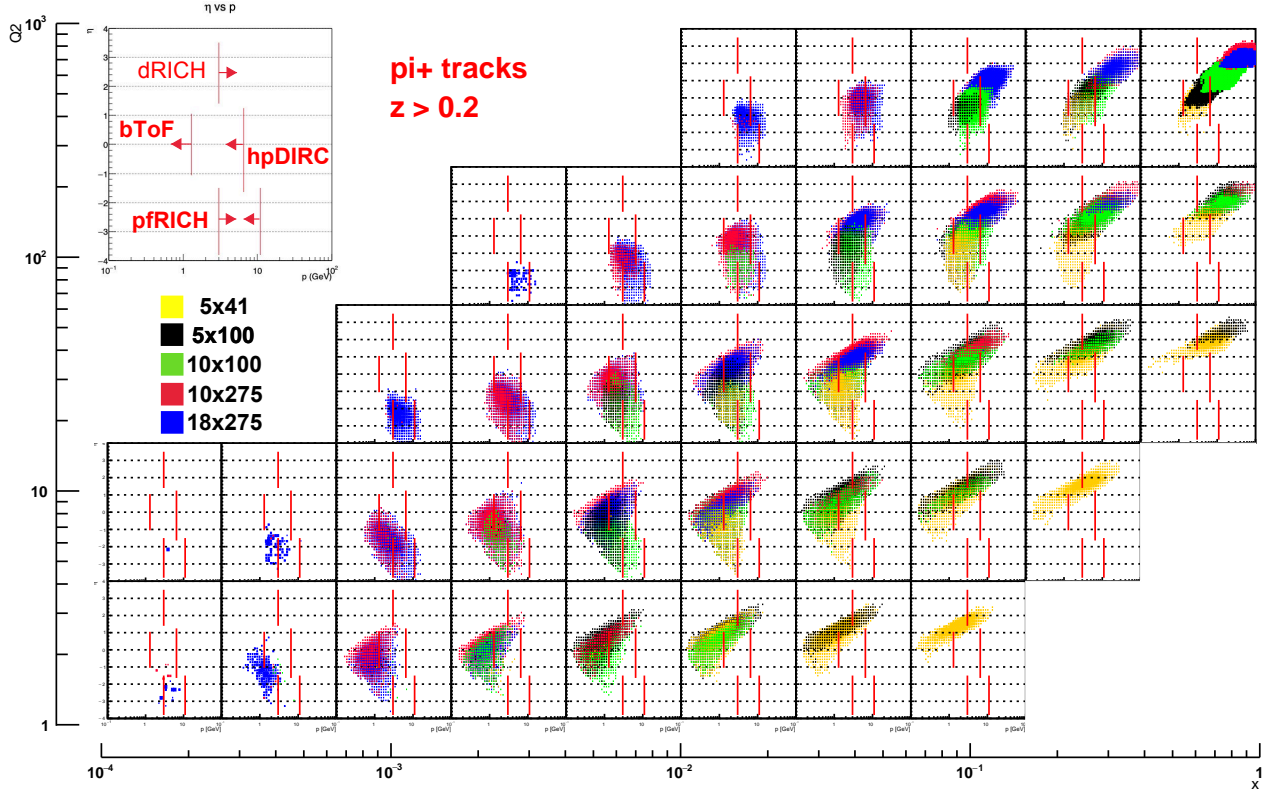


FIG. 16. Acceptance of an exemplary EIC detector (here: ATHENA) in laboratory frame  $\eta/p$  for various energy configurations and  $x, Q^2$  regions. PID limits exemplary for the ATHENA proposal are indicated with red lines. At the highest energies a significant fraction of high  $z$  particles is outside the PID range. The horizontal axes are momenta from 0.1 to 100 GeV, and the vertical axes are pseudo-rapidity from -4 to +4.

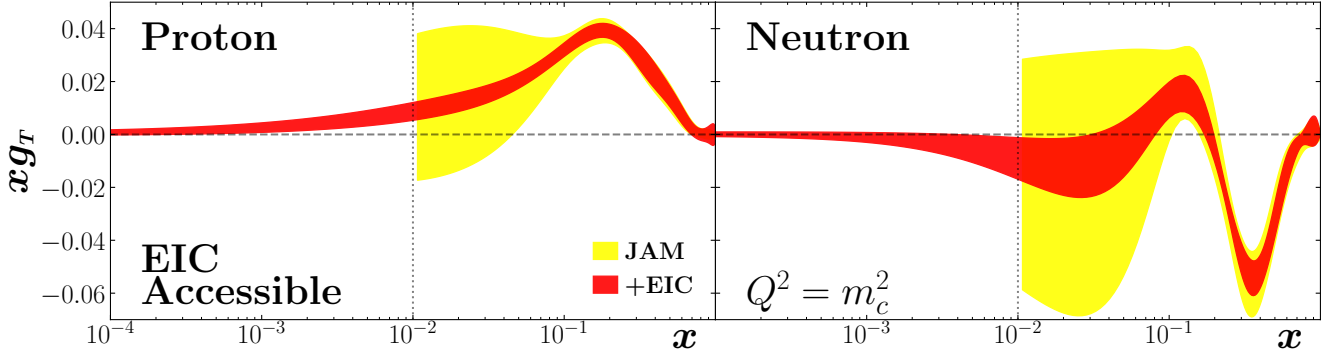


FIG. 17. Impact of EIC data with high luminosity at low/medium energies on  $g_T$  extraction. The improvement at high  $x$  is moderate (but not zero) due to pre-existing data. This extraction uses data at  $18 \times 275$ ,  $10 \times 100$ ,  $5 \times 100$  and  $5 \times 41$ , assuming an integrated luminosity of  $10\text{fb}^{-1}$  at  $18 \times 275$  and the other energies scaled according to their relative instantaneous luminosities.

894

### 1. Impact on the understanding of TMD factorization and applicability to fixed target data

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The TMD factorization formula Eq 38 receives corrections which enter in terms of powers of  $\delta \sim P_{hT}/z/Q$ . Identifying the domain of applicability of TMD factorization is not trivial [178]. In recent analyses, usually the choice  $\delta < 0.25$  is adopted, at least for high  $Q$  [179–182]. These restrictions reduce the significance of a large amount of existing measurements, in particular a majority of data from existing fixed target experiments. Figure 19 illustrates this issue by showing the results of Ref. [183] where the regions of pion production in SIDIS at the EIC are studied

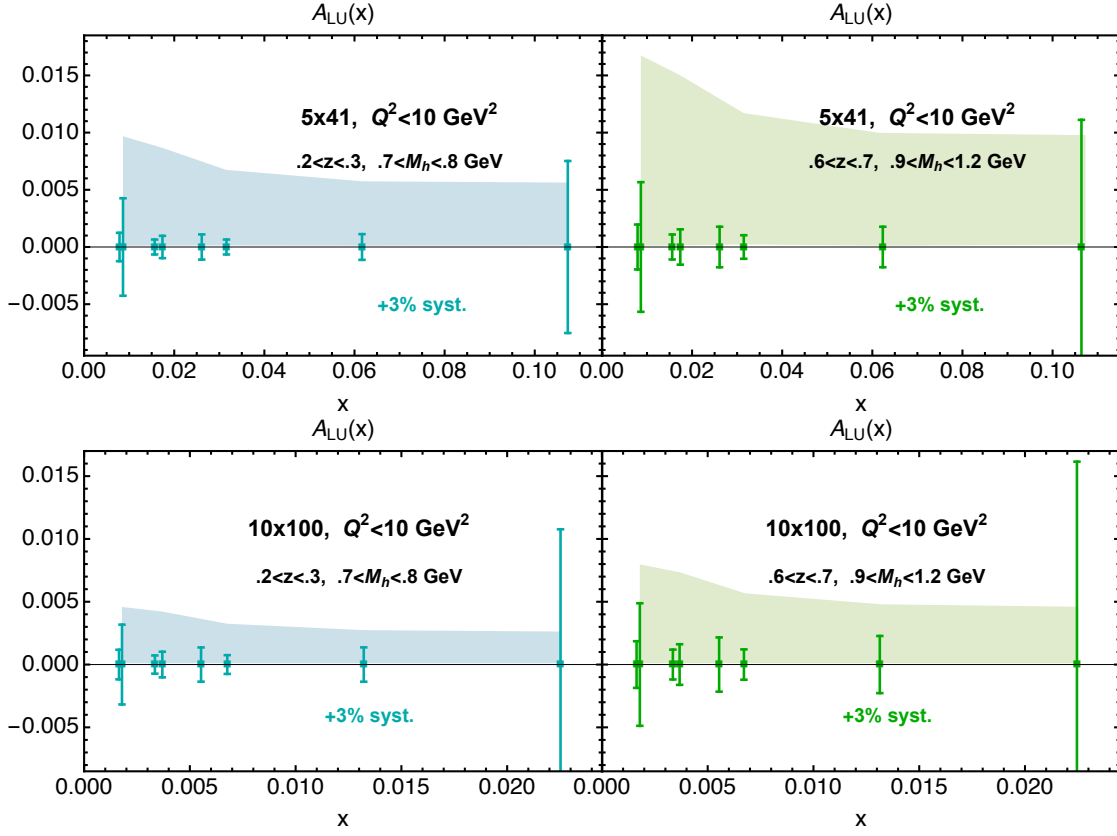


FIG. 18. Beam Spin Asymmetry in semi-inclusive di-hadron production. Predictions corresponding to  $Q^2 = 1 \text{ GeV}^2$  based on the di-hadron fragmentation functions of Ref. [173], low-energy models for the twist-3 PDF  $e(x)$  (see text) and MSTW08 for the unpolarized PDF at LO. Figure is taken from the Yellow Report [8]. The twist-3 fragmentation is neglected. The upper and lower panel show two different energy configuration ; the left (blue) and right (green) plots correspond, respectively, to the fragmentation kinematics of  $(0.2 < z < 0.3, 0.7 < M_h < 0.8 \text{ GeV})$  and  $(0.6 < z < 0.7, 0.9 < M_h < 1.2 \text{ GeV})$ . The bands give the envelope of the model projections discussed in the text folded with the uncertainty of the interference fragmentation function. The projected statistical uncertainties are plotted at zero and correspond to  $10 \text{ fb}^{-1}$  at each CM setting. This illustrates that the data at lower  $\sqrt{s}$  will have a larger impact on constraining  $e(x)$ . Furthermore, the  $Q^2 < 10 \text{ GeV}^2$  data, where the signal is still expected sizable, is restricted to low  $x$  for large  $\sqrt{s}$ , where in turn  $e(x)$  is expected to be small.

900 using results of Ref. [184]. The so-called affinity to TMD factorization region (i.e. the probability that the data can  
 901 be described by TMD factorization) is calculated for each bin of the EIC measurements. The affinity represents the  
 902 probability of the bin to belong to TMD factorization region and spans from 0% to 100%, indicated by color and  
 903 symbol size in the figure. One can see from Fig. 19 that only at relatively high  $z$  and  $P_{hT}$  (and relatively large  $x$   
 904 and  $Q^2$ ) corrections to the TMD factorization description are expected to be negligible. The reach of the EIC data  
 905 into other regions, will be important for the study the connections to other types of factorization, for instance the  
 906 collinear factorization or the region accessed by fixed target experiments, where sizable corrections to the current  
 907 TMD formalism are expected. Comparing this figure with the reach of the different energy option shown in Fig. 16,  
 908 it can be seen that intermediate beam energy option such as  $10 \times 100 \text{ GeV}^2$  operate largely in a region where TMD  
 909 factorization holds, but also contain phase space in the transition region towards other QCD regimes. The flexibility  
 910 to go from one regime of factorization to the other will be a crucial ingredient in our understanding of QCD, and in  
 911 the interpretation of the vast amount of fixed target data, which has a low TMD affinity.

912

## 2. Impact on TMD PDF extraction

913 The theoretical description of TMDs has been extensively studied in coordinate space labeled by  $b$  as the conjugate  
 914 variable of transverse momentum. In the large  $b$  region (small  $q_T \approx p_T/z$ ), TMDs are non-perturbative and encode  
 915 intrinsic properties of hadrons while in the small  $b$ , TMDs are dominated by QCD radiation which is calculable in  
 916 perturbative QCD. In the latter, TMDs can be connected with their corresponding collinear counterparts such as

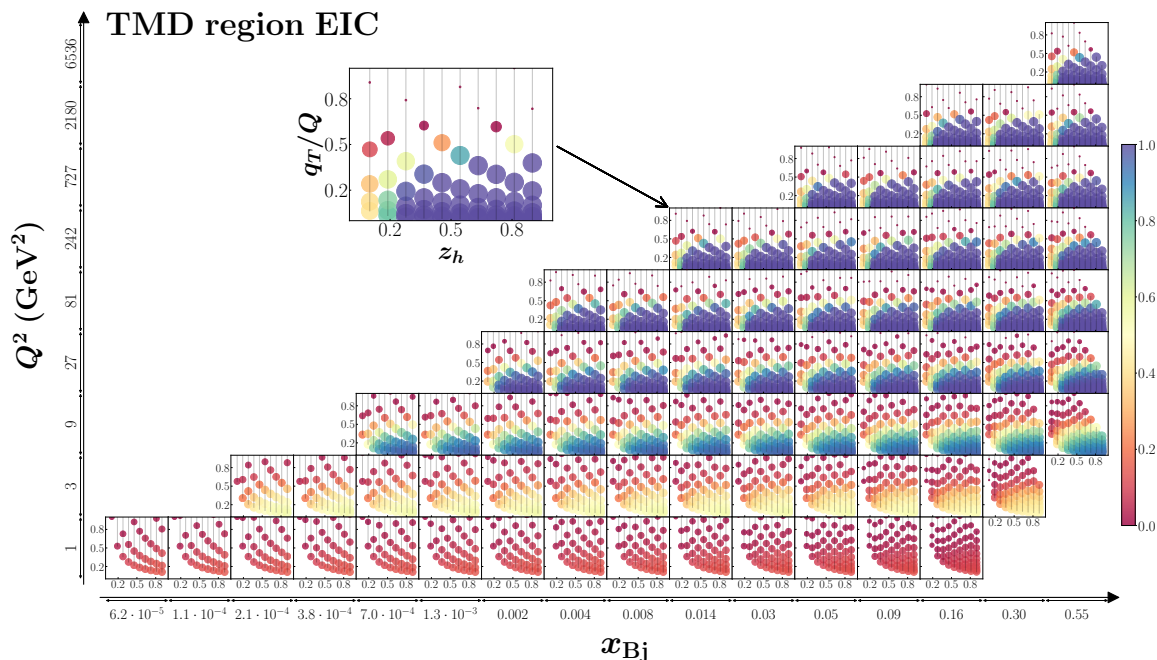


FIG. 19. TMD affinity for EIC kinematics. Bin centers are located in the points corresponding to the bin averaged values of  $x_b$  and  $Q^2$ , and in each of these bins various values of  $z_h$  and  $q_T/Q$  can be measured. In each bin of fixed  $z_h$  and  $q_T/Q$ , the affinity is indicated by a dot with size proportional to the corresponding affinity value. The affinity is color coded according to the scheme on the right of the panels: red (and smaller) symbols correspond to low TMD affinity, while dark blue (and larger) symbols correspond to high TMD affinity. The plot is from Ref. [183]

917 PDFs and fragmentation functions offering a new venue to constrain collinear distributions using TMD observables.  
 918 While the experimental data is sensitive to all regions in coordinate space, as discussed above, the relative contribution  
 919 of each region to the physical observables depend on the kinematics of the final state particles accessible at a given  
 920 collision energy. Because of this, different collision energies from low to high at high luminosity is needed at the EIC  
 921 in order to systemically probe TMDs at different regions of coordinate space. In the sections below, we concentrate  
 922 on the impact on the unpolarized TMD PDFs as well as the Sivers TMD PDF as exemplary cases that would profit  
 923 from increased precision at moderate energies.

924

### 3. The impact study on the unpolarized TMDs

925 The unpolarized TMD distributions and fragmentation functions have been extracted in Refs. [179–182, 185] (SV17,  
 926 PV17, SV19, PV19, MAPTMD22) with high perturbative accuracy up to NNLO and up to  $N^3\text{LL}$  of TMD logarithmic  
 927 resummation. The data used in these global analyses includes Drell-Yan and SIDIS processes measured at fixed  
 928 target experiments [186–194] at relatively low energies, and the collider measurements at higher energy scales [195–  
 929 207]. The span in the resolution scale  $Q$  and in observed transverse momentum  $q_T$  allows for an extraction of the  
 930 non-perturbative Collins-Soper kernel (CS-kernel) and the unpolarized TMDs. These extractions demonstrate an  
 931 agreement between the theory and the experimental measurements.

932 The extremely precise LHC measurements at  $Q \simeq M_Z$  provide very stringent constraints on the CS-kernel and  
 933 TMDs in the region of small values of  $b$ . However, the uncertainty of extractions grows in the region of  $b > 1$   
 934  $\text{GeV}^{-1}$  due to the lack of the precise low- $q_T$  data. The large  $b$  region is important for the understanding of the  
 935 non-perturbative nature of TMDs and the primordial shapes TMDs and CS-kernel. In particular for the  $Q$  range  
 936 accessed by intermediate energies,  $Q \geq 5 - 10 \text{ GeV}$ , TMDs are only very poorly constrained. Low and intermediate  
 937 energies at the EIC will naturally provide precision data in this kinematic regime as shown below. Predictions from  
 938 various groups are different in this region, see Ref. [208], and also disagree with the lattice measurements [209–211].

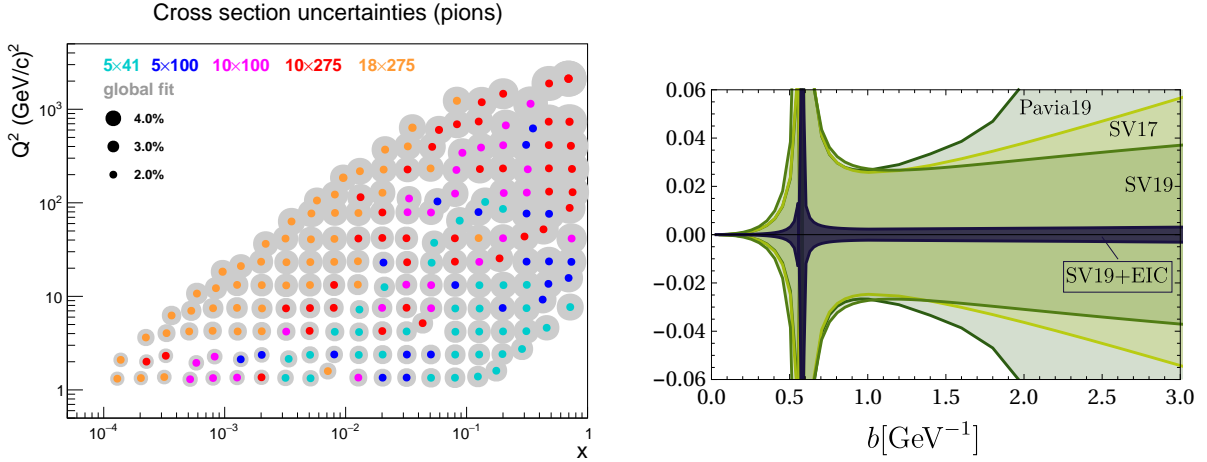


FIG. 20. Left: Impact on unpolarized TMD measurements integrated within  $0 < q_T/Q < 1.0, z > 0.2$ , figure from Athena Proposal. Fit based on P17. The color-code shows the datasets with the highest impact at a given  $x, Q^2$  point. The assumed systematic uncertainty of 2% point-to-point is dominating. However, the extraction of a specific point in  $b$  is sensitive to the collected statistics as shown in the right plot. Right: Impact of the EIC data on the extraction of the CS kernel as function of  $b$  ( $\text{GeV}^{-1}$ ) at  $\mu = 2$  GeV using SV19 as a baseline compared to several other global extractions not using EIC data. Figure from the Yellow Report [8].

939 This disagreement is problematic since it points to a limited understanding of the TMD evolution encoded in the  
 940 CS-kernel, which dictates the evolution properties of all TMDs and describes properties of the QCD vacuum [208].  
 941 The measurements from the EIC will fill in the gap between the low-energy and high-energy experiments, and will  
 942 pin down these functions at higher values of  $b$  corresponding to lower values of  $k_T$ . Ultimately, it will help to unravel  
 943 the 3D nucleon structure in a very wide kinematic region.

944 The unpolarized structure function is the leading contribution to the differential SIDIS cross-section and also serves  
 945 as the weight for polarized asymmetries. As discussed above, mapping the unpolarized TMD over the full phase  
 946 space is also necessary to probe TMD evolution effects which partially cancel in the extraction of spin asymmetries.  
 947 Therefore, the knowledge of unpolarized TMDs is of paramount importance for the whole momentum tomography  
 948 program.

949 To demonstrate the impact, in particular of medium- and low energy data, we consider the PV17 and SV19-fits.  
 950 Figure 20, left shows the relative impact of the different energy options on the extraction of the PV17 based TMD fit.  
 951 It is evident, that low and medium energies dominate over a wide range of phase space, in particular at intermediate  
 952  $x - Q^2$ . This is even more impressive considering that the impact plot is based on the baseline luminosities.

953 The estimation of the impact on the nonperturbative parts of the CS-kernel and unpolarized TMDs has been done  
 954 using the SV19-fit as the baseline. The analysis was performed with the inclusion of EIC pseudo-data (in  $5 \times 41$ ,  
 955  $5 \times 100$ ,  $10 \times 100$ ,  $18 \times 100$  and  $18 \times 275$  beam-energy configurations). The pseudo-data, generated by PYTHIA [212],  
 956 includes expected statistical and estimated systematic uncertainties, for a hand-book detector design with moderate

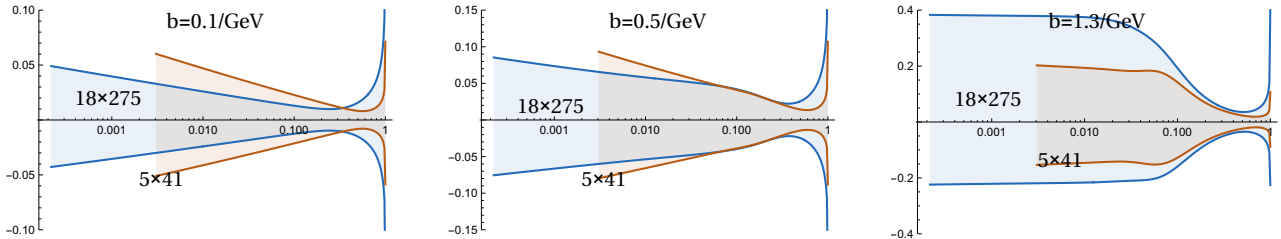


FIG. 21. Comparison of relative uncertainty bands for unpolarized u-quark TMD PDFs at different values of  $b$  as a function of  $x$ . Lighter blue band is the impact of  $18 \times 275$  data, light brown band is the impact of  $5 \times 41$  EIC pseudo data. The dataset used for these projections is the same as used for the Yellow Report [8]. In particular all energy options use the same integrated luminosity.

957 particle identification capability. The estimate for the improvement in the uncertainties for the extraction of the  
 958 unpolarized TMDs is shown in the right panel in Fig. 20 exemplary for  $f_{1T}^u$ . In general, the main impact in the  
 959 unpolarized sector occurs for the CS-kernel, whose uncertainty reduces by a factor of  $\sim 10$ . This is only possible with  
 960 precise and homogeneous coverage of the  $(Q, x, z)$  domain, which can efficiently de-correlate the effects of soft gluon  
 961 evolution and internal transverse motion.

962 Fig. 21 shows the impact of the same integrated luminosity with the highest,  $18 \times 275$ , energy configuration and the  
 963 lowest,  $5 \times 45$  energy configuration on the extraction of the unpolarized u-quark TMD PDFs at different values of  $b$   
 964 as a function of  $x$ . As expected, the lower energy data has a significant impact to constrain the PDF at in the valence  
 965 quark region for all  $b$  and over the majority of the  $x$  range at higher values of  $b$ . This is thanks to the sensitivity to  
 966 smaller values of  $p_T$ . Notice that the high energy option has little impact in the valence region, as large  $x$  values can  
 967 only be accessed at large  $Q^2$ . The combination of low and high energy measurements will have the most homogeneous  
 968 coverage of the kinematics required for the studies of TMDs.

969

#### 4. The impact study on the Sivers functions

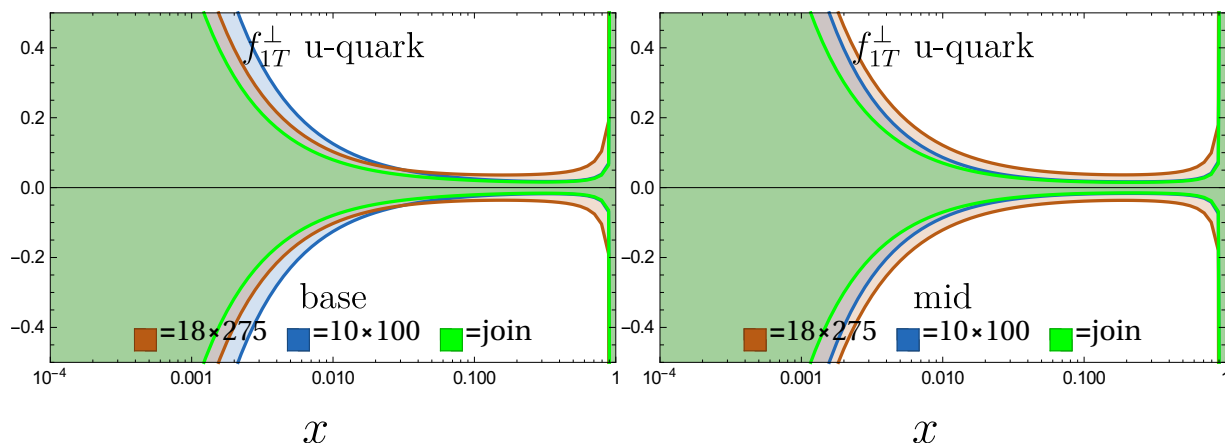


FIG. 22. Expected impact on the u-quark Sivers functions as a function  $x$  as obtained from semi-inclusive pion and kaon EIC pseudo-data for  $10 \times 100$ ,  $18 \times 275$  beam-energy configurations and the combined impact. Fit uses pseudodata from the EIC reference detector described in the Yellow Report [8] and `SV19` fit. Left: impact of equal time data taking with the base configuration, right: impact of proposed luminosity increase at low and mid energies.

970 The non-vanishing Sivers asymmetry triggered a lot of interest in the physics community and many groups have  
 971 performed extractions of the Sivers functions from the available experimental data [213–226]. However, currently  
 972 the global pool of Sivers asymmetry measurements offers a relatively small number of data points that could be  
 973 consistently analysed using the TMD factorization approach. The future measurements by the EIC will provide a  
 974 significant amount of new data in a wide and unexplored kinematic region, and thus have a decisive impact in the  
 975 determination of the Sivers functions.

976 To determine the impact of EIC measurements on the Sivers function, the pseudo-data generated by PYTHIA-6  
 977 [212] was used with a successive reweighing by a phenomenological model for the Sivers and unpolarized structure  
 978 functions from Ref. [216]. The pseudo-data for  $\pi^\pm$  and  $K^\pm$  production in  $e + p$  and  $e + {}^3\text{He}$  collisions at the highest  
 979 ( $18 \times 275$ ) and the lowest ( $5 \times 41$ ) beam-energy configurations were analyzed. The resulting pseudo-data set is about  
 980 two orders of magnitude larger in comparison with the current data. Performing the fit of the new pseudo-data with  
 981 the initial set of Sivers functions taken from the global analysis made in Refs. [225, 226] and based on the current  
 982 SIDIS [227–231] and Drell-Yan [232, 233] measurements, a substantial reduction of uncertainties is obtained. The  
 983 uncertainty bands are reduced by an order of magnitudes for all flavors.

984 Fig. 22 shows the impact on the uncertainty of the u-quark Sivers function at  $b = 0 \text{ GeV}^{-1}$  as a function of  $x$ .  
 985 The distribution of impact between  $5 \times 41$  and  $18 \times 275$  beam-energy configurations is similar to the unpolarized  
 986 case. Namely,  $5 \times 41$  configuration constrains mainly the large- $x$  region, while  $18 \times 275$  configuration constrains  
 987 the low- $x$  region. The combined set of the data gives the most homogeneous error reduction. In turn, it reduces  
 988 significantly uncertainties of the integral characteristics. For example, the integral over Qiu-Sterman function has  
 989 about 3% uncertainty (in the combined case) versus 6% (for  $18 \times 275$  case) or 12% (for  $5 \times 41$  case). Figure 14

shows the projected experimental uncertainties compared to projections based on the extraction in Ref. [223] for more energy options and vs  $Q^2$ . Intermediate energies are most advantageous, since the expected asymmetries are large while still enough statistics for a multi-dimensional analysis are collected. This is in particular evident when plotting the asymmetries vs  $Q^2$  where the drop of the expected asymmetries at high  $Q^2$  can be observed as well as the drop of statistics expected from the EIC in the valence region at high  $Q^2$ .

### 5. TMDs in nuclei

QCD multiple scattering in the nuclear medium has been demonstrated to be responsible for the difference between TMDs in bound and free nucleons within a generalized high-twist factorization formalism [234] and the dipole model [235, 236]. In these models, the scale of the power corrections which modify the relevant distribution for the process is proportional at leading order to  $\alpha_s(Q)$ , which becomes small at large  $Q$ , see for instance [237, 238]. Thus while the EIC will be capable of performing  $e - A$  collisions for a wide range of nuclear targets, a low center of mass energy is optimal for probing nuclear medium modifications to TMDs.

From a phenomenological standpoint, nuclear modifications to collinear PDFs have been performed in Refs. [239–250] and for the collinear fragmentation function in Ref. [251, 252]. In these global analyses, the medium modifications to the distributions enter into the non-perturbative parameterizations. In the TMD description, the QCD multiple scattering naturally leads to a broadening of the transverse momentum distributions. Recently, the first extraction of the unpolarized nuclear modified TMDs have been performed in Ref. [253]. The authors of this paper performed a global analysis at NLO+NNLL to the world set of experimental data from hadron multiplicity production ratio at HERMES [254], Drell-Yan reactions at Fermilab [255, 256] and RHIC [257], as well as  $\gamma^*/Z$  production at the LHC [258, 259]. In analogy to the work that has been done in the past, this analysis took the medium modifications to enter into the non-perturbative parameterization of the collinear distributions as well as the parameterization for the non-perturbative Sudakov factor, which controls the broadening of the transverse momentum distribution. Despite the success of work in [253] in describing the world set of experimental data, there are currently few data points which can be used in order to constrain the TMD FFs. While the HERMES measurement of the hadron multiplicity ratio probed a relatively wide kinematic region, the stringent kinematic cuts applied to ensure the data are within the proper TMD region vastly reduces the total number of useful experimental points. Since Semi-Inclusive DIS is sensitive to both the TMD PDFs as well as the TMD FFs, experimental measurements within the broad kinematical reach of EIC at small and medium  $Q$  represents the optimal process for probing nuclear modifications to TMDs.

### D. Jet Hadronization Studies

Jets are collimated sprays of particles, which are observed in collider experiments. They exhibit a close connection to energetic quarks and gluons that can be produced in hard-scattering processes at the EIC [260–265]. Besides event-wide jet measurements, significant progress has been made in recent years to better understand jet substructure observables, see Refs. [266–268] for recent reviews. Jet substructure observables can be constructed to be Infrared and Collinear Safe making them less sensitive to experimental resolution effects. Nevertheless, hadronization corrections can be sizable for these observables. For several jet substructure observables it is possible to connect the relevant hadronization correction to universal functions. The scaling of these functions can be predicted from first principles which can be tested experimentally by studying jets at different energies and by varying parameters of specific observables. EIC jets at different center of mass energies have different quark/gluon fractions and a different quark flavor decomposition. Therefore, the measurement of jets at high luminosity and low center of mass energies can provide important complementary information to better disentangle the flavor decomposition of the hadronization corrections of jets and also to study their correlation with different initial state PDFs. Several jet observables in the literature have been studied which are particularly sensitive to the quark flavor and quark/gluon differences. Examples include jet angularities [269–272], the jet charge [273, 274], angles between jet axes [275], groomed jet substructure [276], flavor correlations [277], energy-energy correlators [278–280], jets at threshold [281, 282], and T-odd jets [283, 284]. The EIC provides a clean environment with a minimal background contamination from the underlying event/multi-parton interactions making it an ideal place to study low-energy aspects of jets. In addition, the measurements of jets for multiple jet radii at different energies may help to explore in detail the connection of hadron and jet cross sections. Recently, it was demonstrated that inclusive hadron cross sections can be obtained from inclusive jet calculations by taking the limit of a vanishing jet radius [285, 286].

An important aspect of jet observables is their sensitivity to TMD PDFs and FFs. For example, lepton-jet cross sections in the laboratory frame [287–289] and the Breit frame [290–292] give access to (spin-dependent) quark TMD PDFs where the final state radiation can be calculated perturbatively. Similarly, di-jet production can be used to

study gluon TMD PDFs [293, 294]. Moreover, the transverse momentum of hadrons inside the jet relative to the jet axis can provide access to TMD FFs, which is independent of initial state TMD PDFs [295]. Here the choice of the jet axis is important and different physics can be probed [296]. Especially, due to the separation of initial and final state TMD PDFs and FFs, jet observables can provide important complementary information to semi-inclusive deep inelastic scattering. All of these observables and the information content they provide benefit greatly from measurements over a wide kinematic range. In particular, high luminosity at the EIC will allow for a unique quark flavor decomposition.

A measurement that is in particular luminosity hungry, is the detection of diffractive di-jet events. This observable is sensitive to the elusive Generalized TMDs (GTMDs) [297, 298] of gluons. Lower collision energies provide constraints for the moderate  $x$ -range of the gluon distribution, while higher energies are sensitive to the small- $x$  gluon distribution. If, as typically assumed, the gluon spin (helicity and orbital angular momentum) is sizable at moderate  $x$ , it is critical to have very high luminosity at lower/intermediate collision energies at the EIC.

## IV. EXOTIC MESON SPECTROSCOPY

### A. Motivations for an exotic spectroscopy program at the EIC

Modern electro/photoproduction facilities, such as those operating in Jefferson Lab, have demonstrated the effectiveness of photons as probes of the hadron spectrum. However the energy ranges of these facilities are such that most states with open or hidden heavy flavor are out of reach. This is unfortunate as there remains significant discovery potential for photoproduction in this sector. Already electron scattering experiments at HERA [299, 300] observed low-lying charmonia, demonstrating the viability of charmonium spectroscopy in electroproduction at high-energies but were limited by luminosity. Now the proposed EIC, with high luminosity, will provide a suitable facility for a dedicated photoproduction spectroscopy program extended to the heavy flavor sectors. In particular, the study of heavy-quarkonia and quarkonium-like states in photon-induced reactions will not only be complementary to the spectroscopy programs employing other production modes but may give unique clues to the underlying non-perturbative QCD dynamics.

One of the most striking features of quarkonium spectra is the wealth of observed experimental signals which seem to indicate an exotic QCD structure beyond conventional  $Q\bar{Q}$  mesons. Starting with the observation of the narrow  $\chi_{c1}(3872)$  in the  $J/\Psi \pi^+ \pi^-$  invariant mass spectrum by the BELLE Collaboration in 2003 [301], these states, collectively denoted the  $XYZ$ 's, now number in the dozens. The dramatic change in landscape from 2003 up to 2021 is illustrated in figure 23 where new states beyond quark model charmonium are highlighted. These states exhibit properties which are not consistent with expectations of conventional QCD bound states, for example : large isospin violation in the case of the  $\chi_{c1}(3872)$ ; iso-vector quarkonium-like character for the  $Z$ 's; supernumeracy of the vector  $Y$  states. We refer to reviews such as [302, 303] for more detailed discussion. The underlying dynamics governing their nature is not unambiguously known. The experimental signals of these states, usually in the form of sharp peaks in invariant mass spectra or broader enhancements that are required to describe distributions in a more complex amplitude analysis, allow multiple interpretations of their structure, e.g. multi-quark states, hadron-hadron molecules, kinematic cusps or triangle singularities. Disentangling these possibilities is one of the foremost missions of exotic spectroscopy and would further our understanding of the non-perturbative nature of QCD in heavy sectors.

One challenge in this endeavor is that, with few exceptions, the  $XYZ$  signals have only been observed in single production modes, usually  $e^+e^-$  annihilation or  $B$  meson decays. Observation of any of these states at the EIC through photoproduction would thus provide independent and complementary verification of their existence. Further, an ubiquitous feature of  $XYZ$  signals is their proximity to open thresholds and the presence of additional particles in the reconstructed final state. This complicates the interpretation of experimental peaks as complicated kinematic topologies involving nearby open channels may modify or mimic a resonant signal. Here photoproduction provides a unique opportunity to produce  $XYZ$  in isolated final states, thus alleviating the role of kinematic singularities. In this way a null result may be equally important towards uncovering the spectrum of genuine bound-states. Additionally the polarized electron and proton beam setups enable the determination of spin-parity assignments of states for which these are not yet known. The EIC would also have real discovery potential for exotic heavy flavor mesons.

A dedicated spectroscopy effort can make meaningful contributions to several aspects of non-exotic quarkonium physics. Theoretical understanding of photoproduction processes conventionally rely on Regge theory and exchange phenomenology which have been tested extensively in the light sector [304]. Measurement of quarkonium photoproduction cross-sections serves as a testing ground of scattering phenomenology in heavy sectors where perturbative QCD inputs may also be used. In particular the microscopic structure of  $\gamma Q\bar{Q}$  interaction and assumptions such as Vector Meson Dominance (VMD) may be tested [305, 306].

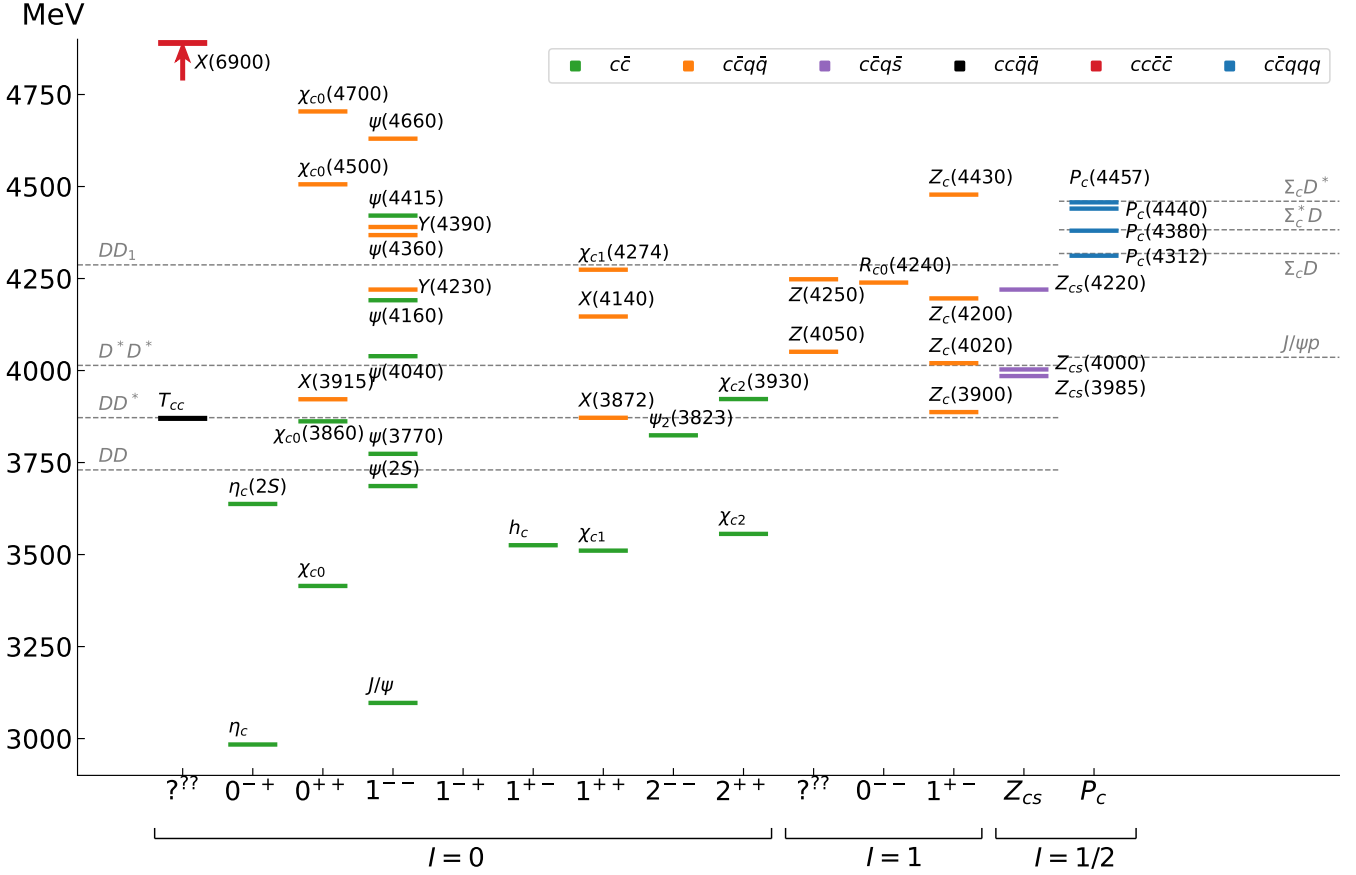


FIG. 23. Experimentally measured charmonia, XYZ and pentaquark spectra from [311]. A '??' refers to unknown spin or parity.

1095 Beyond the charmonium sector, the energy reach of the EIC will also allow the study of near-threshold bottomo-  
 1096 nium photoproduction which may be sensitive to the trace anomaly contribution to the nucleon mass and would be  
 1097 complementary to ongoing studies of  $J/\Psi$  photoproduction studies currently underway at Jefferson Lab [307, 308].  
 1098 Further, this mass range is predicted to also exhibit a rich landscape of pentaquark-like structures [309, 310] the as  
 1099 yet unobserved hidden-bottom partners of the  $P_c$  signals observed in the  $J/\Psi p$  mass spectra in  $\Lambda_c$  decays.

1100

### 1. Photoproduction with the EIC

1101 Given the many physics opportunities around photoproduction of heavy quarkonia, new measurements at the EIC  
 1102 will be essential for understanding both exotic and conventional quarkonium spectra. Photoproduction provides a  
 1103 flexible production mode, able to produce the full spectrum of hadrons of any quantum number. This gives such  
 1104 measurements significant discovery potential and allows mapping out of patterns within the observed spectrum. The  
 1105 trade-off however is that the cross sections for photoproducing heavy mesons are small, only up to  $\mathcal{O}(1 \text{ nb})$ , meaning  
 1106 a dedicated spectroscopy program will require high luminosity at sufficiently large centre-of-mass energies to make  
 1107 a meaningful contribution. The proposed EIC, maintaining high luminosity at its lower centre-of-mass energies,  
 1108 would be well placed to meet these conditions. In particular, even with the lower centre-of-mass settings of 29 and  
 1109 45 ( $\text{GeV}/c^2$ ) there is sufficient energy to directly produce many exotic states of interest in the charmonium sector  
 1110 without the constraints in bounds from parent masses which occur in decay processes. Kinematic generation of peaks  
 1111 through final state interactions, such as triangle diagrams, will also be suppressed over the entire  $W$  range.

1112 When combined with complete measurement of the final state, the polarized electron and proton beams offer means  
 1113 for detailed partial wave analysis to disentangle overlapping states, deduce the quantum numbers of resonant states  
 1114 and study production mechanisms. This is of particular importance for many of the excited  $XYZ$  states which have  
 1115 intrinsically greater decay widths and contribute to more complicated final states. The use of partial-wave analysis



through polarized photoproduction set-ups for exotic searches is currently being pursued in the light-quark sector at the GlueX experiment and much of the expertise will be readily applicable to the EIC setup. This includes the possibility to measure polarized cross-sections, spin density matrix elements, and asymmetries.

The variable beam setups of the EIC allow exploration of Primakoff production of axial vector charmonium [312] and simultaneous measurement of charged charmonium-like isospin multiplets with deuteron beams. Additionally, the electroproduction mode of the EIC allows measurement of  $Q^2$  dependence and photocouplings, a detailed study of which may be a reliable probe of the microscopic nature of exotic hadrons [313, 314]. Electroproduction studies are of particular importance for the  $\chi_{c1}(3872)$  and the closely related  $\tilde{X}(3872)$  candidate claimed in muoproduction by the COMPASS experiment in the  $J/\Psi\pi^+\pi^-$  mass spectrum [315]. Although this new state closely resembles the  $\chi_{c1}(3873)$  in mass and width, its dipion mass distribution was suggestive of a scalar wave instead of the usual  $\rho J/\Psi$  decay mode of the  $\chi_{c1}(3872)$ , implying a different C-parity. Further this state was observed in production with an additional pion in the final state but not in exclusive production, raising further questions as to the nature of the muoproduced peak. Detailed study of the  $J/\Psi\pi\pi$  mass spectra in virtual photoproduction would help to understand the COMPASS result.

## 2. States of interest

The first goal of an exotic spectroscopy program will be to identify the production of the most established states,  $\chi_{c1}(3872)$ ,  $Y(4260)$  and  $Z_c(3900)$ . The decay of these states to a  $J/\Psi$  and pions will provide a clean and well studied final state and we discuss in Section (IV B 5) the prospects for measuring this with the EIC. After that there are many open questions in XYZ physics, particularly with respect to the nature of peaks in invariant mass distributions which we hope to address. Here we consider a few examples with decays which should be readily measurable and make rate estimates for these in Section (IV B 4).

A recent publication from LHCb show structure in the  $J/\Psi K^+$  mass spectra which they can reproduce with the addition of two new resonances with strangeness and hidden charm,  $Z_{cs}(4000)$  and  $Z_{cs}(4220)$  [316] with widths around 100-200 MeV. A similar, narrower state, the  $Z_{cs}(3985)$ , has also been seen in  $K^+ D\bar{D}^*$  by BESIII [317].

The  $X(6900)$  or  $T_{c\bar{c}c\bar{c}}$ (6900) tetraquark candidate has been seen from its decay to  $2J/\Psi$  [318]. Analogue Z states have been seen in the b-quark sector by Belle, with the  $\Upsilon$  or  $h_b$  mesons in combination with a charged pion [319]. Production of these states are also well within EIC centre-of-mass energies. In addition, spectroscopy at the EIC will be able to search in a variety of other final states replacing pions for other mesons such as vectors. We can also look for charm quarks via reconstructing D mesons the most accessible decay mode of which will be  $K^-\pi^+$  with a branching ratio of around 4%, while the decay of XYZ into final states with D mesons is likely to be quite high. As seen later XYZ decay products populate the detector region relatively uniformly giving good potential for reconstructing events including pairs of D mesons. This would be particularly useful for investigating the molecular picture of these states.

## B. Estimates for the EIC

### 1. JPAC Photoproduction Amplitudes

In order to estimate the feasibility of quasi-real photoproduction for states of interest at EIC energies we followed the approach of a recent JPAC Collaboration study in [312]. Here, general principles are used to construct exclusive photoproduction amplitudes of the charmonium states of interest on the per-helicity-amplitude basis. In this way, full kinematic dependence is retained and the production may be propagated along decay chains to reconstructed final states.

In general the amplitude of producing a meson,  $Q$  via the exchange of a particle,  $\mathcal{E}$  with spin  $j$  take the form:

$$\langle \lambda_\gamma \lambda_N | T_{\mathcal{E}} | \lambda_Q, \lambda_{N'} \rangle = \mathcal{T}_{\lambda_\gamma \lambda_Q}^\mu \mathcal{P}_{\mu\nu}^{(\mathcal{E})} \mathcal{B}_{\lambda_N \lambda_{N'}}^\mu \quad (39)$$

where  $\mathcal{T}$  and  $\mathcal{B}$  are Lorentz tensors of rank- $j$  and given by effective interaction Lagrangians which provide an economical way to satisfy kinematic dependencies and discrete symmetries of the reaction. Such methods have been widely used to motivate searches for exotic hadrons through photoproduction [320–328] The form of the exchange propagator,  $\mathcal{P}$ , provides means to consider production in two kinematic regions of interest: near-threshold and at high-energies, where production is expected to proceed through exchanges of definite-spin and Reggeized particles respectively. The center-of-mass range available at the EIC provides wide coverage in energy, thus for first estimates we used a simple linear interpolation between the low- and high-energy models provided in [312].

## 2. Electroproduction

We generalized the aforementioned (real) photoproduction to consider exclusive electroproduction with low- $Q^2$  quasi-real virtual photons via a factorized model whereby the amplitude for producing a virtual photon beam is followed by the t-channel photoproduction of the meson. The produced meson subsequently decays to specific final states which can be measured in the EIC detector:

$$\frac{d^4\sigma}{ds dQ^2 dt d\phi} = \Gamma(s, Q^2, E_e) \frac{d^2\sigma_{\gamma^*+p \rightarrow V+p}(s, Q^2)}{dt d\phi} \quad (40)$$

$\Gamma(s, Q^2, E_e)$  is the virtual photon flux and  $\frac{d^2\sigma_{\gamma^*+p \rightarrow V+p}(s, Q^2)}{dt d\phi}$  is the two-body photoproduction cross section calculated from the model of [312], modified by an additional  $Q^2$  dependence taken from [329]. Eqn. (40) was integrated numerically to give the total cross section for determining event rates. Note, the virtual photon flux integration leads to a factor of around 0.2 for the case of  $\chi_{c1}(3872)$  production relative to real photoproduction for the 5x41 GeV beams.

## 3. Other Models

To estimate how reliable our production rates may be we compared to other approaches that have been published recently.

In [330] a semi-inclusive production mechanism for hadron molecules was investigated. Here the molecular constituents were first photoproduced via Pythia, and then allowed to interact together in given  $X$  and  $Z$  states. Cross sections for semi-inclusive production were given for the highest proposed EIC centre-of-mass energy for  $\chi_{c1}(3872)$ ,  $Z_c$  and  $Z_{cs}$  and are compared to our estimates for exclusive production in Table I. While the estimates for  $\chi_{c1}(3872)$  are an order of magnitude lower than this work, the  $Z_c$  cross section is an order of magnitude higher. We note that the calculations of [330] should be valid for larger  $Q^2$ , in the central region (large  $p_T$ ), those from [312] should be valid at  $Q^2 < 1(\text{GeV}/c^2)^2$ , and peak in the peripheral region (small  $p_T$ ), where we expect the bulk of events to be produced.

Using the same method, Ref. [331] estimates the semi-inclusive production rates of more exotic hadrons, and finds that copious  $P_{cs}$  pentaquarks and  $\Lambda_c \bar{\Lambda}_c$  dibaryons can be produced at EIC. It is also promising to search for double-charm tetraquarks at EIC. In addition, Ref.[2208.02639] also suggests that the possible 24 GeV upgrade of CEBAF [proper ref.] can play an important role in the search of hidden-charm tetraquarks and pentaquarks.

A very similar approach to the current work is taken in [332], where the models of [312] were coupled to a virtual photon produced from electron-proton scattering interactions. Their results are compared to ours in table I, where our estimates are just over a factor 2 lower for the low energy setting and more comparable for the high energy setting. The differences are likely due to our interpolation of low and high models, or handling of phase space and virtual photon flux factors when performing the integration. The threshold at  $Q^2 > 0.01 (\text{GeV}/c^2)^2$  is applied in this comparison but not in our later results where we integrate the full allowable  $Q^2$  range.

In general we can expect integrated cross sections for electroproduction of up to order 1 nb for production of mesons with charm quarks.

TABLE I. Model Comparisons. Note, in the Lanzhou calculations cuts are applied to  $Q^2$  and  $W$ , as indicated in the column title with units in GeV. The same cuts are applied to our calculation when comparing to Lanzhou, but not to the comparisons with Yang. The cut on  $W > 20 \text{ GeV}/c^2$  has a very large effect on the calculated electroproduction cross sections as the photoproduction cross section for  $X$  and  $Z$  of [312] falls rapidly.

	3.5x20 $Q^2 > 0.01; W < 16$		18x275 $Q^2 > 0.01; 20 < W < 60$		18x275 $Q^2 > 0$	
	JPAC	Lanzhou[332]	JPAC	Lanzhou[332]	JPAC	Yang[330]
$\chi_{c1}(3872)$	0.47 nb	1.2 nb	0.00014 nb	0.00021 nb	3.5 nb	0.216-0.914 nb
$Y(4260)$	0.06 nb	0.2 nb	1.5 nb	2.0 nb	14 nb	-
$Z_c^+(3900)$	0.06 nb	0.16 nb	0.00018 nb	0.00048 nb	0.41 nb	3.8-14 nb

TABLE II. Summary of results for production of some states of interest at the EIC electron and proton beam momentum  $5 \times 100(\text{GeV}/c)$  (for electron x proton). Columns show : the meson name; our estimate of the total cross section; production rate per day, assuming a luminosity of  $6.1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ ; the decay branch to a particular measurable final state; its ratio; the rate per day of the meson decaying to the given final state.

Meson	Cross Section (nb)	Production rate (per day)	Decay Branch	Branch Ratio (%)	Events (per day)
$\chi_{c1}(3872)$	2.3	2.0 M	$J/\Psi \pi^+ \pi^-$	5	6.1 k
$Y(4260)$	2.3	2.0 M	$J/\Psi \pi^+ \pi^-$	1	1.2 k
$Z_c(3900)$	0.3	0.26 M	$J/\Psi \pi^+$	10	1.6 k
$X(6900)$	0.015	0.013 M	$J/\Psi J/\Psi$	100	46
$Z_{cs}(4000)$	0.23	0.20 M	$J/\Psi K^+$	10	1.2 k
$Z_b(10610)$	0.04	0.034 M	$\Upsilon(2S) \pi^+$	3.6	24

1198

#### 4. Estimates

1199 In table II we give estimates for the production of a variety of exotic states with the EIC. These are based on the  
 1200 models and parameters detailed in [312], with the addition of the  $Z_{cs}(4000)$  production using kaon exchange; and the  
 1201 modification of the X(6900) model to use a higher branching ratio to  $\Psi\omega$  of 3%, which was previously taken as 1%.  
 1202 These estimates assume a luminosity of  $10^{34} \text{ cm}^{-2}\text{s}^{-1}$ . The additional branching ratios, used to calculate events per  
 1203 day, of  $J/\Psi \rightarrow e^+e^-$  was taken as 6% and  $\Upsilon(2S) \rightarrow e^+e^-$  as 1.98%.

1204 Current measurements of X and Y states contain up to order 10 thousand and 1 thousand events respectively. This  
 1205 is similar to the daily production rate of our estimates. So with an overall detector acceptance of order 10 % the EIC  
 1206 would be able to make significant contributions to our understanding of these states.

1207 We note that a previous investigation of charged final states in electroproduction at an electron-ion collider [333]  
 1208 through a Regge exchange mechanism found similar production rates for the  $Z_c(4430)$ , approximately a factor 2 lower  
 1209 than our estimates for the  $Z_c(3900)$ . They also conclude that the final state rapidity depends on the beam energy, at  
 1210 lower center of mass energies production shifts toward mid-rapidity, where the final state may be reconstructed in a  
 1211 central detector.

1212

#### 5. Detection of final states

1213 Meson photoproduction at the EIC will require a detector with full hermicity. Quasi-real photoproduction results in  
 1214 the scattered electron being very close to the incident beam line. t-channel production provides very little transverse  
 1215 momentum for the recoiling baryon, which will likewise be scattered within a degree or so of the beam. On the other  
 1216 hand the meson itself will be produced relatively centrally at the lower centre-of-mass settings making for excellent  
 1217 detection of its decay products.

1218 The individual particle momentum distributions for the 5x100 centre-of-mass setting are shown in Fig. 24. Also  
 1219 shown are the distributions expected when reconstructed with the EIC Yellow Report matrix detector via the eic-  
 1220 smear package [8]. It is clear the meson decay products are almost entirely directed at the high acceptance central  
 1221 detector region. Protons pass to the far-forward detector region, while there is some electron detection in the backward  
 1222 electron region.

1223 For final states including a  $J/\Psi$ , which are mostly under consideration here, excellent electron/pion separation will  
 1224 allow a clean tag of  $J/\Psi$  events through its narrow width in the  $e^+e^-$  invariant mass. Coupled with a very high  
 1225 detection efficiency this should allow for full identification of the meson decay products and provide a means for peak  
 1226 hunting in many final states including a final  $J/\Psi$ .

1227 Supplementing the meson detection with far-forward and far-backward detector systems will enhance the spec-  
 1228 troscopy program by allowing measurements of the full production process, that is measurement of the reaction  
 1229 variables W, from the  $e^-$  and  $t$  from the recoil baryon. Detecting the scattered electron also allows determination of  
 1230 the longitudinal and transverse polarisation components of the virtual photon, providing further information on the  
 1231 production processes through access to the meson spin density matrix elements. This can be done with the backward  
 1232 detector around 5-10% of the time when the electron beam momentum is lowest (5 GeV), due to the transverse kick  
 1233 to the electron from the Lorentz boost due to the more energetic proton. A dedicated far-backward electron detector  
 1234 such as the proposed low- $Q^2$  tagger could increase the electron detection rate significantly. Detection of both the  
 1235 electron and baryon can also allow for superior background rejection for exclusive event reconstruction.

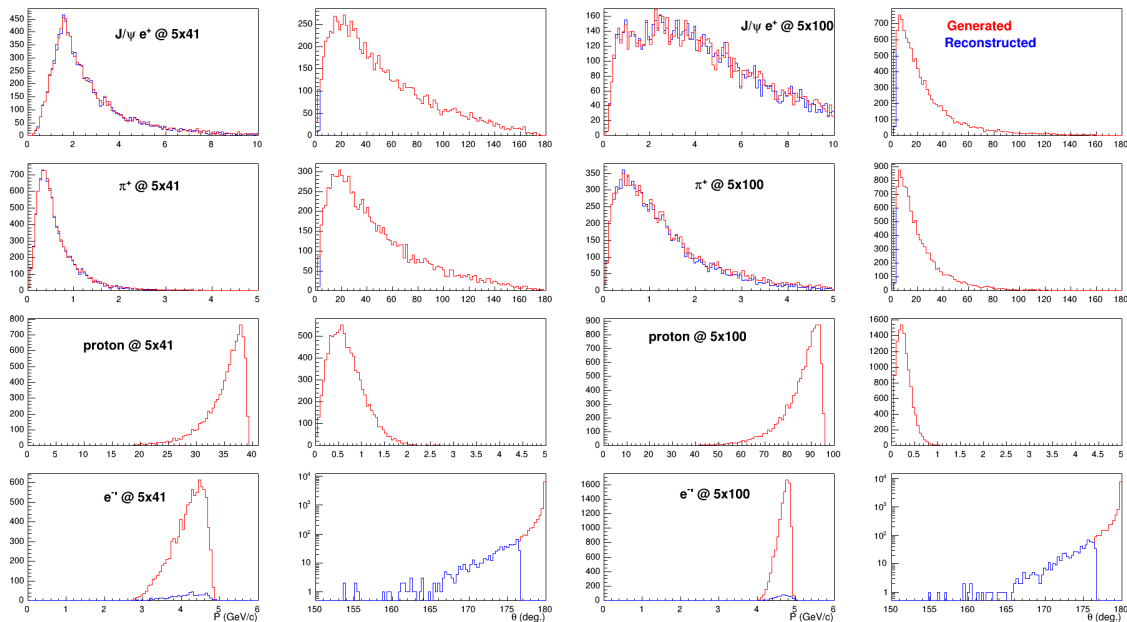


FIG. 24. Momentum and angle distributions for X production. Left(right) columns are for beam configuration 5x41(5x100). Rows, from top to bottom, show  $J/\Psi$  decay  $e^+$ ; X decay  $\pi^+$ ; the scattered proton; and the scattered electron. Red lines show the true generated distributions while blue are the detected particles as expected with the EIC Yellow Report matrix detector.

1236

### C. Outlook

1237 We have briefly examined the case for producing exotic mesons through quasi-real photoproduction at the EIC.  
 1238 Although it is difficult to make strong statements on what we might expect this is exactly due to the uncertainty  
 1239 around the nature and structure of the new states seen at other labs. We have shown that if real exotic states exist  
 1240 then many of these should have sufficiently high cross sections to be measurable. The low centre-of-mass configurations  
 1241 are particularly suited to mesons produced through fixed spin exchanges of light mesons, which have a high cross  
 1242 section close to threshold. Coupled with a high luminosity this would provide a very high production rate, while the  
 1243 kinematics and hermetic detector systems are ideal for reconstructing the mesons we wish to study and allow us to  
 1244 exploit the EIC's discovery potential in exotic heavy flavor spectroscopy.

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## V. SCIENCE HIGHLIGHTS OF LIGHT AND HEAVY NUCLEI

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### A. Introduction

1247 Lepton-induced high-energy scattering with nuclei will be measured at fixed target facilities such as Jefferson Lab  
 1248 12 GeV. These facilities have a rich experimental program that will yield interesting results for years to come. To  
 1249 complement these programs, the EIC will be the first high-energy facility that has the ability to collide electrons and  
 1250 nuclei, which means it comes with unique capabilities:

- 1251 • The EIC has a wide kinematic range in  $Q^2$  and Bjorken  $x$ , enabling high-energy nuclear measurements in  
 1252 unexplored kinematics.
- 1253 • The EIC can have beams of polarized light ions ( $^3\text{He}$ , deuteron, etc. [334]), enabling studies of the polarized  
 1254 nuclear (neutron) structure, the polarized EMC effect, and nuclear spin-orbit phenomena. The deuteron, being  
 1255 spin-1, offers possibilities of spin studies beyond that of the nucleon.
- 1256 • Measurements on nuclei inherently have to deal with nuclear effects such as the Fermi motion, nuclear binding  
 1257 and correlation effects, and possible non-nucleonic components of the nuclear wave function [335]. In inclusive  
 1258 measurements these nuclear effects form one of the dominant sources of systematic uncertainties. With its  
 1259 extensive far-forward detection apparatus in both interactions regions, detecting particles originating from the  
 1260 breakup of the nuclear target (nuclear target fragmentation region) is possible and can help to eliminate or

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control these nuclear effects. (See Fig. 25 for a schematic diagram.) As a consequence, these more exclusive measurements will push the capabilities of the EIC as a precision machine for high-energy nuclear physics.

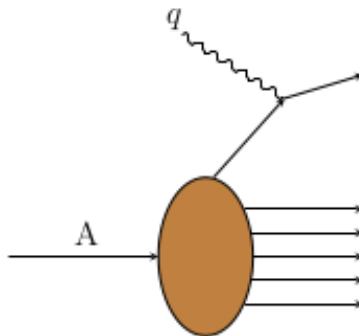


FIG. 25. Schematic diagram of a nuclear breakup process. The virtual photon  $q$  interacts with a constituent of the nucleus  $A$  and particles originating from the breakup of the nucleus can be detected in the far forward region of the EIC detector.

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Measuring nuclear breakup reactions at the EIC has several advantages. In collider kinematics nuclear fragments are still moving forward with a certain fraction of the initial beam momentum and in non-coherent scattering they have a different rigidity from the beam particles. This makes their detection more straightforward than in fixed target experiments where they typically have low momenta in the laboratory frame (10s of MeV/ $c$ ). The detection of these fragments enables additional control over the initial nuclear state in the high-energy scattering event. It can be used to probe effective targets, for instance, free neutron structure in tagged spectator DIS [336, 337], and pion and kaon structure in the Sullivan process [86]. Nuclear breakup measurements also determine which nuclear configurations (densities, virtualities, initial nucleon momentum) play a role in the process, important for instance in a multivariate disentanglement of nuclear medium modification effects such as the EMC effect. A special case of detecting fragments is coherent nuclear scattering in hard exclusive reactions, where the initial nucleus receives a momentum kick but stays intact (no breakup). Measurements of these coherent reactions allow us to perform tomography of light nuclei in quark and gluon degrees of freedom as for the nucleon (Sec. I) and to study coherent nuclear effects in these systems.

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For all these reactions, having high event rates is of high importance (multidimensional cross sections measured with sufficient precision, probing rare nuclear configurations). To obtain these high event rates one needs both high luminosity for a wide kinematic range and high acceptance for the detection of final-state particles. In both interaction regions, the EIC will have a dedicated set of far-forward detectors that enable the detection of nuclear fragments with high acceptance. Due to the intricate engineering challenges (magnets, beam pipe, crossing angle of the beam), each interaction region will have some holes in the acceptance. Having these holes in different regions of the kinematic phase space would enforce the complementarity between the two interaction regions. Having a secondary focus would also increase acceptance of detected fragments down to lower  $p_T$  values. This is especially important for coherent scattering of light nuclei, where the  $p_T$  values are much lower than for the free proton. (see Section VII.)

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In the remainder of the section we offer a brief overview of nuclear reactions that can be studied at the EIC and the physics motivation behind them. These can all benefit from the complementarity offered by having a second IR. We discuss these according to the nature of the measurements, starting with inclusive measurement, then semi-inclusive and tagged reactions, and we conclude with a discussion on exclusive nuclear channels and charm-flavored hypernuclei.

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## B. Inclusive measurements

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EIC can measure inclusive DIS on a wide range of nuclei, from the lightest to heaviest nuclei, and in a wide range of Bjorken  $x$  and  $Q^2$ . This can shed light on the dynamics of nuclear modifications of partonic distributions functions: shadowing and anti-shadowing at low values of  $x$  and the so-called EMC effect at high  $x$ . These high- $x$  measurements benefit from lower center of mass energies and, with the  $Q^2$  range that can be explored at the EIC, the  $Q^2$  dependence of the EMC effect could be further explored. This would enable the disentanglement of leading and higher-twist effects in the medium modifications. QCD evolution applied to the wide  $Q^2$ -range offers a way of getting access to the gluon EMC effect at high  $x$ . In addition, for polarized light nuclei the polarized EMC effect [338] could be further explored, which is so far an unknown quantity that will be explored in an upcoming JLab experiment [339].

### C. Semi-inclusive and tagged spectator measurements

The use of semi-inclusive reactions on nuclei for nuclear TMD studies was highlighted earlier in Section III C 5. Here, we focus on so-called tagged spectator measurements, where one or more nuclear fragments from the nuclear breakup are detected. This helps, as previously outlined, to control the nuclear configurations playing a role in the hard scattering processes. One example is the use of deuteron or  $^3\text{He}$  as effective neutron targets by tagging one (resp. two) spectator protons [336, 337, 340–345]. These neutron data are an essential ingredient in the quark flavor separation of the partonic distribution functions. In the tagged spectator reactions, an effective free neutron target can be probed by performing a so-called on-shell extrapolation of the measured cross sections or asymmetries [337, 345]. The presence of polarized light ion beams enables the extraction of polarized neutron structure in this manner [340–342, 344].

Measuring tagged spectator reactions at larger nucleon momenta (several 100 MeV relative to the ion rest frame) is of interest to several outstanding questions in nuclear physics and how these are interconnected. What is the QCD nature of the short-range, hard core part of the nucleon-nucleon force [346–348]? How do nuclear medium modifications of partonic properties manifest themselves and what nuclear configurations play a role in these [349]? In these kinematics, however, the influence of final-state interactions between products of the hard scattering and the spectator(s) and between the spectators has to be accounted for [350, 351] in order to disentangle them from the QCD phenomenon of interest. These final-state interactions are moreover little explored in high-energy scattering and are an interesting topic that can teach us about the space-time evolution of hadronization dynamics.

While technically not a nuclear process, the Sullivan process  $e + p \rightarrow e' + X + (N \text{ or } Y)$  share characteristics with the previously discussed processes. The physics interest of the Sullivan process lies in the extraction of pion and kaon structure [86, 352]. The pion being the pseudo-Goldstone boson of dynamical chiral symmetry breaking, this can shed light on the mechanism of emergent hadronic mass (EHM) within QCD. For the kaon, the presence of the heavier strange quark opens up the study of the interplay between EHM and the Higgs mechanism. In the Sullivan process, a nucleon or hyperon is tagged in the far-forward region at low four momentum transfer squared  $-t$ . In this manner, the process is dominated by meson exchange in the  $t$ -channel and, by extrapolating the observables to the on-shell pole of the exchanged meson, one can extract pion (nucleon tagging) or kaon (hyperon tagging) structure. Compared with the earlier HERA extractions, the high luminosity and wide kinematic range of the EIC would result in an order of magnitude decrease of statistical errors on the extracted pion pdfs. These measurements require high luminosity ( $> 10^{33} \text{ cm}^{-2} \text{ sec}^{-1}$ ) in order to compensate for the few times  $10^{-3}$  fraction of the proton wave function related to the pion (kaon) pole. Additionally, for kaon structure lower center of mass energies are preferable so that sufficient  $\Lambda$  decays happen in the far forward region, see Sec. VII.

Nuclear properties beyond that of the mean-field shell model can be studied using  $A(e, e' NN)$  two-nucleon knockout reactions. These can especially shed light on the nature of the nuclear short-range correlations (SRCs) and their potential relation to nucleon medium modifications [349]. The EIC will enable measurements of these processes up to  $Q^2$  values a factor of 3-4 higher than has been achieved so far in fixed target setups [353]. In these two-nucleon knockout reactions in selected kinematics, one *leading* nucleon originates from the interaction with the photon, while the other is the *recoil* partner that originated from the SRC-pair. As with the previous discussed processes, the detection of recoil nucleons happens in the far forward detector apparatus, due to the boost in the collider lab frame relative to the ion rest frame. Additionally, detection of nuclear fragments ( $A - 2$ ), and/or veto its breakup, could be possible improving control over the reaction mechanism in these reactions [354].

Measurements of single-nucleon knockout reactions in mean-field kinematics are possible at EIC up to  $Q^2 \approx 20 \text{ GeV}^2$  [353]. These would help to constrain the onset of the nuclear color transparency phenomenon [355], which has not been observed for proton knockout up to  $Q^2 = 14 \text{ GeV}^2$  [356]. Color transparency could also be explored in other kinematics and reaction mechanisms. One example that was recently explored is meson electroproduction on nuclei in backward kinematics [357], see also Sec. ID.

Concerning the detection capabilities of the EIC for these 2N knockout reactions, for the leading nucleon the detection region depends on the ion beam energy. With 41 GeV/A beams, the majority of the leading nucleons is detected in the central detector, while for 110 GeV/A it is detected in the far-forward region, see Fig. 3 of Ref. [353]. Moreover, at 110 GeV/A higher acceptance for recoil nucleons is also achieved. For leading neutrons, however, with 110 GeV the neutrons are outside the angular coverage of the ZDC, and these channels have to be measured at the lower ion beam energy.

### D. Exclusive measurements

Hard exclusive reactions on light nuclei can be measured in both the coherent and incoherent (nuclear breakup) channels [358]. The coherent channel, similarly to the case of the nucleon discussed in Secs. I and II, would give access to 3D tomography of light nuclei in quark and gluon degrees of freedom and the extraction of mechanical

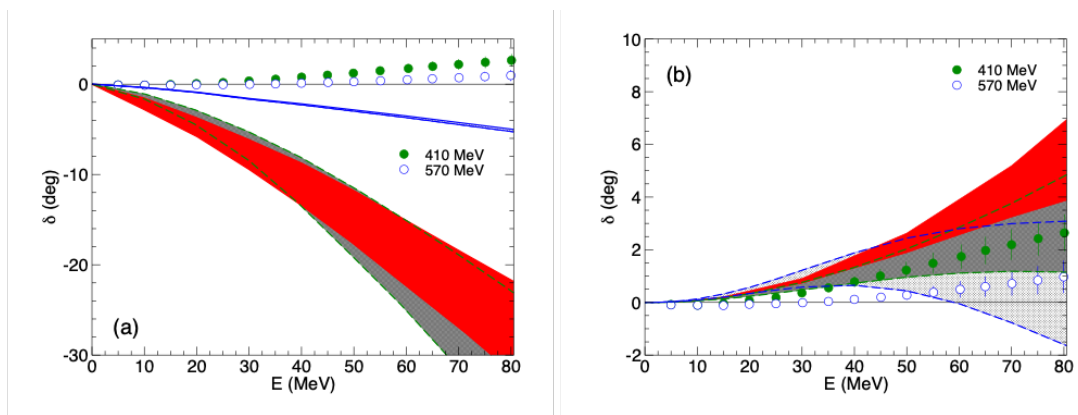


FIG. 26. Predictions for the  $\Lambda_c N \ ^3D_1$  phase shift. (a) Results from covariant  $\chi$ EFT taken from Ref. [373]. (b) Results based on the  $\Lambda_c N$  potential from Ref. [374]. Red (black), green (dark grey), and blue (light grey) bands correspond to  $m_\pi = 138$ , 410, and 570 MeV, respectively. The width of the bands represent cutoff variations/uncertainties. Lattice results of the HAL QCD Collaboration corresponding to  $m_\pi = 410$  MeV (filled circles) and 570 MeV (open circles) are taken from Ref. [375]. The figure is from Ref. [372].

1351 properties of light nuclei. It could also potentially shed light on the size of non-nucleonic components of the nuclear  
 1352 wave function. The incoherent channel, on the other hand, can be used to study medium modifications of nucleon  
 1353 tomography [359, 360] and to probe neutron 3D structure [361]. Three of the lightest nuclei (d,  $^3\text{He}$ ,  $^4\text{He}$ ) have the  
 1354 interesting feature that they have different spin and binding energies [362–366].  $^4\text{He}$  being spin-0 has the advantage  
 1355 that it has only one leading twist GPD in the chiral even sector.  $^3\text{He}$  is a spin-1/2 nucleus, meaning that hard  
 1356 exclusive observables can be similarly defined to those of the free nucleon. Lastly, the spin-1 deuteron has a richer  
 1357 structure of GPDs beyond that of the nucleon (associated with its tensor polarization modes), meaning that new  
 1358 spin-orbit phenomena can be studied. In terms of binding energy, the deuteron is very loosely bound, while  $^4\text{He}$  is  
 1359 very tightly bound and  $^3\text{He}$  falling somewhat in between. This gives us access to different degrees of nuclear effects  
 1360 that can be studied in these systems. Additionally, the availability of high-precision *ab initio* nuclear wave functions  
 1361 for these light nuclei results in a high degree of theoretical control in calculations. The challenges of detecting these  
 1362 exclusive reactions are covered in more detail in Sec. VII. There, the influence of a secondary focus on the lower limit  
 1363 of the measurable  $t$ -range for the exclusive channel especially deserves highlighting.

### 1364 E. Charm-flavored hypernuclei

1365 Hypernuclear physics has been one of the crucial tools for studying the interactions between nucleons and strange  
 1366 hyperons. Most experimental studies on hypernuclei have been focused on  $\Lambda$  hypernuclei and many precise mea-  
 1367 surements have been performed as reviewed in Ref. [367]. Recently, these efforts are extended to hypernuclei with  
 1368 multi-strangeness such as  $\Xi$  hypernuclei.

1369 Recently, there have been interests in charm hypernuclei of which the existence was predicted almost 45 years  
 1370 ago [368, 369] right after the discovery of the charm quark. As the strange hypernuclei structure heavily depends on  
 1371 the  $\Lambda$ -nucleon interactions, the stability of charm hypernuclei depends on the  $\Lambda_c$ -nucleon interactions. Following the  
 1372 seminal works of 1980s, there have been many theoretical model calculations on various states of  $\Lambda_c$  hypernuclei. The  
 1373 calculated spectra of charm hypernuclei are found to be sensitive to the  $\Lambda_c$ -nucleon interactions. (See, for example,  
 1374 Refs. [370, 371] for a review.) As there is no empirical information on the  $\Lambda_c N$  interactions, various ideas were adopted  
 1375 for modeling the potential between  $\Lambda_c$  and the nucleon. In recent calculations, lattice simulation results were used  
 1376 to model this potential. However, depending on the approach to the physics point from the unphysical quark masses  
 1377 used in lattice calculations, the extrapolated potentials lead to very different results for the  $\Lambda N$  interactions [372].  
 1378 Figure 26 shows different predictions for the  $\Lambda_c N \ ^3D_1$  phase shift extrapolated from the same lattice calculations but  
 1379 with different extrapolation methods. It shows that the results are completely different depending on the extrapolation  
 1380 approaches. Therefore, experimental measurements on charm hypernuclei are strongly required to shed light on our  
 1381 understanding of the  $\Lambda_c N$  interactions.

1382 Experimentally, earlier efforts to find charm hypernuclei started right after the seminal work of Ref. [368] and  
 1383 a few positive report on the existence of charm hypernuclei (called supernuclei at that time) were claimed [376].  
 1384 However, no serious follow-up research was reported and, in practice, there is no experimental information on charm

1385 hypernuclei. The experimental investigations in this topic would be possible at future hadron beam facilities [377].  
 1386 The experimental instrumentation of the EIC allows for precise measurements and would offer a chance to study  
 1387 charm hypernuclei. So far  $\Lambda$  hypernuclei have been studied extensively with high intensity meson beams as well as  
 1388 electron beams. Electro-production of Lambda hypernuclei was studied with the  $^AZ(e, e'K^+)_{\Lambda}^A(Z-1)$  reaction and  
 1389 similar reaction,  $^AZ(e, e'D^-)_{\Lambda_c^+}^AZ$  will produce charm hypernuclei by converting a neutron to  $\Lambda_c^+$  and  $D^-$ . Through  
 1390 observation of produced  $D^-$  and scattered electron, the missing mass technique can be applied to the spectroscopic  
 1391 study of charm hypernuclei. Therefore, studying charm hypernuclei with electron-ion collider would open a new way  
 1392 to study heavy-flavored nuclei with the future hadron beam facilities. This investigation can also be extended to  
 1393 the bottom sector [378], which is simpler than the charm sector as there is no Coulomb interaction between  $\Lambda_b$  and  
 1394 nucleons. Therefore, comparing the properties of bottom hypernuclei and strange hypernuclei would give a clear  
 1395 clue on the mass dependence of the strong interactions. The designed energy range of EIC would allow further  
 1396 investigations.

## 1397 VI. PRECISION STUDIES OF LATTICE QCD IN THE EIC ERA

1398 Lattice QCD enables the first-principles solution of QCD in the strong-coupling regime, and thereby facilitates  
 1399 calculations that can both guide the analysis of key physics quantities to be determined at the EIC, and provide  
 1400 complementary calculations that can further the physics potential of the EIC. The calculation of the internal structure  
 1401 of the nucleon, pion and other hadrons in terms of the fundamental quarks and gluons of QCD has been a key effort  
 1402 of lattice calculations since the inception of lattice QCD. Notably, there have been the first-principles calculation  
 1403 of the electromagnetic form factors, and of the low moments of the unpolarized and polarized parton distribution  
 1404 functions and of the generalized form factors. Similarly, the low-lying spectrum of QCD has been a benchmark  
 1405 calculation that now including the electroweak splittings. Nevertheless, the formulation of lattice QCD in Euclidean  
 1406 space imposes important restrictions. Firstly, time-dependent quantities, and in particular those related to matrix  
 1407 elements of operators separated along the light cone, could not be calculated, thereby precluding the computation  
 1408 of quantities, such as the  $x$ -dependent parton distribution functions. Further, scattering amplitudes, and thereby  
 1409 information about resonances in QCD, eluded direct computation. In both the fields of three-dimensional imaging  
 1410 and spectroscopy key theoretical advances have circumvented these restrictions and transformed our ability to address  
 1411 key questions of QCD in the strong-coupling regime.

### 1412 A. Three-dimensional Imaging of the Nucleon

1413 The electromagnetic form factors, and the generalized form factors corresponding to the moments with respect to  $x$   
 1414 of the GPDs, can be expressed as the matrix elements of time-independent, local operators amenable to computation  
 1415 in lattice QCD on a Euclidean grid. In particular, there has been a progression of calculations of the lowest moments  
 1416 of the isovector generalized form factors [110, 379, 380] that have already provided important insight into three-  
 1417 dimensional imaging of the nucleon, notably in discerning the role of orbital angular momentum.

1418 The realization that  $x$ -dependent distributions including the one-dimensional parton distribution functions and  
 1419 the quark distribution amplitudes, and the three-dimensional GPDs could be computed from the matrix elements  
 1420 of operators at Euclidean separations, with its genesis in Large-Momentum Effective Theory (LaMET) [381], or  
 1421 quasi-PDF approach, has spurred a renewal in the first-principles calculation of hadronic and nuclear structure. For  
 1422 the isovector distributions, the basic matrix elements are those of spatially separated quark and anti-quark fields,  
 1423 joined by a Wilson line so as to ensure gauge invariance; an alternative approach to relating the resulting lattice  
 1424 matrix elements to the familiar PDFs is the pseudo-PDF framework [382]. While both the quasi- and pseudo-PDFs  
 1425 methods share the same matrix elements, the former matches the lattice data to the light-cone PDFs using a large  
 1426 momentum expansion, while the latter is based on a short distance expansion. A further framework that encompasses  
 1427 both the quasi-PDF and pseudo-PDF approaches is that of the so-called ‘‘Good Lattice Cross Sections’’ method that  
 1428 admits spatially separated gauge-invariant operators thereby simplifying the lattice renormalization at the expense of  
 1429 computational cost [383]. Characteristic of any of these approaches is the need to attain high spatial momentum on  
 1430 the lattice in order to obtain a controlled description of the  $x$ -dependent PDF. For the most easily accessible isovector  
 1431 nucleon PDFs, there are now several calculations at the physical light- and strange-quark masses. Recent reviews can  
 1432 be found in Refs. [49, 50, 384–390].

1433 Each of the approaches introduced above admits the calculation of the GPDs, and both the incoming and outgoing  
 1434 hadrons now have to be boosted to high but distinct spatial momenta to introduce a non-zero momentum transfer  
 1435  $-t$ .



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## 1. Parton distribution functions

1437 The direct calculation of distribution functions is not possible in lattice QCD as the latter is formulated with a  
 1438 Euclidean metric, while the former have a light-cone nature. The last decade has been instrumental in attaining  
 1439 the  $x$ -dependence of PDFs through a number of approaches, such as the hadronic tensor [391], auxiliary quark  
 1440 field [392, 393], the quasi-PDFs [381], pseudo-PDFs [394], current-current correlators [383], and with an OPE [395].  
 1441 The most intensively-studied methods are the quasi- and pseudo-PDFs, which rely on calculation of matrix elements  
 1442 of non-local operators that are coupled to hadronic states that carry non-zero momentum. The non-local operators  
 1443 contain a straight Wilson line with a varying length in the same spatial direction as the momentum boost. Naturally,  
 1444 the corresponding matrix elements are defined in coordinate space, and can be transformed to the desired momentum  
 1445 space,  $x$ , with a Fourier transform. A factorization process relates the quasi and pseudo distributions to the light-  
 1446 cone PDFs, with the matching kernel calculated in perturbation theory. Both methods have been used for lattice  
 1447 calculations using ensembles of gauge configurations at physical quark masses [396–404]. Such studies correspond to  
 1448 different lattice discretizations (actions) and parameters and a comparison may reveal systematic effects related to  
 1449 the employed methodology, discretization and volume effects.

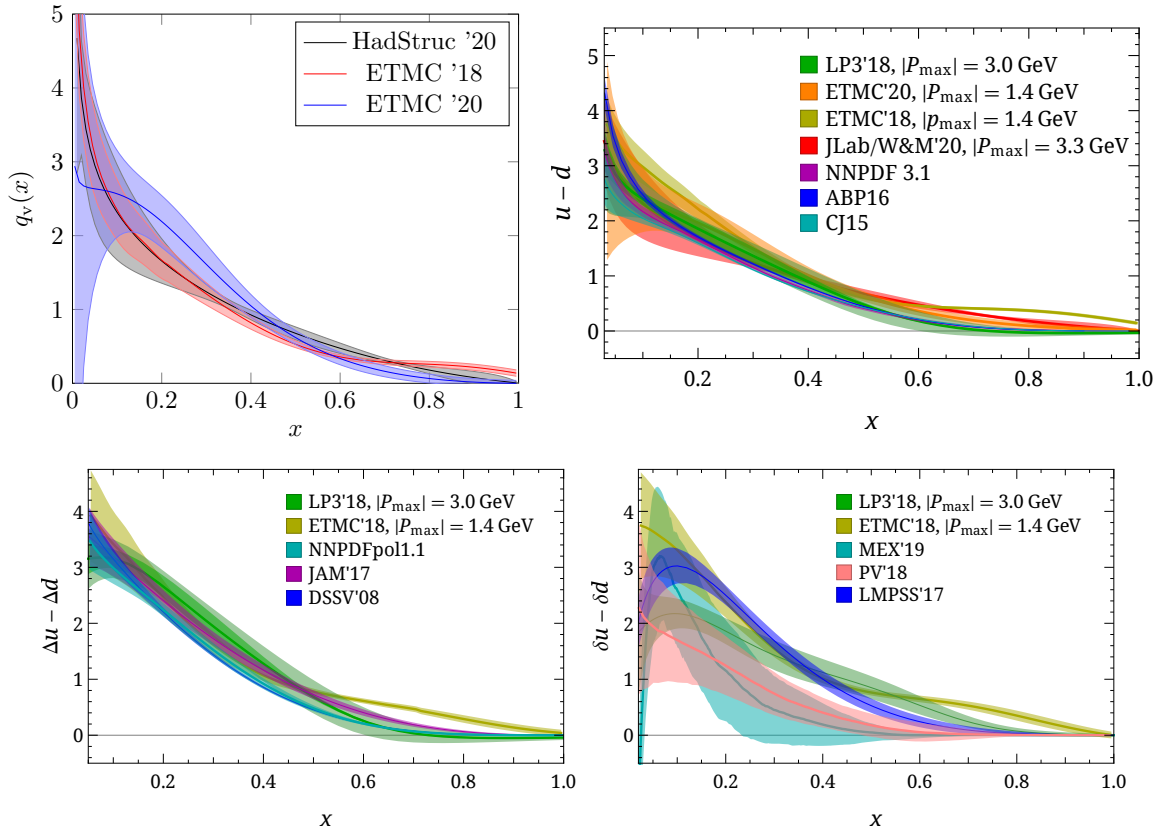


FIG. 27. Upper left: A selection of lattice-QCD results on the unpolarized PDF using the quasi-PDFs method [405] (red band) and pseudo-ITDs from Ref. [402] (gray band) and Ref. [403] (blue band). A comparison of unpolarized isovector nucleon PDFs from lattice QCD (upper right), helicity (lower left) and transversity (lower right) at or near the physical pion mass [397–403, 405] with global fits. Plots taken from Ref. [390]. All results are given in the  $\overline{\text{MS}}$  scheme at a renormalization scale of 2 GeV.

1450 In Fig. 27 we show results for the unpolarized isovector valence PDF for the proton. The results indicated by  
 1451 HadStruc'20 [402] and ETMC '20 [403] have been obtained using the pseudo-PDFs method, while ETMC'18 [397]  
 1452 uses the quasi-PDFs approach. The results are very encouraging, exhibiting agreement for a wide range of values for  
 1453  $x$ . The small tension at large  $x$  is due to systematic effects such as higher-twist contamination and the ill-defined  
 1454 inverse problem in the reconstruction of the  $x$  dependence of the PDFs. In fact, Refs. [397, 403] analyze the same  
 1455 raw data, and they differ in the analysis (quasi-PDFs versus pseudo-PDFs). This corroborates that the large- $x$  region  
 1456 has contamination from the aforementioned systematic effects. A similar tension is also present in the comparison

of the lattice data, e.g., of Ref. [402] with the global analyses of experimental data sets shown in the right panel of Fig. 27. When predicting spin-dependent PDFs, lattice calculations may already provide comparable predictions to phenomenological global analyses. The lower panel of Fig. 27 summarizes the lattice predictions for helicity and transversity nucleon isovector PDFs at physical pion mass [397, 399–401]. The helicity lattice results are compared to two phenomenological fits, NNPDFpol1.1 [406] and JAM17 [407], exhibiting nice agreement. The lattice results for the transversity PDFs have better nominal precision than the global analyses by PV18 and LMPSS17 [408]. The success in extracting the  $x$  dependence of PDFs is a significant achievement for lattice QCD, and has the potential to help constrain PDFs in kinematic regions where experimental data are not available. The synergy of lattice QCD results and global analysis is currently under study and some results can be found in Refs. [409–411].

## 2. Generalized parton distributions

Information on GPDs from lattice QCD is mostly extracted from their Mellin moments, that is the form factors (FFs) and generalized form factors (GFFs). This line of research has been very successful within lattice QCD, and several results for the form factors using ensembles with physical quark masses appeared in the last five years. Furthermore, the flavor decomposition for both the vector and axial form has been performed, giving the individual up, down, strange and charm contributions to these quantities [412–417]. A summary of state-of-the-art calculations can be found in Ref. [50]. In the left panel of Fig. 28 we show results on the axial form factor at physical quark masses from various lattice groups employing different lattice discretization and analysis methods. Its forward limit is the axial charge,  $g_A \equiv G_A(0)$ , which is a benchmark quantity for lattice QCD, and is related to the intrinsic spin carried by the quarks in the proton. As can be seen, the results are in very good agreement, despite the fact that not all sources of systematic uncertainties have been fully quantified. The level of agreement indicates that remaining systematic effects are small. Further,  $g_A$  is found to be in agreement with the world average of experimental data [418]. This is a breakthrough for lattice QCD calculations, as they demonstrate that agreement with experiment is achieved once systematic uncertainties are eliminated.

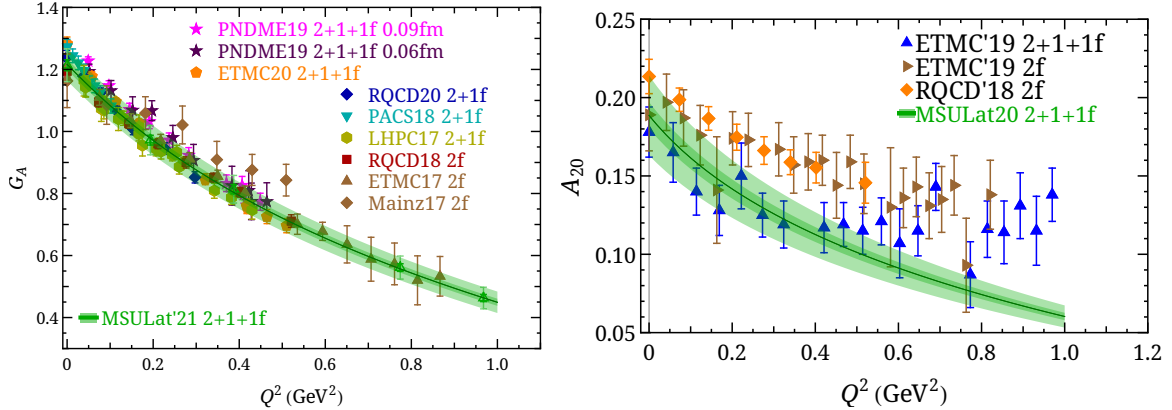


FIG. 28. Summary of lattice calculations of  $G_A(-t)$  (left) and  $A_{20}(-t)$  (right) using ensembles at or near physical quark masses. The label of  $G_A$  results correspond to: ETMC '20 [419], RQCD '20 [420], PNDME '19 [421], PACS '18 [422], RQCD '18 [423], ETMC '17 [424], LHPC '17 [425] and MSULat'21 [426]. The corresponding results for  $A_{20}$  are: ETMC '19 [427]<sup>a</sup>, RQCD '18 [428], and MSULat'20 [429].

<sup>a</sup> Larger-volume results are plotted for the ETMC'19 2f calculation.

More recently, lattice results on the GFFs associated with the sub-leading Mellin moments of GPDs (one-derivative operators) became available at the physical pion mass. In the right panel of Fig. 28 we show results on  $A_{20}$ , which appears in the decomposition of the energy momentum tensor. Its forward limit is the quark momentum fraction,  $\langle x \rangle \equiv A_{20}$ , which enters the spin decomposition [13]. Extracting GFFs is more challenging for a number of reasons. First, the introduction of covariant derivatives increases the gauge noise, as well as the uncertainties due to cutoff effects. Second, in general the number of GFFs increases, requiring independent matrix elements to disentangle the GFFs. Third, beyond the NNNLO Mellin moments, there is unavoidable mixing under renormalization. The introduction of matrix elements with greater than three covariant derivatives introduces power-divergent mixing with matrix elements with few derivatives, thereby precluding the calculation of the higher Mellin moments. Consequently, there are limitations in mapping the three-dimensional structure of the nucleon from the FFs and GFFs.

1492 Methods such as large momentum factorization (quasi-distributions) and short distance factorization (pseudo-  
1493 distributions) are very promising in extracting the  $x$ -dependence of GPDs [430–433] avoiding the challenges associated  
1494 with renormalization that are present in the calculation of GFFs mentioned above. However, the calculations are very  
1495 taxing because, unlike FFs and GFFs, GPDs are frame dependent objects and are defined in a symmetric (Breit)  
1496 frame. This increases significantly the computational cost, as a separate calculation is needed for each value of  $t$ . The  
1497  $x$ -dependence of nucleon GPDs has already been explored, in the Breit frame, for the unpolarized ( $H$ ,  $E$ ), helicity  
1498 ( $\tilde{H}$ ,  $\tilde{E}$ ) and transversity ( $H_T$ ,  $E_T$ ,  $\tilde{H}_T$ ,  $\tilde{E}_T$ ) GPDs [434, 435]. Such calculations are very timely, since the EIC will  
1499 measure the DVCS process with polarized electrons and longitudinal and transverse polarized protons to extract  
1500 the CFFs of  $H$ ,  $E$  and  $\tilde{H}$ . It should be noted that, to date, lattice calculations of GPDs are exploratory and are  
1501 available for only a few values of  $t$  for zero and nonzero skewness,  $\xi$ . Nevertheless, lattice results are useful for a  
1502 qualitative understanding of GPDs. For instance, one can find characteristics for the  $t$  dependence for each operator  
1503 under study. For instance, the lattice results of Fig. 29 indicate that the decay of the GPD with  $t$  is fastest in  $H$ ,  
1504 followed by  $H_T$ , and then  $\tilde{H}$ . Also, one can compare the hierarchy of GPDs at each value of  $t$ . On this aspect, it is  
1505 found that at  $t = 0$ ,  $f_1 \equiv H(t = 0)$  is dominant, followed by  $h_1 \equiv H_T(t = 0)$  and  $g_1 \equiv \tilde{H}(t = 0)$ . As  $-t$  increases,  
1506  $H$  remains dominant, while the hierarchy of  $H_T$ , and then  $\tilde{H}$  interchanges. Finally, lattice results can be used to  
1507 check sum rules. For more details we refer the reader to Refs. [435, 436]. We emphasize that lattice calculations on  
1508 GPDs are at the proof-of-concept stage, but results are promising. Once the lattice data can access a wide range  
1509 of  $t$ , their  $t$ -dependence can be parameterized. This is very useful because the parameterizations can be used to  
1510 extract the GPDs in the impact-parameter space as done in Refs. [426, 429] at physical pion mass. The green bands  
1511 in Fig. 28 show the moments of lattice  $x$ -dependent GPD results at zero skewness; they are in nice agreement with  
1512 the traditional local-operator methods, which shows there will be a promising future for lattice QCD contributions  
1513 in GPD tomography. Figure 30 shows the first LQCD results of impact-parameter-dependent 2D distributions at  
1514  $x = 0.3, 0.5$  and  $0.7$  [429]. Similar tomography results for helicity GPD,  $\tilde{H}(x, \xi = 0, Q^2)$  can be found in Ref. [426].

1515 The progress in the field of  $x$ -dependent GPDs from lattice QCD is being also extended to twist-3 GPDs [437]. We  
1516 anticipate that, in the near future, lattice results will be incorporated in phenomenological analysis of GPDs at both  
1517 the twist-2 and twist-3 level. Lattice-computed twist-3 GPDs can have advantages with regards to extracting twist-2  
1518 GPDs at kinematics where twist-3 contributions aren't negligible. In fact, this may even be a required step before  
1519 one attempts to extract twist-2 GPDs from DVEP data.

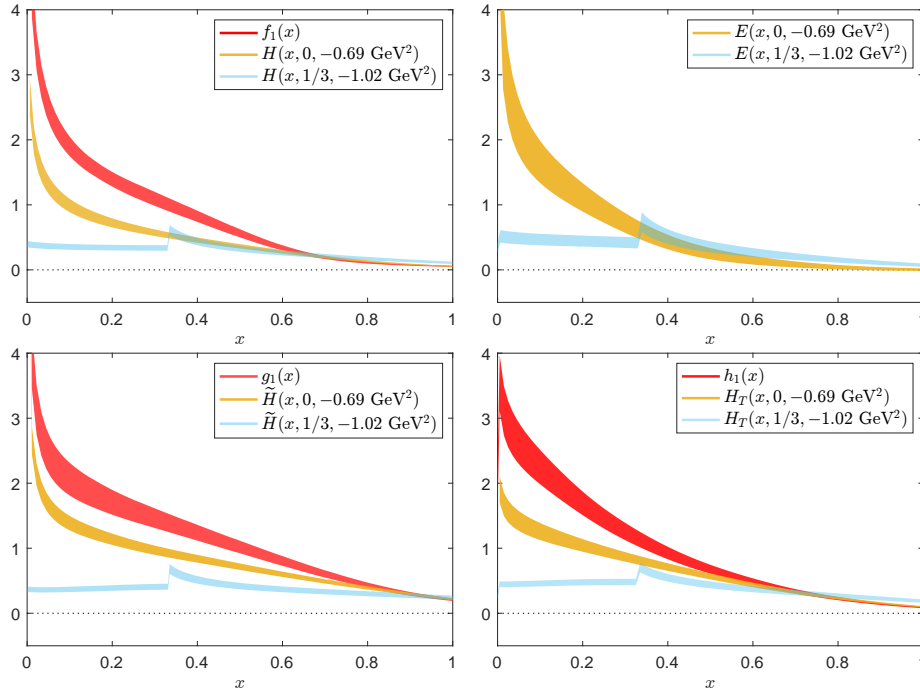


FIG. 29. The non-polarized  $H$  and  $E$ , helicity  $\tilde{H}$  and transversity  $H_T$  GPDs at  $\{t, |\xi|\} = \{0, 0\}, \{-0.69 \text{ GeV}^2, 0\}, \{-1.02 \text{ GeV}^2, 1/3\}$  extracted from the 260-MeV pion mass lattice calculations of Ref. [434, 435].

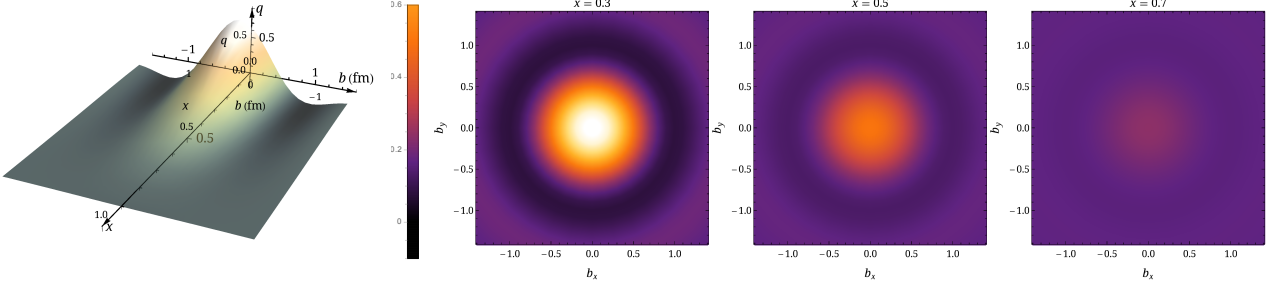


FIG. 30. (left) Nucleon tomography: three-dimensional impact parameter-dependent parton distribution as a function of  $x$  and  $b$  using lattice  $H$  at physical pion mass. (right) Two-dimensional impact-parameter-dependent isovector nucleon GPDs for  $x = 0.3, 0.5$  and  $0.7$  from the lattice at physical pion mass. Source: Ref. [429].

1520

### 3. Transverse momentum dependent distributions

1521 In contrast to GPDs, TMDs describe the three-dimensional structure in terms of the longitudinal momentum-  
 1522 fraction  $x$ , and the transverse momentum of the partons. One of the additional challenges that arise in TMD  
 1523 calculations is the presence of the rapidity divergences that need an additional regulator. Such divergences can be  
 1524 factorized into the so-called soft function, which can be separated into a rapidity-independent and a rapidity-dependent  
 1525 part. The latter defines the Collins-Soper (CS) kernel, which depicts the rapidity evolution. One of the challenges is  
 1526 that the soft function is non-perturbative for small transverse momenta.

1527 The TMDs involve the matrix elements of staple-like Wilson lines that extend along the light cone, imposing  
 1528 analogous restrictions on their calculation within lattice QCD as encountered for the case of PDFs and GPDs described  
 1529 above. The first efforts at overcoming these restrictions employed space-like-separated staples that approached the  
 1530 light-cone as the length of the staple increased [438], in particular focusing on the time-odd Boer-Mulders and Sivers  
 1531 functions [439, 440] and their relation to the corresponding processes in Drell-Yan and SIDIS, including calculations  
 1532 for the pion [441].

1533 More recently, there has been extensive work on exploring TMDs within the quasi-PDF approach [442–444], as well  
 1534 as the soft function [445, 446]. The Collins-Soper kernel has been studied by a few collaborations [209–211, 447, 448]  
 1535 and a comparison is shown in Fig. 31. Presently, such a comparison is qualitative, as systematic uncertainties are not  
 1536 fully quantified. Nevertheless, the agreement is very good and encouraging.

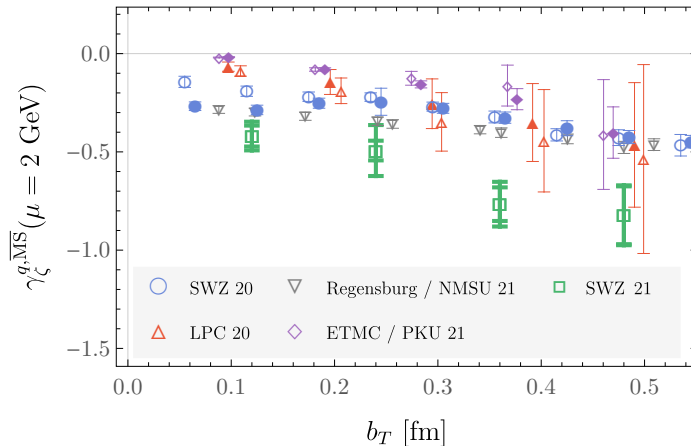


FIG. 31. The Collins-Soper kernel as a function of  $b_T$  as extracted from various lattice QCD calculations. We show results from SWZ [210, 448], LPC [209], Regensburg/NMSU [211], and ETMC/PKU [447]. Open and filled symbols of the same shape and color correspond to results from the same lattice group. Source: Ref. [448].

#### 4. Gluon and flavor-singlet structure

1537

1538 The calculation of the flavor-singlet structure of hadrons is considerably more challenging than those for the flavor-  
 1539 non-singlet quantities that have been the focus of the most precise studies. The challenges are primarily related  
 1540 to the degrading signal-to-noise ratio that impacts calculations both of the gluon distributions, and of the flavor-  
 1541 singlet quark distributions with which they mix. Recently, the first calculations of the unpolarized gluon  
 1542 distributions in the nucleon have been performed using quasi-PDF [449] and pseudo-PDF [450–452] methods, as  
 1543 well as the first lattice gluon helicity study [453]. Within the present statistical precision and through a qualitative  
 1544 comparison with global analyses of the gluon helicity distribution, the lattice calculation hinted at a positive gluon  
 1545 polarization contribution to the nucleon spin budget.

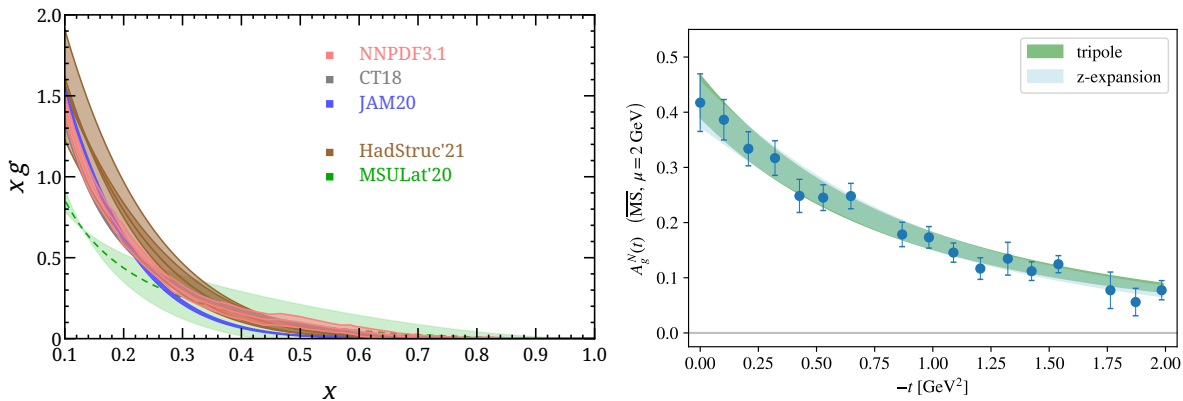


FIG. 32. Left: lattice results on the unpolarized nucleon gluon PDF using a two-parameter parametrization  $xg(x) = Nx^\alpha(1-x)^\beta$  by MSULat'20 [450] and HadStruc'21 [451]. Also shown are the unpolarized gluon PDFs extracted from global fits to experimental data: CT18 [454], NNPDF3.1 [455], and JAM20 [456]. Right: the gluon nucleon GFF in a lattice calculation corresponding to  $M_\pi = 450(5)$  MeV; the bands show a multipole fit with  $n = 3$  (green), and a model-independent  $z$  expansion (blue). Source: Ref. [457].

1546 A comparison of the calculation with phenomenological parametrizations is shown as the left-hand panel in Fig. 32.  
 1547 While this calculation is at unphysically large pion masses, with limited understanding of the systematic uncertainties,  
 1548 it demonstrates the potential of lattice QCD to complement and augment insights into hadron structure from  
 1549 experiment, notably at large  $x$ .

1550 The calculation of the gluon contributions to three-dimensional structure of hadrons proceeds as in the case of that  
 1551 of the valence quarks described above. In particular, the gluonic contribution to the GFF has been computed [111,  
 1552 457, 458] thereby enabling, when combined with the corresponding quark contributions, the pressure and shear forces  
 1553 within a nucleon to be computed, shown as the right-hand panel of Fig. 32.

1554

### B. LQCD and Spectroscopy

1555 The ability to study multi-hadron states and resonances from lattice QCD calculations was transformed by the  
 1556 realization that, for the case of two-body elastic scattering, infinite-volume, momentum-dependent phase shifts could  
 1557 be related to energy shifts at finite volume on a Euclidean lattice [459–461]. The formalism for elastic scattering has  
 1558 now been extended to coupled-channel scattering, and to multi-hadron final states facilitating a range of calculations  
 1559 that impact our understanding of the spectroscopy of QCD. Notably, there are now calculations of coupled-channel  
 1560 scattering describing the nature of the isoscalar  $a_0$ ,  $f_0$  and  $f_2$  resonances [462], and the first calculation of the decays  
 1561 of the exotic  $1^{-+}$  meson [463].

1562 Beyond the challenge of computing the spectrum of resonances and their decays, an important development has  
 1563 been that of a formalism for the photo- and electro-production of two-hadron final states, an example of the so-called  
 1564  $1 + \mathcal{J} \rightarrow 2$  processes [465, 466]. The formalism has been applied to the case of  $\pi^+\gamma \rightarrow \pi^+\pi^0$ , shown in Figure 33.  
 1565 Recently, this has been extended to the case of coupled-channel, multi-hadron final states [467] thereby providing an  
 1566 essential framework underpinning the spectroscopy opportunities through photoproduction at the EIC.

1567 The calculation of the spectrum of the exotic charmonium and bottomonium states anticipated at the EIC poses  
 1568 several additional challenges beyond those encountered in the light-quark sector. Firstly, a precise understanding  
 1569 of light- and strange-quark spectroscopy is a precursor to precision calculations in the heavy-quark sector since the

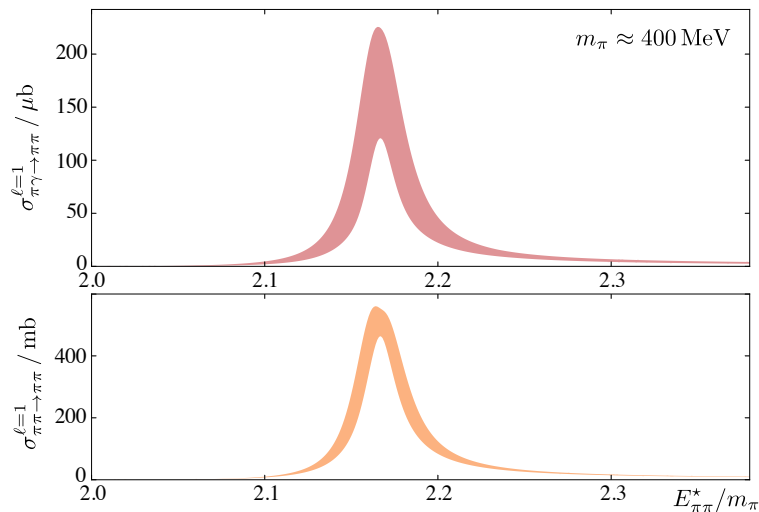


FIG. 33. The upper panel shows the  $\pi^+\gamma \rightarrow \pi^+\pi^0$  cross section as a function of the  $\pi\pi$  center-of-mass energy in a calculation with a pion mass  $m_\pi \simeq 400$  MeV. The lower panel shows the  $l = 1$  elastic  $\pi\pi$  scattering cross section, with the  $\rho$  resonance visible in both cases. Source: Ref. [464].

1570  $c\bar{c}$  can mix with such states in many of the most interesting channels. Secondly, with increasing mass of the quark  
 1571 constituents, the splitting between the different energies on the lattice is compressed, with many  $J^P$  states at similar  
 1572 energies requiring additional constraints to identify the states from the lattice data. Finally, there are the many open  
 1573 channels that must be included. The work so far is largely exploratory [468, 469], with the inclusion of only a limited  
 1574 number of coupled channels. However, controlled calculations of many of the exotic states anticipated at the EIC are  
 1575 now computationally feasible, with studies both of the  $\chi_{c1}(3872)$  and the  $X(6900)$  most easily attainable.

### 1576 C. Outlook

1577 Many of the "no-go" theorems that until recently have imposed limitations on the range of quantities accessible to  
 1578 first-principles calculation in lattice QCD have now been circumvented through a progression of theoretical advances,  
 1579 with demonstrations of the ability of lattice QCD calculations to add to our understanding of the internal structure and  
 1580 spectroscopy of hadrons. The advent of the era of exascale computing will enable the precision calculations needed to  
 1581 exploit the opportunities afforded by the EIC [385, 470]. Notably, in addition to the emerging precision computations  
 1582 of the isovector quantities, such calculations will be extended to the isoscalar sector. Precise computations within  
 1583 lattice QCD of the three-dimensional measures of hadron structure, combined with the two-dimensional Generalized  
 1584 Form Factors accessible through exclusive processes at the EIC, will constrain the model dependence in global analysis  
 1585 of experimental data, and will facilitate a more precise three-dimensional imaging of hadrons that either experiment  
 1586 or first-principles calculation can achieve alone.

1587 Despite these advances, there remain physical processes that elude current lattice QCD calculations, notably the  
 1588 direct calculation of real-time scattering cross sections, fragmentation functions, and nuclear response functions. The  
 1589 rapid advance of Quantum Information Science, and its role as a high-priority research area, will play an increasingly  
 1590 important role in addressing many of these key problems, recognised in the report of the NSAC subcommittee [471].  
 1591 Thus far, the investigation of quantum field theory on quantum computers has been restricted to far simpler systems  
 1592 than that of QCD, but the role of QIS both in advancing lattice gauge theory is reviewed in ref. [472]. Further,  
 1593 strategies for exploiting quantum computing to directly address processes relevant to the EIC, such as Compton  
 1594 Scattering, are now being formulated [473].

## VII. SCIENCE OF FAR FORWARD PARTICLE DETECTION

### A. Far-forward detection overview

In contrast to colliders that are mainly built to study particles produced at central rapidities, much of the EIC physics critically relies on excellent detection of the target and target fragments moving along, and often within, the outgoing ion beam. Consequently, EIC detectors are from the outset designed with an elaborate far-forward detection system that is closely integrated with the interaction region of the accelerator. The forward detection has several stages: the endcap of the central detector, trackers within a large-bore dipole magnet in front of the accelerator quadrupole (quad) magnets, two sets of Roman pots (one for charged particles at lower rigidities, so-called “off-momentum detectors”; the other for tagging protons or light ions near the beam momentum) after a larger dipole behind the quads as seen in Fig. 34 which shows the layout of IP6 during the time of the Yellow Report, which is largely unchanged. Additionally, a zero-degree calorimeter is employed for tagging neutrons and photons at very small ( $<5$  mrad) polar angles.

This arrangement allows for high- $p_T$  cutoffs to be determined by the magnet apertures, such as is the case for the neutron/photon cone going toward the zero-degree calorimeter (which must traverse the full hadron lattice), and for charged particles and photons being tagged in the first, large-bore dipole magnet after the IP, which contains a detector for far-forward particles at polar angles roughly between 5.5 and 20 mrad. The bore of the first dipole (called B0pf in IP6) has a radius of 20 cm (while the pre-conceptual design for IP8 has an equivalent dipole magnet with a slightly larger radius), which in principle allows for larger acceptance than 20 mrad, but support structure and services for the detectors will limit how much of the bore can be filled with active detector material. As designs progress, it may be possible to achieve a larger acceptance in the dipole spectrometer at both IP6 and IP8.

On the other hand, for lower-energy proton beams, unavoidable inefficiencies will occur in the transition regions. There is a low- $p_T$  cutoff due to the beam itself, which is most severe for the detection of recoil protons from mid- to high-energy beams (which provide the highest luminosity), for light ions at all energies, and for heavy ion fragments with  $A/Z$  close to that of the original beam. For ions, where the  $p_T$  *per nucleon* is usually small, acceptance at very low- $p_T$  is extremely important. With a traditional IR layout, low- $p_T$  acceptance can be improved by reducing the angular spread of the beam via reduced beam focusing. However, this has the drawback that it also reduces luminosity and still does not make it possible to reach  $p_T=0$ .

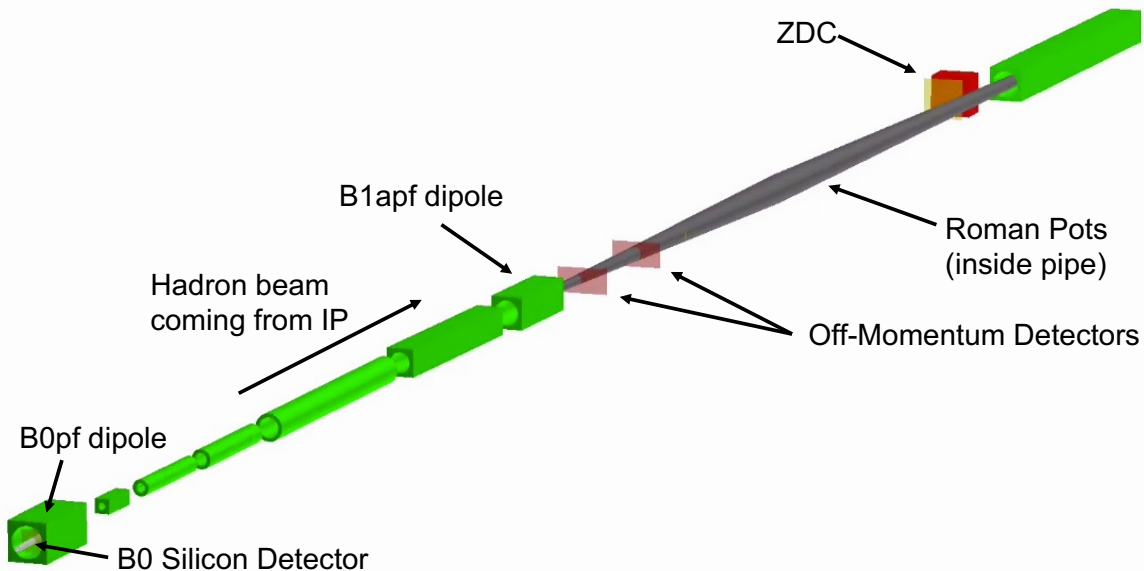


FIG. 34. Layout of the IP6 Far-Forward region generated with the EICROOT simulation package [474] including the dipole magnets (rectangular boxes), quadrupole magnets (cylinders), and the four detector subsystems currently proposed to cover the geometric acceptance.

The kinematics of the EIC are uniquely suited to a more sophisticated forward detection concept than previous colliders. In DIS, the typical longitudinal momentum loss  $dp/p \sim x$ . At the same time, the intrinsic momentum spread of the particles in the beam is a few  $\times 10^{-4}$ . With a  $10\sigma$  margin, *all* recoil protons with  $x > 0.01$  will thus

separate out from the beam even at  $p_T=0$ , and at much lower  $x$  for non-zero  $p_T$ . Since this method only relies on a fractional longitudinal momentum loss (magnetic rigidity), it is independent of the beam energy. For heavy ions, which typically only experience small changes in momentum, rigidity ( $\sim A/Z$ ) can change through emission of nucleons. In particular, emission of a single neutron from an  $A \sim 100$  nucleus corresponds to a change in rigidity at the 1% level, which in principle also allows the EIC to detect most nuclear fragments.

To take full advantage of the EIC kinematics, the forward detection requires two elements: dispersion and focusing. The former is generated by dipole magnets and translates a momentum (rigidity) change into a transverse position offset:  $dr = Ddp/p$  (e.g., with  $D = 40\text{cm}$ , the transverse displacement for a particle with  $dp/p = 0.01$  and  $p_T = 0$  will be 4 mm). This value has to be compared with the ( $10\sigma$ ) beam size at the detection point (Roman pot). Without focusing, this is typically a few cm, but with a secondary focus it can be reduced to 2-3 mm (depending on the beam momentum spread). The beam size on the Roman pot does in principle not depend on the focusing of the beam at the collision point ( $\beta^*$ ), but in a practical implementation the same magnets are used to generate both the primary and secondary focus. However, in contrast to the unfocused case, this means that with a secondary focus the best low- $p_T$  acceptance is achieved at the highest luminosity. A secondary focus could in principle be used at either IP6 or IP8 of the EIC. However, while the current IP6 layout has some dispersion (17 cm), it does not have a secondary focus. In contrast, IP8 is designed for a much larger dispersion and incorporates a secondary focus – making it complementary to IP6 and opening up unique physics capabilities, as can be seen in Fig. 35.

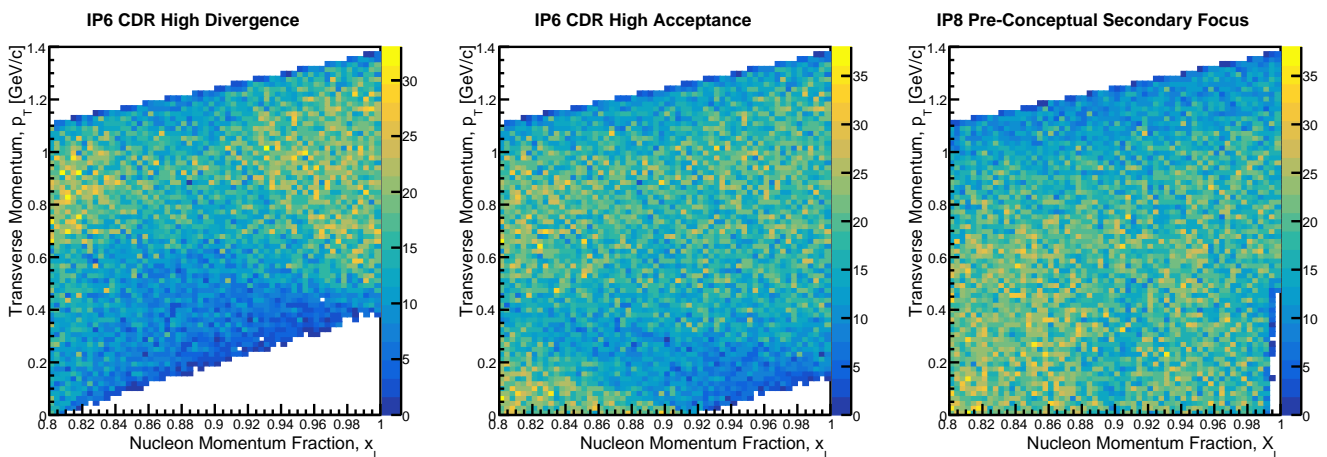


FIG. 35. Two-dimensional plots of proton acceptance in transverse momentum,  $p_T$  the nucleon momentum fraction. The acceptance is shown for three configurations: accepted protons in the IP6 Roman pots with the CDR high divergence optics (left), for accepted protons in the IP6 Roman pots with the CDR high acceptance optics (middle), and for accepted protons in the IP8 Roman pots at the secondary focus with the pre-conceptual optics configuration (right). All samples were generated for 18 GeV on 275 GeV protons with an  $x_L > 0.8$  and with  $0 < \theta < 5$  mrad; the cutoff at the top of the plots is due to the event generation region, while the acceptance in the bottom right varies with different configurations.

## B. Detection of recoil baryons and light ions

As discussed in sections 7.2.2 and 7.3.8 of the Yellow Report [8] and earlier in this paper, exclusive reactions on the proton and light nuclei form an essential part of the EIC physics program. The wide kinematic reach of the EIC makes it ideal for probing different parts of the nuclear wave function, revealing how the internal landscape of nucleons and nuclei changes with  $x$ . Measurements of exclusive processes require high luminosity, a range of collision energies, and excellent far-forward detection. Key issues are detector acceptance for the recoil proton or light ion and optimized reconstruction resolution of the momentum transfer,  $t$ .

*a. Proton detection:* Detecting the recoiling nucleons is important to cleanly establish the exclusivity of the reaction. It also makes it possible to reconstruct  $t$  directly from the proton. Since the EIC reaches its highest luminosity with the most asymmetric beam energies (i.e., 5-10 GeV electrons colliding with hadrons at maximum energy), it is essential that the far-forward detection works optimally for high-energy protons. Here, the greatest challenge is to detect low- $p_T$  protons which stay within the beam envelope. This capability can be improved by using a secondary focus, which essentially provides full acceptance for  $x > 10^{-2}$ , and significantly improves the low- $p_T$  acceptance for lower  $x$ . For lower proton beam energies, a secondary focus is still useful, although less crucial.



However, at lower energies, high- $p_T$  protons will start experiencing losses in the apertures of the accelerator quadrupole magnets, leading to a reduced acceptance for detectors downstream of these magnets. Embedding a tracking detector, such as is envisioned with the B0 tracker in IP6, provides increased coverage of high- $p_T$  protons at the lower beam energies. This issue can be alleviated by using magnet technologies that allow for higher peak fields, which makes it possible to increase the apertures, but there are other technical constraints that could make this challenging, especially at IP6, and more study is needed to determine what level of improvement is possible. In conjunction with a secondary focus, this would further enhance the capabilities of the EIC to do transverse proton imaging.

*b. Determination of transverse momentum in exclusive reactions:* Another important consideration for exclusive reactions is reconstruction of  $t$ . In principle it can be done either by using the recoiling system detected in the far-forward detectors, or from the scattered electron and produced particle (charged meson or DVCS photon) detected in the central detector. There are advantages to both methods. For example, the former method is very straightforward, but requires a good understanding of the beam effects (e.g. angular divergence). Ideally one would want to be able to apply both, but this requires that the central detector can provide a sufficiently good  $p_T$ -resolution. This is a challenge for a tracker, but even more so for the EM calorimetry if one wants to be able to determine  $t$  ( $\Delta_\perp$ ) from the DVCS photon (or the photons from  $\pi^0$  production). However, while such a dual capability is useful for protons, it becomes essential for ions, where the ability to determine  $t$  from the ion is more limited and vanishes entirely when the ion is not detected (high  $A$  and low  $p_T$ ). Being able to determine  $t$  from the DVCS photon would thus greatly enhance the ability to do transverse imaging of ions.

*c. Light ion detection:* Coherent exclusive scattering on light ions differs from protons in two ways. First, the available ion beam energies are restricted a range between 100 GeV/A and  $275 \times Z/A$  GeV/A, as well as a discrete energy at 41 GeV/A. Second, scattered ions travel much closer to the beam, making low- $p_T$  acceptance very challenging (and conversely, the high- $p_T$  acceptance much less so, even for the high- $t$  tails). This is the combined result of two effects: cross sections for ions peak at lower  $t$ , and a given  $t$  corresponds to a lower  $p_T$  per nucleon. The former means that in contrast to the proton, clean imaging of light ions *requires* an acceptance down to  $p_T \sim 0$ , and the latter that implementing such an acceptance is particularly difficult. A secondary focus is thus essential for high-quality measurements of coherent scattering on light ions. However, if the central detector has the ability to reconstruct the  $p_T$  from the produced photon or meson as discussed above, a secondary focus would allow for a hybrid method where ions with higher  $p_T$  are detected (the incoherent backgrounds become more challenging as one moves towards the first diffraction minimum), while the low- $p_T$  part is reconstructed by vetoing the breakup (which is generally easier to do with light than heavy ions). A hybrid measurement would not be as clean as one where all recoiling ions are detected, but it would make it possible to reach lower  $x$  and higher  $A$ , extending the discovery potential of the EIC.

### C. Spectator detection

Detection of nuclear breakup is essential for a broad range of EIC physics topics. From a detection perspective, these broadly fall into two categories: spectator nucleons and nuclear fragments. In the first case, the spectator nucleon typically experiences a very small change in momentum, but its magnetic rigidity ( $A/Z$ ) is very different from that of the original beam. A proton spectator will thus initially continue moving with the beam, but will separate quickly from it after passing the first dipole magnet. The detection challenge here thus lies primarily in providing adequate magnet apertures. An key example of spectator proton tagging are measurements of neutron structure in deuterium and  $^3He$ .

In the case of nuclear fragments, they may be detected as a way of vetoing breakup or part of the direct measurement. The former case was discussed above (Sec. VII B in the context of light and medium nuclei, but coherent processes on heavy ions are different in that even with a secondary focus, the high- $p_T$  tails cannot be measured directly as the ion always stays inside the beam envelope. A secondary focus can, however, make it possible to detect residual ions that have lost a single nucleon ( $A-1$  tagging). Adding such a capability will significantly improve the efficiency for vetoing the large incoherent backgrounds, making a reasonably clean measurement possible.

Finally, there are several measurements that rely on detection of the spectator nucleons, the residual nucleus, or nuclear fragments in the final state. One example is the case when the struck nucleon and its partner are in a short-range correlation with a high relative momentum. In this case, the spectator nucleon will not only have a different  $A/Z$  compared with the original ion, but also a large  $p_T$ . The breakup kinematics can then be best constrained if the residual  $A-2$  nucleus can be detected, which is facilitated by a forward spectrometer with a secondary focus. A related topic is detection of rare isotopes produced in the interaction, which is discussed in Sec. VII G. Additional detail, including discussion of the theoretical framework for several of the tagged measurements can be found in Ref. [343, 351]

*a. Neutron structure through spectator tagging* Light ion beams can be used as an effective free neutron target via spectator tagging. Deuterium is the simplest system, while  $^3He$  can be polarized (70%) and thus give access

to the neutron spin structure. Spectator tagging can be applied to any primary measurement ( $F_2$ , DVCS, etc), but a key common challenge is to account for final-state interactions (FSI). However, recent studies [345] have shown that free neutron structure can be extracted by on-shell extrapolation to the non-physical pole, where the neutron is by definition free and unaffected by FSI. In contrast to the pion, this approach is much more robust for the heavier nucleon where the extrapolation takes place over a shorter interval. The extrapolation is done by fitting the measured  $t$  distribution, but focuses on the low-to-moderate values of  $t$  part, where the extrapolation has minimal model dependence.

Experimentally, this measurement relies on a high-resolution determination of the  $p_T$  distribution, and of having sufficiently large magnet apertures to tag a spectator proton with low  $p_T$  [345]. As a cross check, it is also possible to apply the same method to the bound proton by tagging the neutron from deuterium in the ZDC.

*b. Proton and neutron spectators from deuteron beams* Deuteron beams can be used as an effective free neutron target via spectator tagging, where the undisturbed proton is measured to isolate scattering from the proton. To isolate nearly on-shell neutrons, the goal is to tag protons which had low initial momenta (corresponding to low  $-t$ ) in the deuteron rest frame. Measurements will be made over a range of  $t$ , so that the extrapolation to the on-shell neutron can be performed over different ranges of  $t$  to ensure stability of the extrapolation. As noted above, detection of these protons in the Off-Momentum Detector and Roman Pots is relatively straightforward and the key issue is minimizing the loss of acceptance in the apertures of the accelerator magnets.

Similar studies of the proton structure of the proton structure can be performed with neutron tagging used to isolate scattering from a low-momentum proton. In this case, the results can be compared to the known proton structure, and these studies can be used to study the  $t$ -dependence and test the extrapolation to the on-shell proton. For the low  $t$  values required for these measurements, the neutrons have  $x_L$  near unity and small  $P_T$  and are detected in the ZDC.

*c. Double tagging from  $^3\text{He}$  breakup* While the deuteron is the most common target used to study unpolarized neutron structure, polarized  $^3\text{He}$  serves as the most effective target for measuring neutron spin structure, as the neutron carries most of the spin in  $^3\text{He}$ . Inclusive measurements can provide some information, with the protons acting mainly as a dilution to the asymmetries associated with scattering from the polarized neutron. But double tagging of the two spectator protons in  $^3\text{He}$  can be used to isolate scattering from the neutron without dilution or corrections for the proton contributions [344]. In this case, the goal is to measure spectators with low momenta in the  $^3\text{He}$  rest frame which have momenta close to the beam momentum per nucleon and small  $P_T$ , but lower mass and therefore roughly 2/3 of the rigidity of the  $^3\text{He}$  beam. One can also examine events with one large-momentum proton to identify high-momentum neutrons in the initial state to look at the spin structure as a function of initial neutron momentum, which is relevant for understanding the spin EMC effect.

*d. Tagged Pion structure - nucleon spectators from proton beams* Measurement of the  $\pi^+$  electromagnetic form factor can be accomplished at the EIC by the detection of the neutron spectator in coincidence with the scattered electron and  $\pi^+$ , i.e. an exclusive reaction with  $e' - \pi^+ - n$  triple coincidence. The neutron is emitted with 80-98% of the proton beam momentum, and is detected in the ZDC. The pion form factor measurement only requires  $-t$  measurements up to about 0.4  $\text{GeV}^2$ , so a moderate acceptance ZDC is sufficient to catch the events of interest. Very good ZDC angular resolution is required for two reasons. First, to separate the small exclusive  $\pi^+$  cross section from dominant inclusive backgrounds, a cut may be placed on the detected neutron angle in comparison to the reconstructed neutron angle (from  $e'$  and  $\pi^+$  using momentum conservation). Second, a  $t$  reconstruction resolution better than  $\sim 0.02 \text{ GeV}^2$  is necessary for a quality form factor measurement and such resolution is only possible when reconstructed from the initial proton and final neutron momenta. The ZDC is thus of crucial importance to the feasibility of a pion form factor measurement at the EIC.

*e. Tagged Kaon structure - hyperon spectators from proton beam* Measurements of the  $K^+$  electromagnetic form factor at high  $Q^2$  via the Sullivan process would yield valuable information on nonperturbative DCSB-Higgs-boson interference effects in hard exclusive processes. The reaction of interest is  $e + p \rightarrow e' + K^+ + \Lambda$ , where the  $\Lambda$  is emitted with  $> 70\%$  of the proton beam momentum. We expect that lower beam energies are optimal, to ensure a high  $\Lambda$  decay fraction, as non-decayed  $\Lambda$  will be impossible to distinguish from neutron hits.

The  $\Lambda$  needs to be identified from its decay products to ensure the clean identification of the exclusive events from inclusive backgrounds, and to reconstruct  $t = (p_p - p_\Lambda)^2$  with sufficiently high resolution. One complication is that the  $\pi^-$  from the dominant  $\Lambda \rightarrow p\pi^-$  decay channel cannot be detected in the far forward detectors for decays occurring at or after the B0 magnet. Such measurements would require dedicated detectors for negative particles or be limited to decays occurring sufficiently before B0. The neutral  $\Lambda \rightarrow n\pi^0 \rightarrow n\gamma\gamma$  decay seems a better choice. For the measurement to be feasible, three hit events need to be reliably identified in the ZDC with sufficiently good energy and angle resolution for  $t$  reconstruction. Even more challenging is confirming that the Sullivan process dominates at low  $-t$ , which requires a measurement of the  $\Lambda/\Sigma^0$  ratio. This entails the reliable detection of four neutral hits in the ZDC, from  $\Sigma^0 \rightarrow \Lambda\gamma \rightarrow n\pi^0\gamma$ . Thus, this is a measurement that is significantly more challenging than that of the pion form factor, although if it is feasible, it would be an important addition to the EIC scientific program.

1769 The acceptance for neutral decay products could potentially be increased significantly if calorimetry were included in  
 1770 the B0 magnet. This option was mentioned as a possibility in the Yellow Report, but including both tracking and  
 1771 calorimetry is technically challenging due to spatial constraints inside the magnet and further design work is needed  
 1772 to know what is be possible.

#### 1773 D. Tagging of active nucleons - high spectator momenta

1774 While the previous sections focused on tagging of relatively low-momentum spectators, other key studies are focused  
 1775 on isolating high-momentum nucleons and/or mapping out tagged nucleon structure over a wide range of initial  
 1776 virtualities. Studies of Short-Range Correlations between pairs of bound nucleons require tagging of final state  
 1777 nucleons at both high and low values of  $p_T$  to fully exploit the measurement capability. This provides a unique  
 1778 challenge for the detector acceptances, as multiple far-forward subsystems play a role in covering the phase space.  
 1779 In general, the active nucleon in a reaction will be scattered with relatively large polar angles ( $\theta > 5$  mrad), while  
 1780 the recoil nucleons and spectator nuclear fragments (for  $A > 2$ ) are usually at smaller values. Additionally, in the  
 1781 case of the recoil protons, there is a magnetic rigidity change with respect to the ion beam which further complicates  
 1782 detection. It is in principle also possible to tag an A-2 spectator nucleus, in the final state, but this is uniquely  
 1783 challenging to do the small scattering angles for the spectator nucleus, and the small rigidity change, dependent on  
 1784 the struck SRC pair. Tagging of A-2 nuclei can be enhanced with Roman Pots at a secondary focus.

1785 In cases where both final-state nucleons from an SRC pair are measured, the spectator nucleon is detected in the  
 1786 far-forward region while the active (struck) nucleon is measured in the main or far-forward detectors. At higher  
 1787 energies, the acceptance is more complete when measuring a spectator neutron and active proton, since the polar  
 1788 angle coverage for struck protons is extended to  $\sim 20$  mrad in the B0 tracking detector, while the neutron acceptance  
 1789 is limited to  $\sim 5$  mrad by the magnet aperture. For active neutrons, the lower beam energy configurations (e.g. 5x41  
 1790 GeV/n) are more beneficial since the larger active neutron scattering angle can place them in the acceptance of the  
 1791 main detector endcap hadronic calorimeter (i.e.  $\theta > \approx 30$  mrad). Additionally, if more of the open bore space in  
 1792 the dipole spectrometer can be used for active detector material, it would further enhance the capabilities for active  
 1793 proton tagging beyond the current 20 mrad assumption.

1794 Having some capability for tagging in the higher- $p_T$  regime allows simultaneous study of both free nucleon struc-  
 1795 ture and nuclear modifications with the same experimental setup. Studies of Short-Range Correlations and nuclear  
 1796 modifications enable the EIC to provide insight into the EMC effect and other physics at higher-x.

#### 1797 E. Vetoing of breakup

1798 Separation of coherent and incoherent photoproduction of photons (Deeply Virtual Compton Scattering) and vector  
 1799 mesons is critical to many aspects of the EIC physics program. In the Good-Walker paradigm, one can relate the  
 1800 coherent cross-section to the average nuclear configuration, while the incoherent cross-section is sensitive to event-  
 1801 by-event fluctuations of the nuclear configuration, including gluonic hot-spots [475]. One can do a two-dimensional  
 1802 Fourier transform of  $d\sigma_{\text{coherent}}/dt$  to determine the transverse distribution of gluons in the nuclear target - the nuclear  
 1803 equivalent of the GPD. By studying different mesons with different masses, and using photons with different  $Q^2$ , one  
 1804 can map out nuclear shadowing as a function of position within the nucleus.

1805 The challenge in these measurements is in adequately separating coherent and incoherent production, by detecting  
 1806 the products of nuclear breakup [476]. To determine the transverse gluon distributions, it is necessary to measure  
 1807  $d\sigma_{\text{coherent}}/dt$  out to the third diffractive minimum [8], to avoid windowing artifacts in the Fourier transform. At this  
 1808 minimum, a rejection factor of 500:1 is needed to adequately remove the incoherent background.

1809 In most cases, nuclear dissociation leads to neutron (or, less frequently, proton) emission from the target. These  
 1810 are relatively straightforward to detect, although very high efficiency is required. However, some soft excitations will  
 1811 produce excited nuclear states that decay by photon emission. These photons typically have energies of a few MeV  
 1812 (or less) in the nuclear rest frame. Gold (planned as the main EIC heavy nuclear target), is particularly bad. It has a  
 1813 77 keV excited state with a 1.9 nsec lifetime. Because of the lifetime, this state is almost impossible to observe in an  
 1814 EIC detector. It's next states have energies of 269 and 279 keV respectively. The lab-frame energies depend on the  
 1815 EIC beam energies, but for 110 GeV/n gold beams, the maximum energy is 65 MeV. For photon emission away from  
 1816 the far-forward direction, the energy will be lower. This is likely beyond the reach of the planned EIC detectors, but  
 1817 could be accessible in an upgrade. Because the energy transfer to the target (and hence the energy spectrum of the  
 1818 excitations) depends on  $t$ , is it critical to be able to detect emission of protons, neutrons, and soft photons over the  
 1819 full phase space. As noted earlier, the addition of calorimetry in the B0 magnet would improve the acceptance, but  
 1820 is technically challenging.

1821 Since the knockout of a single neutron (and possibly evaporation of another) is an important contribution to the  
 1822 incoherent background, the ability to tag and veto on A-1 nuclei (*e.g.*, Zr-89 from a Zr-90 beam) is also very important  
 1823 for a clean measurement. High-resolution photon detection is also synergistic with a potential rare isotopes program  
 1824 discussed below.

1825 It is also possible to mistake coherent production for incoherent, if a second collision in the same beam crossing  
 1826 dissociates a nucleus [477]. This could affect the measurement of the incoherent cross-section at small  $|t|$ . Although  
 1827 the background rate can be subtracted, statistical uncertainties will remain. However, most of these events can be  
 1828 removed if the ZDC has very good timing.

## 1829 F. Backward (u-channel) photoproduction

1830 In backward (u-channel) photoproduction, the produced meson takes most of the energy of the incident proton,  
 1831 and so goes in the forward direction, while the proton is shifted many units of rapidity, and, at the EIC, is visible in  
 1832 the central detector [67]. Instead of having small Mandelstam  $t$ , as in conventional photoproduction,  $t$  is large (near  
 1833 the kinematic maximum) and  $u$  is small. This process may be modelled using Regge trajectories involving baryons,  
 1834 but it is not easy to see how such simple reactions can lead to nucleons being shifted many units of rapidity; there  
 1835 may be connections with baryon stopping in heavy-ion collisions. A systematic exploration of production of different  
 1836 mesons at higher energies is needed to fully characterize this reaction, and test the Regge trajectory approach.

1837 Reconstruction of these events requires a forward detector that is able to reconstruct multi-particle final states.  
 1838 For the full  $18 \times 275$  GeV beam energy, the products of light meson ( $\omega$ ,  $\rho$  or  $\pi^0$ ) mostly end up with  $\eta > 6.2$ , in  
 1839 the zero degree calorimeter (ZDC). At lower beam energies, or with heavier mesons, the products are at smaller  
 1840 pseudorapidity. This requires a forward detector with as full an acceptance as possible, *i.e.* with no holes in the  
 1841 acceptance) for both charged and neutral particles.

## 1842 G. Rare isotopes (including photons for spectroscopy)

1843 As discussed in the recent EIC Yellow Report, simulation studies suggest that the EIC has the potential to produce  
 1844 and detect rare isotopes along with their gamma photon decays, allowing this new machine to complement the results  
 1845 from dedicated rare isotope facilities.

1846 Direct detection of the rare isotopes will use the Roman Pot (RP) detectors. At first approximation, the produced  
 1847 rare isotopes will have the same momentum-per-nucleon as the ion beam and no angle relative to the beam. Under  
 1848 this approximation, the rigidity ( $R = p/Z$ ) of the isotope is directly related to its  $A/Z$  as

$$1849 \quad R_{Rel} = (R - R_{beam})/R = \Delta p/p = \left(\frac{A}{Z}\right) / \left(\frac{A_{beam}}{Z_{beam}}\right). \quad (41)$$

1850 Under the above assumption, the isotope's hit position in the dispersive direction at the RP gives a measurement  
 1851 of  $A/Z$ . Figure 36 shows the expected hit positions for known and predicted isotopes both at the first RP for the  
 1852 primary IR and at the first RP located near the secondary focus in the second IR, assuming a  $^{238}\text{U}$  beam. Isotopes  
 1853 with the same  $Z$  and different  $A$  values are shown at the same vertical position in the plots. In addition, using the  
 1854 beam parameters from table 3.5 of the 2021 EIC CDR [9] for heavy nuclei at 110 GeV/A on electrons at 18 GeV,  
 1855 the  $10\sigma$  beam exclusion are is shown by the gray box. As can be clearly seen, none of the heavy rare isotopes can be  
 1856 detected in the primary IR, while the second IR has the potential to detect the majority of the isotopes. At the  
 1857 RP in the second IR, isotopes with the same  $Z$  that differ by a single neutron are expected to be separated by 1.5  
 1858 mm for  $Z = 100$  and 5 mm for  $Z = 25$ .

1859 For uniquely determining the isotope, a direct measurement of  $Z$  is needed. The simplest way to do this is by  
 1860 placing a Cherenkov detector behind the RPs at the secondary focus. The number of Cherenkov photons produced  
 1861 by the isotope will be proportional to  $Z^2$ .

1862 Measuring gamma decay photons is also important as the level transitions reveal the structure of the final isotope.  
 1863 The photons are produced isotropically in the isotope's rest frame but can be Lorentz up-shifted significantly in the  
 1864 lab frame. This shift, as well as the requirement that these photons be detected in coincidence with an isotope, means  
 1865 that photon background will be small. LYSO crystals that do not require cryogenics can therefore be used for this  
 1866 measurement. In addition, while spectroscopy would benefit from a good photon acceptance, it would not be a critical  
 1867 requirement.

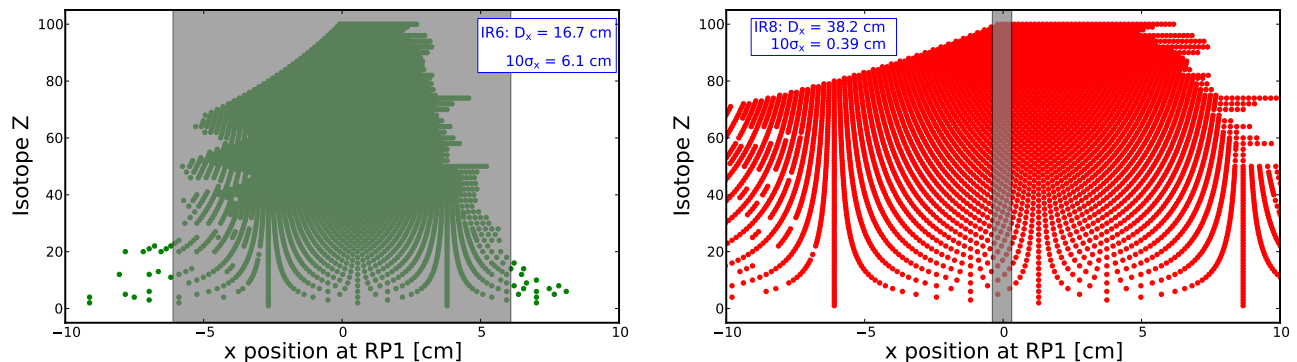


FIG. 36. Left: Isotope Z vs. hit position in the first RP for the primary IR; right: Isotope Z vs. hit position in the first RP at the secondary focus for the second IR. The gray box on each plot shows the  $10\sigma$  beam exclusion area. The plots are made assuming a  $^{238}\text{U}$  beam.

## VIII. RADIATIVE EFFECTS AND CORRECTIONS

### A. Introduction

QED radiative corrections (RC) are an integral part of the hadronic-structure studies with electron (or muon) scattering. In experiment, they can reach tens of per cent for unpolarized cross sections and several per cent for polarization asymmetries, while also altering dependence of observables on all kinematic variables of DIS ( $x, y, Q^2$ ) as well as altering dependence on azimuthal angles both in SIDIS and deep-exclusive reactions. Thus, they can become a significant source of systematics in a program of hadronic studies with EIC.

Significance of electromagnetic RC for analysis of scattering data should not be underestimated, as was clearly demonstrated by different outcomes of Rosenbluth and polarization methods for measurements of the proton electric form factor, see [478] for an overview. Current and planned experiments probing 3D hadronic structure require precise measurements of GPD and TMD contributions to cross sections and spin asymmetries that may be possibly obscured or altered by radiative effects. For this reason, proper inclusion of RC is one of priority tasks in experiment planning and data analysis.

Historically, the approach developed by Mo and Tsai in 1960s [479] was successfully applied for both DIS and elastic electron scattering on protons and nuclei. In 1970s Bardin and Shumeiko developed a covariant approach to the infra-red problem in RC [480] that was later applied to inclusive, semi-exclusive and exclusive reactions with polarized particles.

Emission of multiple soft photons is conventionally included via exponentiation [481]. A different approach for including higher-order corrections [482] uses a method of electron structure functions based on Drell-Yan representation that allows RC resummation in all orders of QED.

For high transferred momenta, such as in HERA or EIC, electroweak corrections have to be included. Corresponding formalism was developed for HERA [483, 484], while the codes presently used for JLab would have to be updated to include weak boson exchanges.

Higher precision of modern experiments presents new demands on the accuracy of RC. It is common to divide RC, in a gauge invariant way, into two categories, namely, model-independent and model-dependent. For model-independent RC, QED corrections do not involve extra photon coupling to a target hadron. Still, kinematics shifts due to extra photon emission require knowledge of hadronic response in off-set kinematics that can be handled either by iterative procedures, or existing data on the same reaction from other experiments, or input from theoretical models. On the other hand, model-dependent corrections correspond to extra photon exchange or emission by a target hadron. They require knowledge of hadronic structure beyond what can be learned in a considered experiment from a given reaction.

### B. Monte Carlo generators for radiative events

Classically, radiative corrections are applied to measured data post-hoc, i.e. a correction factor is calculated using analytical formulas and then multiplied onto the measured result, effectively mapping the measured radiative rate to an ideal Born-level rate (e.g. [479, 485]). On the other hand, to calculate a cross section, the detector acceptance is also required, and either calculated analytically from geometry, or integrated numerically using Monte Carlo methods.

This post-hoc application of a—typically analytically integrated—correction has limited precision, as it must necessarily make simplifying assumptions about the detector acceptance, more so since radiative processes beyond a peaking approximation can radically shift the event kinematics.

Therefore, the Monte Carlo algorithms, classically used to calculate the acceptance, were extended to include full cross section and reaction models including radiative corrections. The MC result, together with the luminosity, is then not a calculation of the acceptance, but of the expected count rate, and results of experiments are often presented as the ratio of the observed to predicted count rates. A proper implementation of this approach includes automatically all interactions between radiative corrections and other detector effects like bin-migration and detector acceptance, possibly even as a function of time. Such codes were developed for example for the HERA experiments H1 and ZEUS [483, 484].

Efficient MC simulations require a small variance of event weights. Radiative generators must overcome the fact that the radiative cross section varies by many orders of magnitude, with possibly multiple, unconnected regions of phase-space with high cross-section, for example for nearly collinear emission of photons along electron trajectories.

In these cases, naive rejection sampling methods show poor performance as only very few events are accepted. Automatic volume reweighting approaches like foams can in principle be effective, but suffer from the high derivatives near peaks. Efficient approaches therefore exploit the analytical structure of the underlying cross section to generate events efficiently.

For fixed target electron scattering experiments, many suitable codes for QED radiative corrections exist, however mostly limited to first-order approximations, sometimes improved by approximate higher-level corrections (see e.g. [481, 486–489]). Recently, true higher-order MC generators became available [490]. The validity of such generators has been tested deep into the radiative tail, recently for lower energies in [491].

The translation of these generators to collider kinematics is straight forward, with the caveat that numerical precision problems might crop up.

Beyond DIS reactions, the mapping of the radiative process back to the Born-level base process becomes tedious. The QED radiative Feynman graphs resemble QCD higher-order graphs, opening the door to a unified approach that can handle both QCD and QED radiative effects, and corresponding algorithms are currently being implemented in HEP generators [492]. Using the factorization theorem, the resummed leading logarithmic higher-order corrections can be described with distribution and fragmentation functions [493, 494]. Higher-order corrections are resummed in the form of parton showers, treating partons and photons on equal footing [495]. The approach has to be extended to include non-logarithmic higher order corrections.

### C. Opportunities to reduce model dependences

While QED radiative corrections seem straight forward to calculate, they often require external input and make model assumptions, for example about hadronic contributions. For example, recent experimental results on two-photon exchange, i.e. the next order of corrections for elastic scattering, are not particularly well predicted by current calculations (for an overview, see [478]), and are an open research topic in theory and experiment.

Whether semi-analytical or Monte Carlo approaches are chosen for RC calculations, it is important that integration over the phase space of the radiated photon is done with a realistic hadronic tensor, as pointed out in Ref.[496]. In particular, radiative tails from exclusive meson production can contribute to SIDIS or baryon resonance contributions would be enhanced due to kinematic shifts from the radiated photons. Uncertainties in large- $x$  behavior of PDF may also affect RC calculations. In order to address these problems, the hadronic physics community needs to maintain a comprehensive database of exclusive and semi-inclusive reactions, whereby JLab/EIC data from lower energies and momenta transfers would be used for RC calculations for highest EIC energies. Artificial Intelligence approaches may also be instrumental in developing multi-dimensional iterative procedures, especially for SIDIS. In particular, SIDIS measurements at lower-energy Interaction Point at EIC may be used as an input for RC calculations for higher energies of the same machine, thereby providing necessary energy coverage for self-consistent RC approaches. Extension of conventional PDF analysis to large Bjorken  $x$  values and studies of its impact on RC also have to be planned.

With an exception of elastic ep-scattering [478], most of approaches to exclusive electron scattering considered model-independent RC that include only coupling of the extra photon to lepton lines, see, e.g., Refs.[497, 498] for VCS and Ref.[499] for exclusive pion production. Importance of model-dependent RC - still unaccounted for - is indicated both by experiment and theory. The JLab experiment [500] measured DIS with a transversely polarized  $^3\text{He}$  target and revealed a few per cent spin asymmetry that only appears beyond Born approximation, and it is similar in magnitude to single-spin asymmetries due to T-odd effects arising from hadronic structure. Effects at a level of several per cent due to two-photon exchange were also predicted theoretically for exclusive electroproduction of pions [501, 502].

A collaborative effort between development of advanced models of hadronic structure, experimental data analyses

and RC implementation will aim to minimize experimental systematics on one hand and provide access to hadronic PDFs, TMDs and GPDs in kinematics otherwise not accessible in direct measurements. In this respect, dedicated workshops (e.g. [503]) help bring together experts across several fields and facilitate such collaborations.

## IX. ARTIFICIAL INTELLIGENCE APPLICATIONS

Artificial Intelligence (AI) is defined as a “machine-based system that can, for a given set of human-defined objectives, make predictions, recommendations or decisions influencing real or virtual environments” [504]. Among the topics that are grouped under the term AI, machine learning and autonomous systems are of particular importance for the EIC:

- Machine Learning (ML) represents the next generation of methods to build models from data and to use these models alone or in conjunction with simulation and scalable computing to advance research in nuclear physics. It describes how to learn and make predictions from data, and enable the extraction of key information about nuclear physics from large data sets. ML techniques have a long history in particle physics [505, 506]. With the advent of modern deep learning (DL) networks, their use expanded widely and is now ubiquitous to nuclear physics, as found promising for many different purposes like anomaly detection, event classification, simulations, or the design and operation of large-scale accelerator facilities and experiments [507, 508].
- Autonomous systems are of interest for monitoring and optimizing the performance of accelerator and detector systems without human control or intervention. This can include responsive systems that adjust their settings to background conditions as well as self-calibrating accelerator and detector systems. An ambitious goal is the usage of real-time simulations and AI over operational parameters to tune the accelerator for high luminosity and high degrees of polarization.

The EIC community has started to incorporate AI into the work on the physics case, the resulting detector requirements, and the evolving detector concepts. Initiatives such as AI4EIC and the related AI working group in the EIC User Group will work with the community to systematically leverage these methodologies during all phases of the project. AI4EIC aims at identifying problems where AI can have an impact and at finding solutions that can be cross-cutting for the EIC community. The initiative will create a database with benchmark datasets and challenges to allow testing new AI approaches and methods and compare to previous ones. An overarching research theme of the EIC community is the work towards an autonomous experiment with intelligent decisions in the data processing from detector readout and control to analysis.

AI will advance precision studies of QCD in both theory and experiment. A prominent examples is the applications of AI to the inverse problem of using measured observations to extract quantum correlation functions, e.g., with variational autoencoders (VAEs) that utilize a latent space principal component analysis to replicate lost information in the reconstruction of the posterior distribution [509]. Other examples are AI methods to accelerate simulations for the design of experiments and for nuclear femtography to image quarks and gluons in nucleons and nuclei.

### A. Accelerate Simulations with AI

Physics and detector simulations are being used to develop the physics case, the resulting detector requirements, and the evolving detector concepts for the experimental program at the EIC. The high-precision measurements envisioned for the EIC require simulations with high-precision and high accuracy. Achieving the statistical accuracy needed is often computationally intensive with the simulation of the shower evolution in calorimeters or the optical physics in Cherenkov detectors being prime examples. Fast simulations with parameterizations of detector response or other computationally efficient approximations that are pursued as alternative lack the accuracy required for high-precision measurements. Here, AI provides a promising alternative via fast generative models, e.g., generative adversarial networks (GANs) or VAEs.

A promising approach is AI-driven detector design where the parameters of detector and its costs are being tuned using Bayesian optimization. AI-driven detector design has been used for detector components [510] and recently for detector concepts [511].

### B. Nuclear Femtography and AI

Tomographic images of the nucleon, referred to as nuclear femtography, are critical for understanding the origin of the mechanical properties of the nucleon such as mass and orbital angular momentum decompositions into

2006 contributions from quark and gluon dynamics. The development of the new imaging methodology, deeply-virtual ex-  
 2007 clusive processes in electron scattering, and their dedicated exploration through the future EIC’s beam and detector  
 2008 technology, will make nuclear femtography a reality for the first time.

2009 Efficiently constructing the images from future large complex experimental data sets along with first principles  
 2010 constraints from large-scale numerical lattice-QCD calculations requires the exploration of an ensemble of advanced  
 2011 AI and ML techniques. In the case of studies of GPDs, the data analytic strategy to go from precisely understanding  
 2012 the performance of detectors in searching for high-energy diffractive events, through accurately extracting the Compton  
 2013 Form Factors as the key link between experimental data and the input for imaging construction, to generating the  
 2014 images through complex neural-network numerical regression that takes into account various physical constraints  
 2015 including direct lattice QCD results. To accomplish this, it is essential to assemble an interdisciplinary group of  
 2016 nuclear theorists and experimenters, along with computer scientists and applied mathematicians, to build the first  
 2017 AI/ML-based platform for the state-of-art nuclear sub-femto-scale imaging. The physical quantities connecting images  
 2018 and experimental data are Compton Form Factors (CFFs). To extract CFFs from data is complicated due to several  
 2019 CFF combinations corresponding to various quark-proton polarization configurations appearing simultaneously in the  
 2020 cross section terms for each beam and target polarization configuration. A neural-network (NN) approach, exploiting  
 2021 dispersion-relation constraints, was recently adopted to obtain the flavor-separated CFFs [51].

2022 Generally considered to offer the most robust and flexible method for multidimensional probability density esti-  
 2023 mation, Artificial Neural Networks (ANNs) represent a new paradigm to tackle this complex problem. Initial ANN  
 2024 applications to CFF extraction were reported in [19, 57, 512] using standard supervised NN architectures. The sys-  
 2025 tematic application of AI to the extraction of multidimensional structure functions is currently in its initial stages.  
 2026 Possibly the most crucial aspect of these methods is the treatment of uncertainties and their propagation from direct  
 2027 experimental observables (such as cross sections and asymmetries) to the densities of physics interest (such as the  
 2028 distributions of electric charge or forces). With emerging JLab 12 GeV data and beyond from various experimental  
 2029 sources, a suite of ML technologies will need to be explored to properly assess the optimal deep neural network  
 2030 architectures with proper treatment of uncertainty through robust UQ techniques. This ML strategy can also be  
 2031 systematically extended to extract the subleading CFFs once leading twist CFFs have been extracted with controlled  
 2032 uncertainties. in the future which is, in part, made a more tangible goal once we have a better extraction of the leading  
 2033 ones. We will systematically compare performances and the influence of various choices, such as the detailed structure  
 2034 and depth of the ANN, prior assumptions of the local variation of the CFFs with respect to the kinematic variables,  
 2035 and prior assumptions of the full determination of the number and type of contributing CFFs. A statistically rigorous  
 2036 analysis of the NN performance with respect to architecture (depth and width of the network), local variation of the  
 2037 CFFs with respect to the kinematic variables, and prior assumptions of the full determination of the number and  
 2038 type of contributing CFFs will need to be performed to fully quantify any systematic errors from using ANNs. With  
 2039 the goal of extracting all of the leading CFFs, one needs to develop eight independent ANNs, each with the goal of  
 2040 inputting experimental cross section data (e.g. DVCS asymmetries), and predicting a CFF with minimal bias.

### 2041 C. Inverse problems of quarks and gluons with AI

2042 Since quarks and gluons are not directly observable states of nature due to confinement, understanding their  
 2043 emergent phenomena such as hadron structure and hadronization from experimental data is unavoidably an inverse  
 2044 problem. Traditionally, ML techniques have been mostly applied in the form of regression that capitalize the model  
 2045 expressivity offered by ANN [455, 513]. In recent years however, a number of machine learning applications have been  
 2046 developed to tackle similar problems in nuclear physics, such as the reconstruction of neutron star equations of state  
 2047 from the observational astrophysical data [514–517], the deconvolution problem of the Kaellen-Lehmann equation [518],  
 2048 inverse Schroedinger equation solvers [519], inference on nuclear energy density functionals [520, 521], and quantum  
 2049 many-body calculations [522] (see the recent review in Ref. [508]). The emerging features of these applications includes  
 2050 ML-theory emulators that mitigate large scale computational costs for parameter searches [520, 521], generative models  
 2051 to improve Markovian sampling in lattice QCD [523], design of explainable ML architectures for parton showers [524]  
 2052 to mention few. Many of these applications are likely to cross pollinate the field of hadronic physics, and they will  
 2053 have a transformational impact for the scientific discoveries at the EIC.



## X. THE EIC INTERACTION REGIONS FOR A HIGH IMPACT SCIENCE PROGRAM WITH DISCOVERY POTENTIAL

### A. Introduction

The compelling science program of the EIC focusing on the low to medium CM energies has been described in this document. Here we describe the two interaction regions (IRs) dedicated to the experimental programs, and some of the important differences between them. The overall layout of the EIC is shown in Fig. 37.

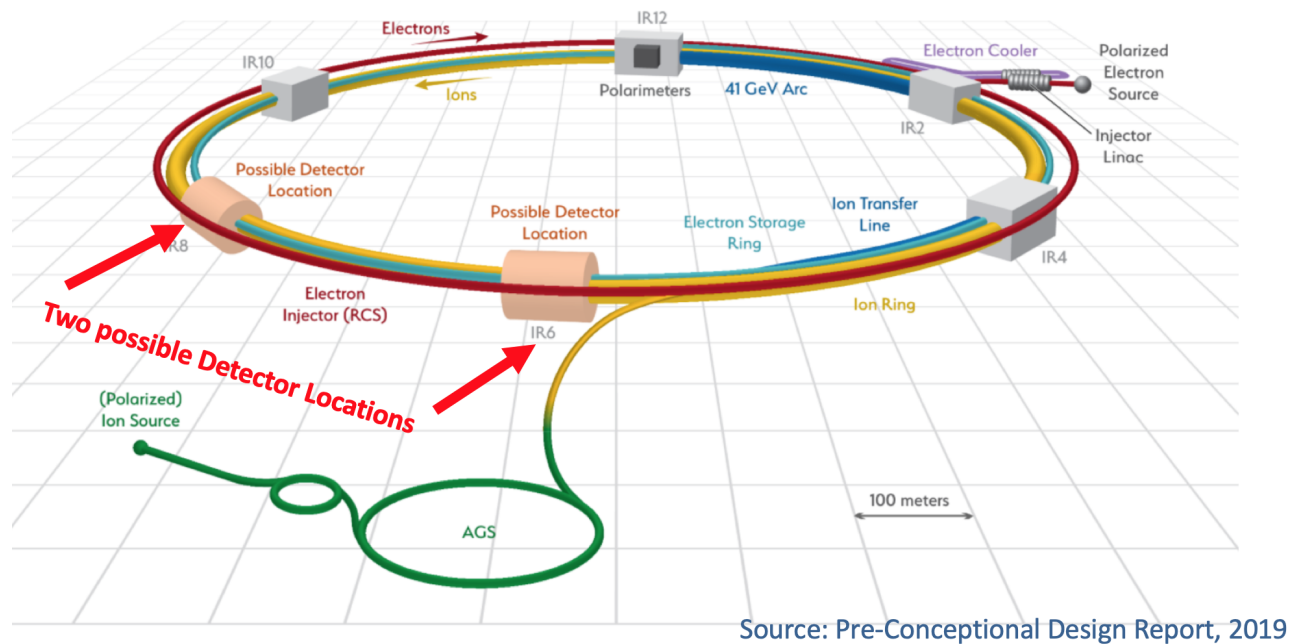


FIG. 37. The EIC layout at Brookhaven National Laboratory. Electron and the ion beams directions are identified in the upper left. There are several beam intersection points (IPs); the 6 o'clock (IP6) and 8 o'clock (IP8) locations are suitable for the installation and operation of large-scale detector systems, with appropriate existing infrastructure. IP8 may be most suitable for high-luminosity optimization at low to intermediate CM energies as well as for the installation of a secondary focus for forward processes requiring high momentum resolution. Both beams will be highly polarized, with proton and electron beam polarizations over 70%.

One of the EIC design requirements is the capability of having two IRs. The EIC configuration therefore includes two IRs where collisions will occur, and where substantial near-full-acceptance detectors may be installed. The two IRs are IR6 (for the primary IR at 6 o'clock) and IR8 (for the second IR at 8 o'clock). Here the RHIC clock location nomenclature is used, where the STAR detector is located in IR6 and PHENIX/sPHENIX detector is located in IR8.

IR6 and IR8 are not identical, nor are their existing experimental halls. RHIC and EIC bring beams together horizontally for collisions; in the arcs there is one "inner" beamline (closer to the arc center of curvature) and one "outer" beamline (further from the arc center of curvature). For the EIC, the IR6 crossing geometry is such that both beams cross from inner to outer beamlines (illustrated in Figure 38), while the IR8 crossing geometry is from outer to inner beamlines. Hence the primary IR6 layout requires less bending than the second IR layout at IR8. Other spatial layout and RHIC experimental hall structural design differences exist that are inherited by the EIC project.

The physical layout differences between IR6 and IR8, and their separate implementation timelines, permit them to be developed to enhance the overall facility science impact and discovery potential. For example, IR6 might deliver the highest luminosities at highest CM energies, while IR8 may be designed to provide higher luminosities at mid-range CM energies. The former would emphasize discovery potential such as gluon saturation, while the latter would emphasize rare exclusive processes for 3D nuclear imaging and mechanical properties.

This section first briefly describes the primary IR design, as defined in the EIC Conceptual Design Report (CDR) [9]. This section then outlines the present implementation of the second EIC IR at IR8, consistent with nuclear physics, accelerator, and engineering requirements. The second IR may also provide a different acceptance coverage than the

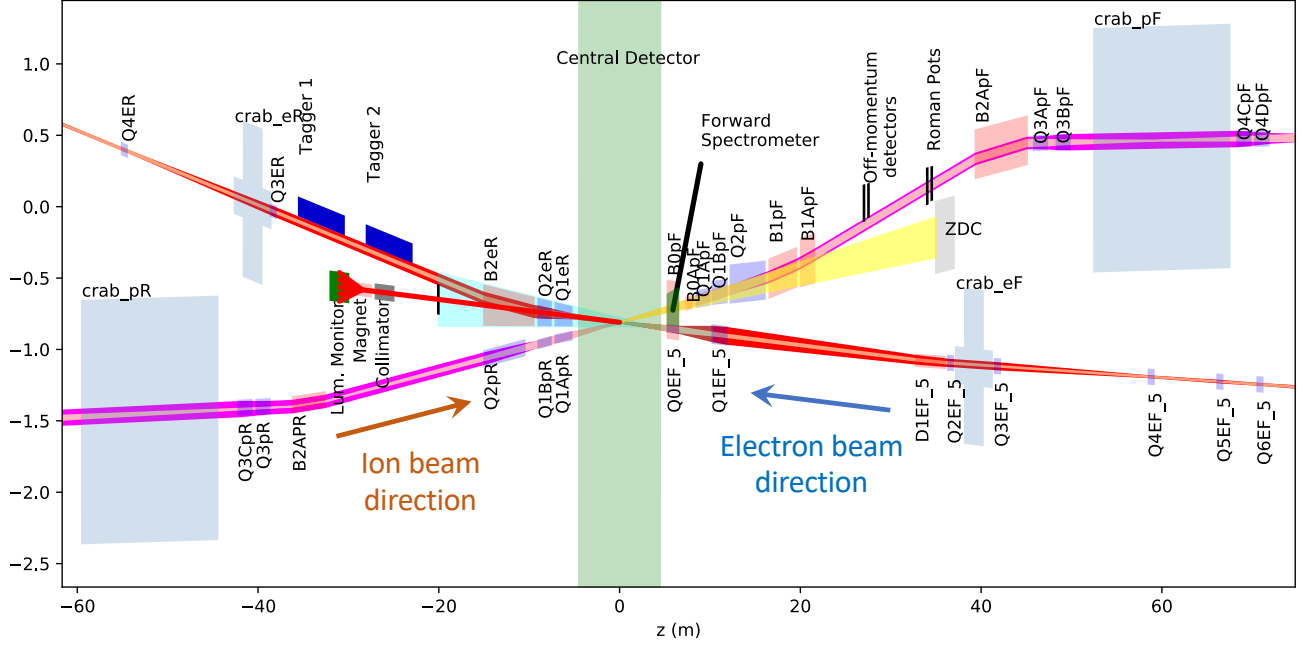


FIG. 38. Schematic top view of the EIC IR6 primary IR, in the high divergence configuration from the Conceptual Design Report [9] Figure 3.3. The y-axis positive direction points outward from the ring curvature; both beams cross from inner (negative y-axis) to outer (positive y-axis) beamlines.

2078 first IR. We include discussion of the operation of both IRs over the entire energy range of  $\sim 20\text{--}140$  GeV center of  
 2079 mass, and include consideration of different modes of two-IR EIC operations and their anticipated beam dynamics  
 2080 constraints.

2081

### B. Primary IR design parameters

2082 The luminosity and the design of the reference first EIC interaction region is optimized emphasizing the discovery  
 2083 potential of the EIC by providing the highest luminosity near the upper end of the CM energy range, from  $\sim 80\text{--}120$   
 2084 GeV, while covering the entire range of parameters required by the Nuclear Physics Long Range Plan. The  
 2085 parameter set and design is based on 1160 colliding bunches in each beam as described in the CDR [9]:

- 2086 • Peak luminosity of  $L = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  at a CM energy of 105 GeV;
- 2087 • Crossing angle  $\theta_c = 25$  mrad;
- 2088 • Maximum  $\beta$ -functions in the low- $\beta$  quadrupole magnets,  $\beta_{\text{max}} \leq 1800$  m (for protons in the vertical direction)  
 2089 and acceptable nonlinear chromaticity resulting in sufficient dynamic aperture;
- 2090 • IBS growth times in horizontal and longitudinal directions of  $\tau_{\text{IBS}} > 2$  hours.

2091 The design and layout of IR6 are reasonably mature, as illustrated in Figure 38.

2092

### C. Second IR design and downstream tagging acceptance

2093 The EIC requirements include sufficient flexibility to permit alternative optimizations of the two experimental IRs.  
 2094 For example, the IRs may be optimized for highest luminosities at different CM energies. Moreover, the two IRs and  
 2095 corresponding detectors may have acceptances and capabilities optimized for different parts of the physics program  
 2096 as described in this white paper.

2097 To first order, the luminosity at the IP is inversely proportional to the distance between the last upstream and  
 2098 first downstream final focus quadrupoles (FFQs). The statistical uncertainty of measurements in the central detector

2099 scales as this distance. However, the closer the beam elements are to the IP, the more they obstruct the acceptance  
 2100 at shallow angles with respect to the beam axis and restrict the acceptance for forward particles. The solenoidal  
 2101 field used in the central detector region to measure the high  $p_T$  particles in the central detector is not effective in  
 2102 determining the momenta of particles moving parallel to the beam direction, and additional fields are needed.

2103 From kinematics, the reaction products are biased towards small angles around the original ion beam. In particular,  
 2104 the detection of small-angle products requires acceptance to the recoiling target baryon (3D structure of the nucleon),  
 2105 hadrons produced from its breakup (target fragmentation), or all the possible remnants produced when using nuclear  
 2106 targets (including the tagging of spectator protons in polarized deuterium). The detection should be done over a  
 2107 wide range of momenta and charge-to-mass ratios with respect to the original ion beam. The second IR design should  
 2108 address these measurement difficulties posed by the beam transport elements.

2109 From machine design and luminosity considerations, it is not desirable to leave a very large detector space free  
 2110 of beam focusing elements to allow the small-angle products to accumulate sufficient transverse separation from the  
 2111 incident beams. The solution is to let the small-angle particles pass through the nearest elements of the machine  
 2112 final-focusing system, which simultaneously perform the function of angle and momentum analyzer for the small angle  
 2113 reaction products. Ideally, this forward detection system must be capable of accepting all reaction products that have  
 2114 not been captured by the central detector. In particular, similarly to the IR6 detector, this implies sufficiently large  
 2115 apertures of the forward ion final focusing quadrupoles to accommodate particle scattering angles from zero all the  
 2116 way up to the minimum acceptance angle of the central detector. Of course, detection of zero angle particles requires  
 2117 that they are outside of the beam stay-clear region in another dimension, namely, in the rigidity offset. The IR8  
 2118 design is particularly optimized for separation of such particles from the beam and their detection as described below.  
 2119 A significant challenge of this approach is to balance often contradictory detector and machine optics requirements.  
 2120 For example, the choice of the apertures of the forward ion final focusing quadrupoles, and therefore the forward  
 2121 angular acceptance, are a balance of the detection requirements and engineering constraints. One would like to make  
 2122 the apertures sufficiently large without exceeding the technical limits on the maximum aperture-edge fields.

2123 Figure 39 illustrates  $x_L - p_T$  acceptance with two successive improvements to second IR acceptance. Without  
 2124 forward spectrometry (left), the detection of low-angle scattered particles is limited by the beam divergence at the  
 2125 IP. By introducing forward spectrometry (center), this limit can be lowered, but particles with high rigidity  $x_L = 1$   
 2126 still escape detection. Adding a secondary focus point with flat dispersion (right) improves the  $x_L$  acceptance gap  
 2127 further.

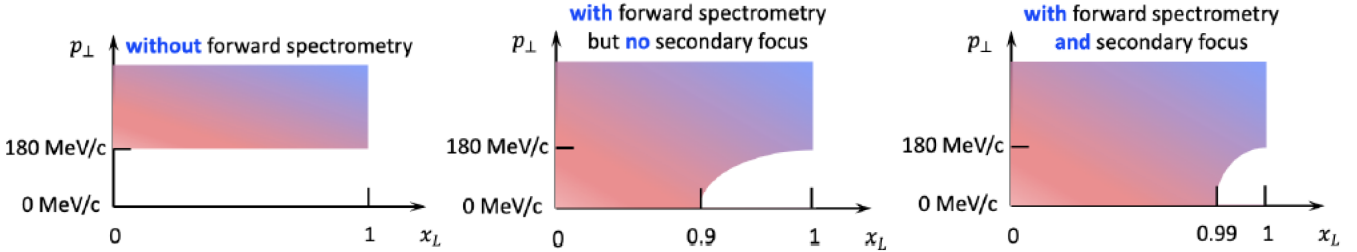


FIG. 39. Illustration of forward spectrometry and secondary focus effects on detector acceptance (shaded) in the  $x_L - p_T$  space for 275 GeV protons.

2128 The maximum detectable  $x_L$  at a point in the beam-line can be calculated to first order using,

$$2129 \quad x_L < 1 - 10 \frac{\sqrt{\beta_x^{2nd} \epsilon_x + D_x^2 \sigma_\delta^2}}{D_x}, \quad (42)$$

2130 where  $\beta_x^{2nd}$  is the Twiss  $\beta$ -function at the second focus,  $\epsilon_x$  is the horizontal beam emittance,  $D_x$  is the horizontal  
 2131 dispersion at the second focus, and  $\sigma_\delta$  is the beam momentum spread. At a point in the lattice with low  $\beta$  function  
 2132 and high dispersion  $D_x$ , one can reach the fundamental limit for the maximum  $x_L$  given by

$$2133 \quad x_L < 1 - 10\sigma_\delta. \quad (43)$$

2134 The present EIC second IR secondary focus design is very close to this theoretical limit. Further improvements are  
 2135 quite limited by space availability in the experimental hall and magnetic field constraints.

2136 The selection of crossing angle is an important design choice for the second IR. This crossing angle must not be too  
 2137 large ( $> \sim 50$  mrad) for various reasons:

- 2138 • Constraints from the existing experimental hall geometry.
- 2139 • The IP must be shifted towards the ring center to permit the RCS to bypass the detector.
- 2140 • Large crossing angle requires more aggressive crabbing, which in turn is limited by cost, impedance, and beam dynamics issues.
- 2141
- 2142 • Detector acceptance becomes unacceptably small at larger crossing angles.
- 2143 • Limits proximity of final focus quads and overall IR luminosity.

2144 The crossing angle must also not be too small ( $< \sim 25$  mrad), since the existing hall geometry requires spectrometer dipoles to bend towards the electron beam. Bending away as in the primary IR is not possible because of the second IR collision geometry. This pushes the second IR crossing angle away from the 25 mrad used in the primary IR. The second IR design choice of crossing angle is presently 35 mrad.

2148 Figure 40 shows the layout of the second IR with the proposed detector component placements. The ancillary detectors in the downstream hadron beam side have been integrated, while space is available for luminosity monitor, low  $Q^2$  tagger and local hadron polarimetry.

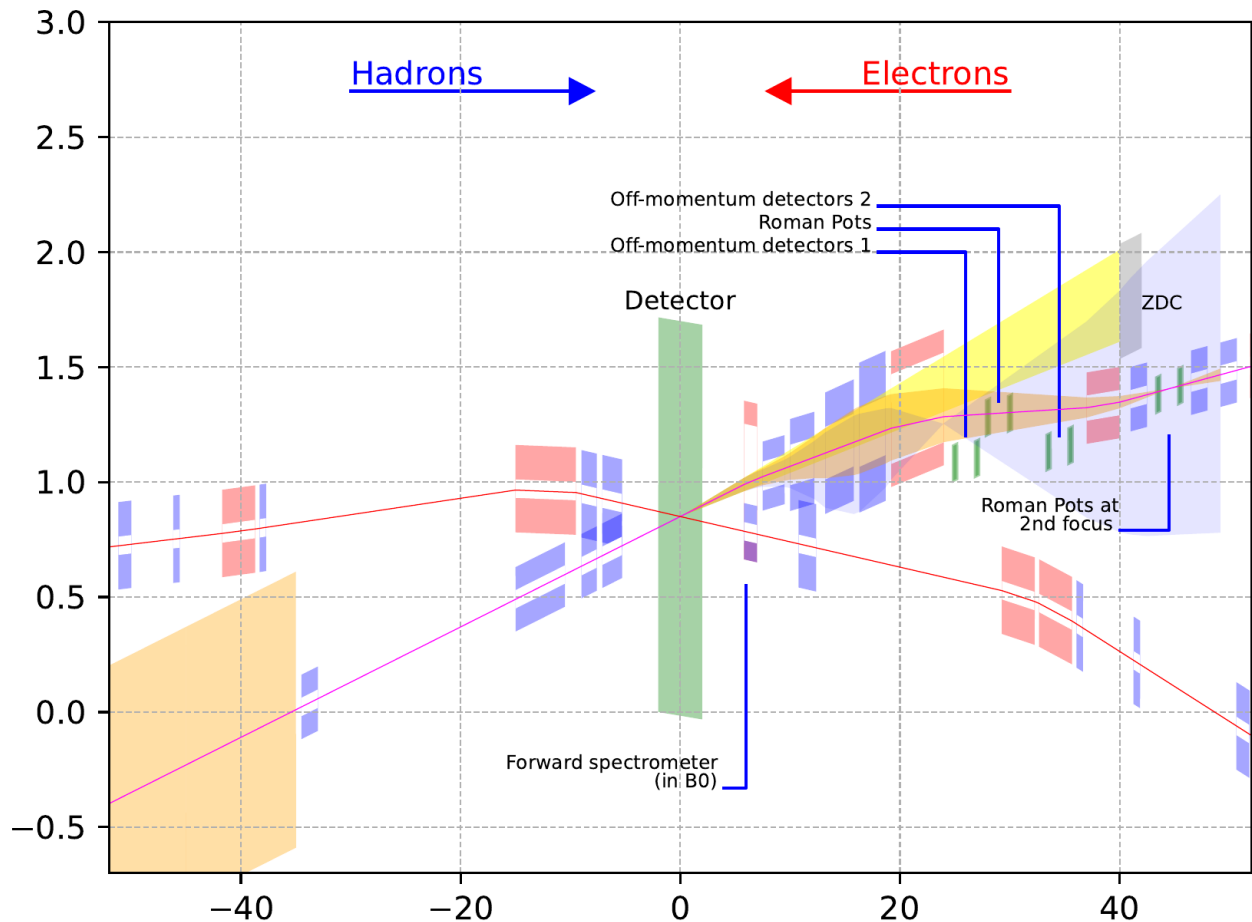


FIG. 40. Layout of the second IR with a 35 mrad crossing angle indicating locations of the main forward and auxiliary detector component. The color shaded areas show the  $\pm 5$  mrad  $p_T$  acceptance for particles with yellow representing neutrons while orange and blue represent protons with  $x_L = 1$  and 0.5 respectively.

## D. Technical design of an optimized low energy and high luminosity interaction region

The above detection requirements make the detector and machine designs intertwined and closely integrated. There is no longer a clear separation between the detector and machine components. Several detection parameters directly impact the design choices for the second IR and vice versa. The major parameters critical to both detector and machine aspects of the design are summarized in Table III. This table also provides a comparison of primary and second IR parameters. One of the important design differences is the inclusion of a secondary focus in the second IR to provide improved downstream tagging resolution as described in Section X C.

TABLE III. Summary of second IR design requirements and their comparison to the first IR.

#	Parameter	EIC IR #1	EIC IR #2	Impact
1	Energy range electrons [GeV] protons [GeV]	5–18 41, 100–275	5–18 41, 100–275	Facility operation
2	Crossing angle [mrad]	25	35	$p_T$ resolution, acceptance, geometry
3	Detector space symmetry [m]	-4.5/+4.5	-5/5.5	Forward/rear acceptance balance
4	Forward angular acceptance [mrad]	20	20–30	Spectrometer dipole aperture
5	Far-forward angular acceptance [mrad]	4.5	5	Neutron cone, Max. $p_T$
6	Minimum $\Delta(B\rho)/(B\rho)$ allowing for detection of $p_T = 0$ fragments	0.1	0.003–0.01	Beam focus with dispersion, reach in $x_L$ and $p_T$ resolution, reach in $x_B$ for exclusive proc.
7	RMS angular beam diver- gence at IP, h/v [mrad]	0.1/0.2	<0.2	Min. $p_T$ , $p_T$ resolution
8	Low $Q^2$ electron acceptance	<0.1	<0.1	Not a hard requirement

### 1. Design constraints

The design constraints for the second IR include:

- The second IR must transport both beams over their entire energy ranges with required path lengths. All second IR dipole magnets must have sufficient field integrals to provide the necessary bending angles keeping the IR footprint fixed from the lowest to the highest energy, while respecting geometric constraints of the existing infrastructure. The quadrupoles must also provide sufficient focusing to properly transport the beams over the entire energy range. Use of NbTi superconducting magnets implies that none of the second IR magnets can have aperture-edge fields higher than 4.6 T at highest beam energies; more complicated magnets, such as the B0 spectrometer, may be limited to significantly lower fields [9]. For collisions, the second IR magnets must have sufficient strengths to focus the beams at the IP while having sufficiently large apertures to meet the detection requirements discussed below. Simultaneous operation of the two IRs is also subject to the beam dynamics constraints discussed later.
- Consistent with the two detector complementarity approach, the second IR could be designed to provide a near flat luminosity above  $\approx 45$  GeV. This supports leveling of the EIC luminosity curve at a higher level over a wider energy range, as can be seen in Fig. 41. The second IR may also be designed to provide a different acceptance coverage than the first IR.
- The ion and electron beams cross at a relatively large angle of 35 mrad at the IP. High luminosity is preserved through the use of crab cavities. This angle moves the ion beam away from the electron beam elements and makes room for dipoles located just downstream of the central detector area. The dipoles serve two purposes. First, they shape the beam orbits providing their geometric match, making the IR footprint fit in the available detector hall and tunnel space, and creating room for detectors. Second, the dipole systems allow momentum analysis of the particles with small transverse momentum with respect to the beams. Particles with large transverse momenta are analyzed using the solenoidal field and the B0 magnet in the central detector.

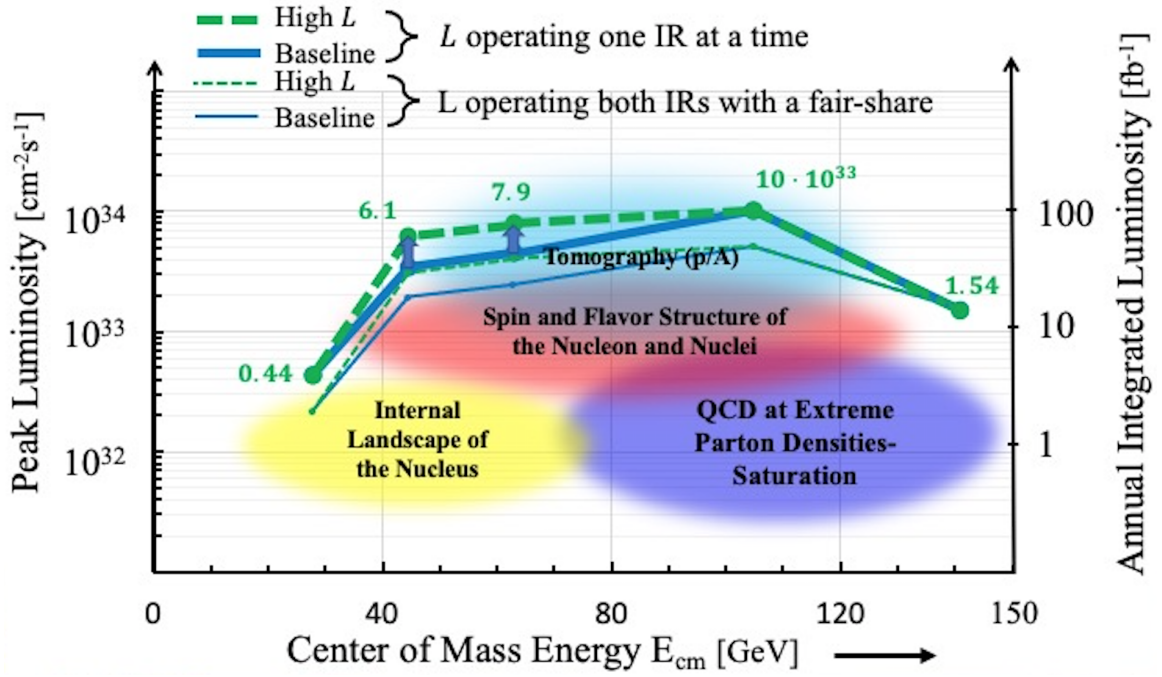


FIG. 41. Estimated luminosity versus CM energies for the operation of one (thick lines) or two (thin lines) interaction regions. The blue lines show estimates of the reference luminosity. The green lines show the high luminosity operation with potentially improved beam optics and cooling at lower CM energies. (As shown in [525])



FIG. 42. Apparent horizontal broadening of the beam spot size at the IP due to the crab tilt. Blue left: RMS hadron bunch length  $\sim 10\text{cm}$ , red middle: Looking along the beam with no crabbing, and red right: What the RP sees  $\sim 1.25\text{mm}$ .

2181

## 2. Effect of horizontal crabbing in secondary focus

2182 Since the secondary focus is within the region where the hadron beam is crabbed, hadron crabbing effectively  
 2183 broadens the horizontal beam spot size seen by the Roman Pot (RP) detectors in the secondary focus, as illustrated  
 2184 in Figure 42. This beam spot size is one of the sources of uncertainty in a  $p_T$  measurement. Ignoring for the moment  
 2185 other sources such as the beam angular spread at the IP, the transverse position of a scattered particle at an RP  $x_{RP}$   
 2186 is related to  $p_T$  as

$$2187 \quad x_{RP} = M_{11}x_{IP} + M_{12}p_T/p, \quad (44)$$

2188 where  $x_{IP}$  is the scattered particle's transverse position at the IP and  $p$  is the beam momentum.  $M_{11}$  and  $M_{12}$  are  
 2189 elements of the linear beam transfer matrix from the IP to the RP known from the magnetic optics design:

$$2190 \quad M_{11} = \sqrt{\beta_{RP}/\beta_{IP}} \cos \Delta\Psi, \quad (45)$$

$$2191 \quad M_{12} = \sqrt{\beta_{RP}\beta_{IP}} \sin \Delta\Psi,$$

2192 where  $\beta_{RP}$  and  $\beta_{IP}$  are the Twiss  $\beta$ -functions at the RP and IP, respectively, and  $\Delta\Psi$  is the betatron phase advance  
 2193 from the IP to the RP. The measured  $p_T$  can be expressed as

$$2194 \quad p_T = p \frac{x_{RP}}{\sqrt{\beta_{RP}\beta_{IP}} \sin \Delta\Psi} - p \frac{1}{\beta_{IP}} \frac{\cos \Delta\Psi}{\sin \Delta\Psi} x_{IP}. \quad (46)$$

2195 Since it is challenging to measure  $x_{IP}$  precisely, the second term on the right-hand side of the above equation represents  
 2196 a measurement uncertainty

$$2197 \quad \Delta p_T = \left| p \frac{1}{\beta_{IP}} \frac{\cos \Delta\Psi}{\sin \Delta\Psi} x_{IP} \right|. \quad (47)$$

2198  $x_{IP}$  consists of a random betatron component  $x_\beta$  and a longitudinal-position-correlated component  $z\theta/2$ :

$$2199 \quad x_{IP} = x_\beta + z\theta/2, \quad (48)$$

2200 where  $z$  is the particles longitudinal position from the center of the bunch and  $\theta$  is the total beam crossing angle.

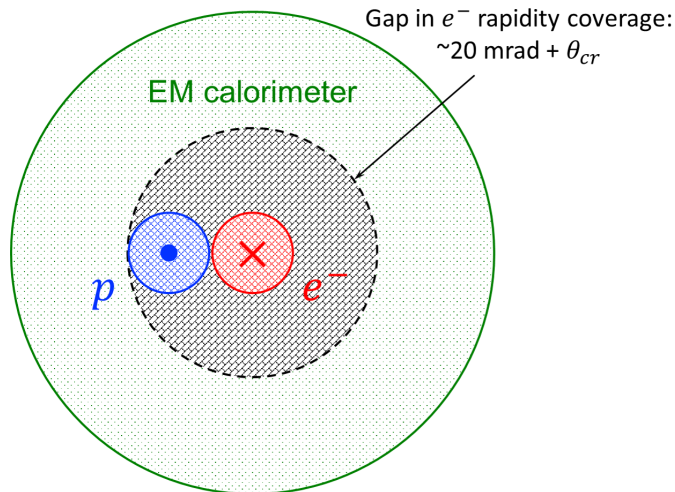
2201 The second term in Equation 48 describes the beam spot size smear. It is typically much greater than the first  
 2202 term. Therefore, the uncertainty term in Equation 47 can be greatly reduced by measuring the event's  $z$  position. It  
 2203 has been suggested that, with a feasible RP timing of  $\sim 35$  ps, the  $z$  position can be resolved down to  $\sim 1$  cm.

2204 Another factor in the uncertainty term of Equation 47 is  $\cos \Delta\Psi$ . By placing the RP at a position with  $\Delta\Psi$  close to  
 2205  $\pi/2$ ,  $\Delta p_T$  in Equation 47 can in principle be made arbitrarily small. There may be practical considerations limiting  
 2206 the available choice of  $\Delta\Psi$  such as the requirement of placing the RP before the crab cavities, which have small  
 2207 apertures and kick the particles. In the presented design of the second IR,  $\Delta\Psi$  is adjusted as close to  $\pi/2$  at the RP  
 2208 as allowed by other constraints to minimize  $\Delta p_T$ .

2209 Physics simulations set a requirement on the contribution of the crabbing tilt to  $\Delta p_T$  of

$$2210 \quad \Delta p_T < 20 \text{ MeV}. \quad (49)$$

2211 Another issue with the size of the crossing angle is that it contributes to the gap in the electron rapidity coverage



2212 FIG. 43. Gap in the electron rapidity coverage due to the crossing angle and the ion beam pipe. The blue and red circles  
 2213 represent the ion and electron beam pipes at the EM calorimeter location. The black dashed circle outlines the solid angle  
 2214 without full azimuthal detector acceptance.

2215 in the rear direction as illustrated in Figure 43. There is no full azimuthal coverage within an angle defined by the  
 2216 crossing angle and the size of the ion beam pipe. Assuming 5 cm for the radius of the ion beam pipe at a 2.5 m distance  
 2217 in the rear direction from the IP, the total polar angle of the gap in the rapidity coverage is about  $20 \text{ mrad} + \theta_{cr}$ .  
 2218 There is also a subtle point worth mentioning regarding the impact of the crabbing on the RP resolution, and the  
 2219 advantage of measuring both the vertex  $z$ - and the time-coordinates.  $Z$ -coordinates will be measured by the MAPS  
 2220 Si vertex tracker. However, if the vertex is measured e.g.  $z = +5 \text{ cm}$ , this does not determine if the collision happened  
 2221 at the leading edges of the two bunches (with mean  $x$  displaced in negative direction) or at the trailing edges of the  
 2222 collision (with mean  $x$  displaced in positive direction). This is where the time measurement comes in, to determine  
 where in the longitudinal profile of the crab the event happened.

## 2223 E. Operations with Two IRs

2224 In the period of the EIC project, the second IR (IR8) will have no detector and no capability of being tuned for  
 2225 collisions. All operations will focus on beam parameter, luminosity, and polarization optimization for the single IR

2226 and detector that are part of the project scope.

2227 Operations of the EIC later, with two IRs, involves multiple scenarios, each with beam dynamics and design  
2228 constraints that involve tradeoffs of available luminosity, operations time, and mode switching. The beam-beam  
2229 force is the local nonlinear electromagnetic force colliding beams exert on each other; this force creates a nonlinear  
2230 beam-beam tune shift that is a known limitation of many collider operations. This beam-beam tune shift is already  
2231 optimized in the single-IR EIC design. Thus both IRs cannot operate simultaneously with full parameters necessary  
2232 for maximum luminosity, as this would exceed the acceptable beam-beam tune shift limit. It is therefore infeasible to  
2233 add net luminosity available to experiments by adding an IR in the EIC under optimized collider conditions where  
2234 the beam-beam tune shifts limit integrated luminosity.

2235 There are two alternatives to EIC operations with two IRs: EIC luminosity can be maximized separately for each  
2236 detector in dedicated runs where only one IR is tuned for collisions; or EIC luminosity can be shared and optimized  
2237 as much as possible between the two IRs in runs where both IRs are set up to share total facility luminosity.

2238 The separate luminosity scenario is technically straightforward. The non-luminosity IR would be detuned to reduce  
2239 chromatic effects, and beams would be steered to avoid collisions at that IR. For each run, the overall facility would  
2240 then be optimized to maximize operational parameters necessary to optimize the science program for the given run  
2241 time at the operating IR.

2242 The shared luminosity scenario is technically more complicated. Section 4.6.4 of the EIC CDR [9] includes a  
2243 section titled “Beam-beam Effects with Two Experiments” (pages 431–3) that describes one possibility for luminosity  
2244 sharing. This involves design choices in the facility, and placement of the second IR and experiment in IR8, to enable  
2245 an operating configuration that collides half the bunches at each of IR6 and IR8. Each individual bunch experiences  
2246 only one collision per turn, so the total beam-beam tune shift limit for each bunch is respected. This CDR section  
2247 also indicates that long-range beam-beam effects (present when beam timing is adjusted to share luminosity) may  
2248 further limit the total luminosity available at both IRs.

2249 The shared luminosity scenario may have other beam dynamics limitations (such as limitations of global chromatic  
2250 correction) that would further limit the total available combined luminosity to both experiments. These beam  
2251 dynamics considerations are being studied in the context of EIC second IR design and overall EIC lattice design  
2252 optimization. Figure 41 shows this best-case scenario as the “fair-share” curves, representing a 50% sharing of total  
2253 luminosity between the two IRs.



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